

③A

 $RV \rightarrow KA$ 

$$(a+b)^* \cdot ab = V_0 \quad \times$$

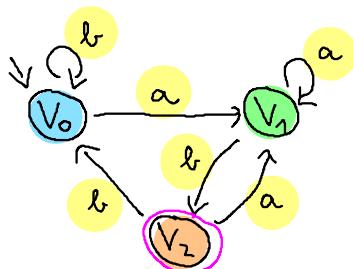
$$\frac{dV_0}{da} = [(a+b)^* ab + b] = V_1 \quad \times$$

$$\frac{dV_0}{db} = (a+b)^* ab = V_0$$

$$\frac{dV_1}{da} = (a+b)^* ab + b = V_1$$

$$\frac{dV_1}{db} = [(a+b)^* ab + \varepsilon] = V_2 \quad \checkmark$$

$\uparrow \varepsilon \in L(V_2)$



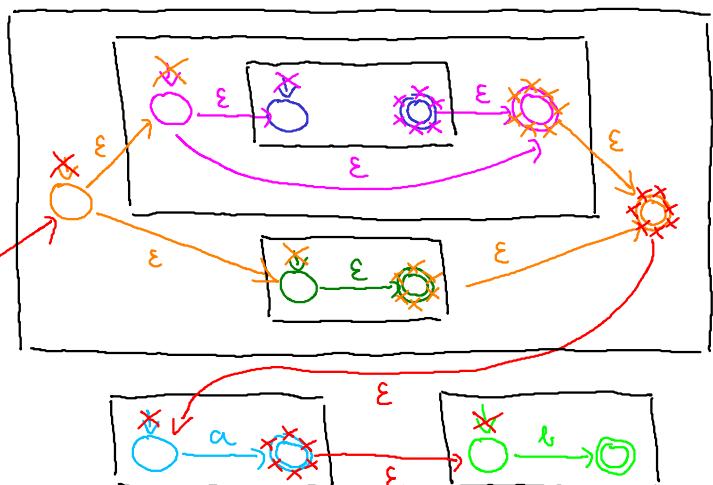
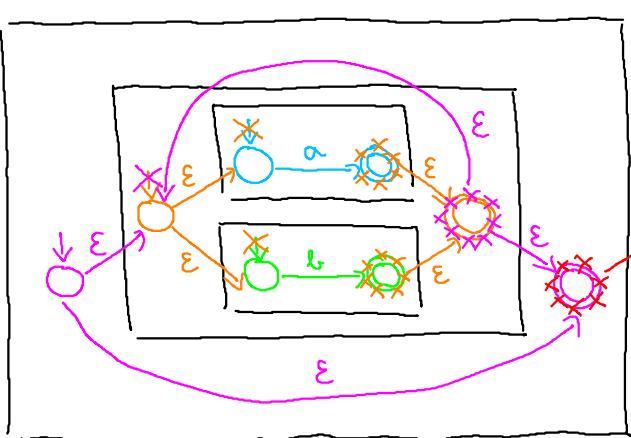
$$\frac{dV_2}{da} = (a+b)^* ab + b = V_1$$

$$\frac{dV_2}{db} = (a+b)^* ab = V_0$$

③C

 $RV \rightarrow KA$ 

$$(a+b)^* \cdot (\phi^* + \varepsilon) \cdot a \cdot b$$



(4A)  $KA \rightarrow RV$  PRR

	0	1	2
$\leftarrow \rightarrow A$	$\{A\}$	$\{B\}$	$\{B\}$
$\leftarrow B$	$\{B\}$		

$$A = OA + 1B + 2B + \varepsilon$$

$$B = OB + \varepsilon$$

$$B = O^* \cdot \varepsilon = O^*$$

$$A = OA + (1+2)O^* + \varepsilon$$

$$A = O^* [ (1+2)O^* + \varepsilon ]$$

(4B)  $KA \rightarrow RV$  LRR

	0	1	2
$\leftarrow \rightarrow A$	$\{A\}$	$\{B\}$	$\{B\}$
$\leftarrow B$	$\{B\}$		

$$A = AO + \varepsilon$$

$$B = A1 + A2 + BO$$

$$A = \varepsilon \cdot O^* = O^*$$

$$B = O^*(1+2) + BO$$

$$B = O^*(1+2)O^*$$

$$A + B = O^* + O^*(1+2)O^* = O^* [ \varepsilon + (1+2)O^* ]$$

(5)  $RG \rightarrow RV$  PRR

$$\Rightarrow S \rightarrow OS | 1A | 1$$

$$A \rightarrow 2A | 0$$

$$S = OS + 1A + 1$$

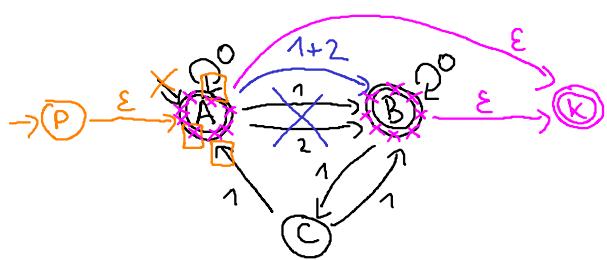
$$A = 2A + 0$$

$$A = 2^* 0$$

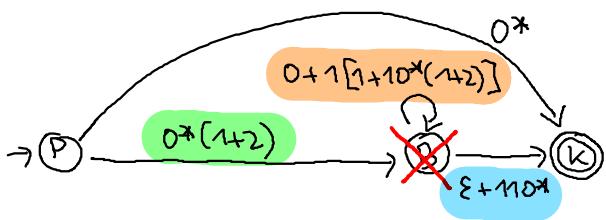
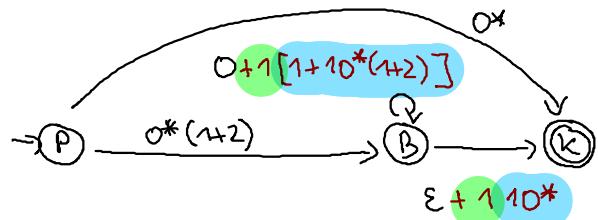
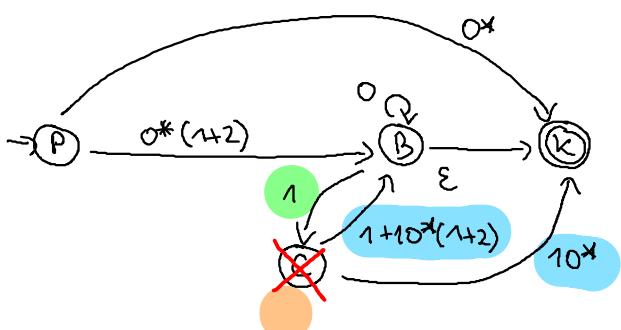
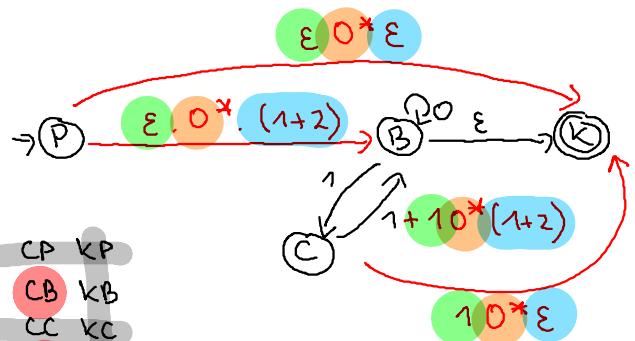
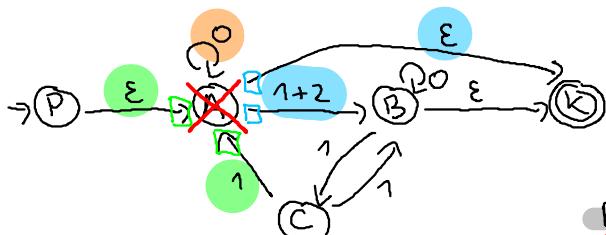
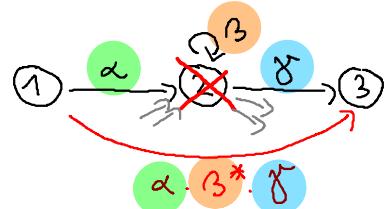
$$S = OS + 12^* 0 + 1$$

$$S = O^* ( 12^* 0 + 1 )$$

⑤  $KA \rightarrow RV$



$$1 \xrightarrow{\alpha} 2 \quad 1 \xrightarrow{\alpha} 2$$



$$O^* + O^*(1+2) \{ O+1[1+10^*(1+2)] \}^{*} [ \epsilon + 110^* ] =$$

$$\Rightarrow P \longrightarrow K$$

⑦

 $RG \rightarrow RV$ 

$$\begin{aligned} &\rightarrow S \rightarrow \epsilon A \\ &\cancel{\rightarrow A \rightarrow 0C | 0D | \epsilon K} \\ &B \rightarrow 1B | 2B \quad (1+2)B \\ &C \rightarrow 2B | 0C | 1K \\ &D \rightarrow 0C \\ &K \rightarrow \epsilon \end{aligned}$$

$$\begin{aligned} &\rightarrow S \rightarrow \epsilon A \\ &\cancel{A \rightarrow 0C | 0D | \epsilon K} \\ &B \rightarrow (1+2)B \\ &\cancel{X \rightarrow 2B | 0C | 1K} \\ &D \rightarrow 0C \\ &K \rightarrow \epsilon \end{aligned}$$

$$\begin{aligned} &\rightarrow S \rightarrow \epsilon A \\ &A \rightarrow OD | 00^* 2B | (\epsilon + 00^* 1)K \\ &\cancel{X \rightarrow (1+2)B | \phi} \\ &D \rightarrow 00^* 2B | 00^* 1K \\ &K \rightarrow \epsilon \end{aligned}$$

$$\begin{aligned} &\rightarrow S \rightarrow \epsilon A \\ &A \rightarrow OD | (\epsilon + 00^* 1)K \\ &\cancel{X \rightarrow 00^* 1K | \epsilon D} \\ &K \rightarrow \epsilon \end{aligned}$$

$$\begin{aligned} &\rightarrow S \rightarrow \epsilon A \\ &\cancel{X \rightarrow (\epsilon + 00^* 1)K} \\ &K \rightarrow \epsilon \end{aligned}$$

$$\begin{aligned} &x \rightarrow \alpha Y \\ &x \rightarrow \alpha Y \\ &\rightarrow S \rightarrow \alpha K \quad \alpha = \\ &K \rightarrow \epsilon \end{aligned}$$

$$\begin{aligned} &\rightarrow S \rightarrow \epsilon A \\ &A \rightarrow OD | \epsilon K | 00^* 2B | 00^* 1K \\ &B \rightarrow (1+2)B \\ &D \rightarrow 00^* 2B | 00^* 1K \\ &K \rightarrow \epsilon \end{aligned}$$

$$\begin{aligned} &\rightarrow S \rightarrow \epsilon A \\ &A \rightarrow OD | (\epsilon + 00^* 1)K \\ &D \rightarrow 00^* 1K \\ &K \rightarrow \epsilon \end{aligned}$$

$$\begin{aligned} &\rightarrow S \rightarrow \epsilon A \\ &A \rightarrow (\epsilon + 00^* 1)K | 00^* 1K \\ &K \rightarrow \epsilon \end{aligned}$$

$$\begin{aligned} &\rightarrow S \rightarrow \epsilon (\epsilon + 00^* 1)K \\ &K \rightarrow \epsilon \end{aligned}$$

$$\begin{aligned} &\rightarrow S \rightarrow (\epsilon + 00^* 1)K \quad \epsilon + 00^* 1 \\ &K \rightarrow \epsilon \end{aligned}$$