

# NDBI021 User preferences

substantially modified this year

One third Peter Vojtáš, KSI MFF UK

11/14 Introduction

remaining thirds Lád'a Peška, KSI MFF UK

# Outline of this part of lectures

- Substantially modified this year – this course follows on the NSWI166 (previous NDBX021, NDBI037 can be consulted)
- Motivation remains
  - User requirements (implicit/explicit) – possibly conflicting, multicriterial
  - (partly) linear models to enable lab paper solutions
- What is new
  - building a larger portfolio of aggregation models for testing which fits better to user modelling (pure heuristic)
  - More emphasis to visual part ...
- We begin with fast repetition of LMPM - Linear Monotone Preference Model + upgrade to 4D ...
  - Data cube, Preference cube, contour lines, top-k, ...
- First lab on paper solutions

# Multicriterial conflicting requirements – No such product

## Do any of these come close?

Price  -

In Stock

Order status  All  Brand New  Unwrapped, Nearly New and Used

Brands  Acer (0)  Apple (0)  ASUS (0)  Dell (0)  HP (0)  Lenovo (0)  MSI (0)

Next 2

Display size  -

Colour

Processor type  Intel Core i7 (0)  Intel Core i5 (0)  Intel Core i3 (0)  AMD Ryzen 5 (0)  AMD Ryzen 3 (0)

Next 8

Size of operational RAM  -

Storage Type  SSD (0)  HDD + SSD (0)  HDD + Opta... (0)  HDD (0)  Flash (0)

Storage capacity  -

Professional Laptops **f t m**

Display size from 14" to 17.3" X

Size of operational RAM from 8 GB to 32 GB X

Storage capacity from 1,500 GB to 2,000,000 GB X

Clear selected Parameters

Professional Laptops we will display

**Specify category**

0 Results

**No matching products.**

Professional Laptop

Office

RTX Studio

Extended Warranty

How to choose a laptop

Modify Results

Radius

Minimum Year

Maximum Year

Minimum Price

Maximum Price

Mileage

Style  AWD / 4WD  Commercial  Convertible

Your Search | Save search

Certified X SUV / Crossover X Min Year: 2000 X Max Year: 2016 X

Min Price: \$10,000 X Max Price: \$14,000 X Mileage: Under 30,000 X

Automatic X





Edit this search | Start a new search

Sort by Price - Lowest Per page 25 Page 1 of 1

**Sorry, we couldn't find your dream car.**

We can alert you as soon as one is available. Just save this search and set up alerts with My Autotrader.

**Do any of these come close?**

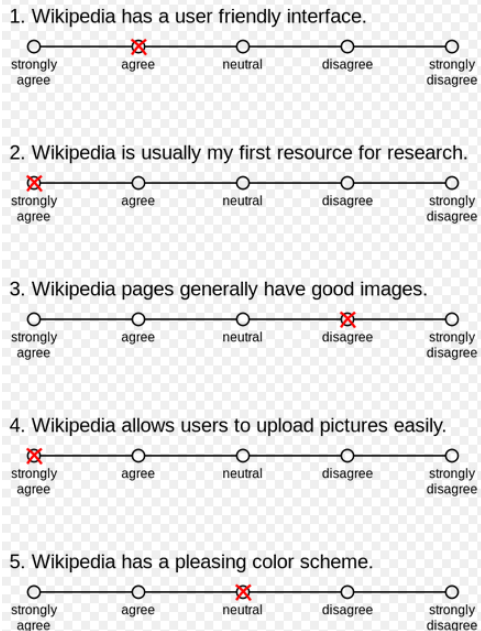
 <p>CALL NOW: (888) 306-0830</p> <p>2011 Nissan Juke \$13,000</p>	 <p>Sneak Peek</p> <p>2014 Jeep Compass \$13,493</p>	 <p>2016 Jeep Patriot \$13,994</p>	 <p>2014 Jeep Patriot \$13,990</p>
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**Close! How to measure it?**

# Preference – human, intuitive, ...scaled

- IT - more and more about the people and for the people
- Quality – in the language (good, better, best, bad, worse worst), we sense the visual stimuli in the environment – e.g., depth and motion - step-wise, psychology Likert's scale, we will represent ordering by numbers (ratings)

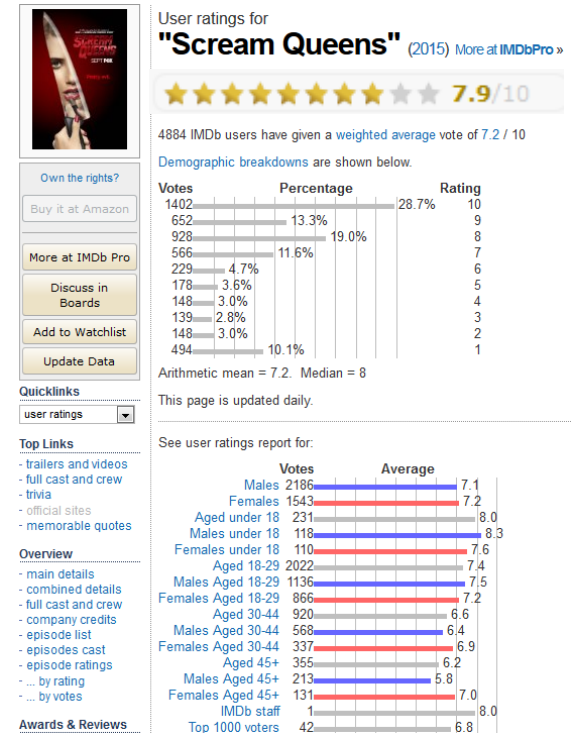
## Example Likert Scale



NDBIO21 User Preferences  
Vojtaš 11/14



Introduction



# Decathlon data – scale-points, multicriterial

P	Athlete	Points	P	100m	P	Long	P	Shot	P	High	P	400m	P	110mh	P	Discus	P	Pole	P	Javeli n	P	1500m
1	Šebrle CZE	9026		110,64	1	8.11	4	15.93	1	2.12		246,89	1	13,92	4	48.53	2	5.3	1	70.16		54.21,85
2	Nool EST	8604		410,66	2	7.8	3	15.83	5	2.12		847,70	3	13,99	1	47.92	4	5.2	6	68.15		14.21,98
3	Dvorak CZE	8527		210,73	3	7.69	9	15.67	7	2.06		147,79	4	14,22	3	46.74	11	5.1	2	66.94		124.26,13
4	Lobodin RUS	8465		1710,76	8	7.49	1	15.33	12	2.03		948,01	7	14,30	5	46.73	10	5	3	66.66		104.27,65
5	Zsivoczky HUN	8173		310,84	6	7.39	8	15.16	4	2		1448,67	10	14,30	7	46.61	12	5	14	63.93		114.31,69
6	Ambrosch AUT	8122		1010,87	11	7.35	16	15.1	13	2		348,76	9	14,36	9	46.41	9	4.9	15	61.65		34.33,58
7	Kürtösi HUN	8099		1410,89	4	7.32	10	14.85	2	1.97		1748,76	2	14,46	11	44.07	1	4.8	5	60.57		44.35,97
8	Warners NED	8085		810,90	5	7.19	7	14.77	3	1.97		1048,77	8	14,48	2	43.32	6	4.8	16	59.97		64.36,36
9	Hämäläinen FIN	8028		610,93	12	7.17	6	14.71	14	1.97		548,81	6	14,56	8	41.64	8	4.8	7	59.83		24.39,11
10	Jensen NOR	8004		910,99	7	7.16	17	14.67	15	1.97		448,91	12	14,61	12	41.56	3	4.7	10	58.51		164.40,22
11	Schönbeck GER	7891		1310,99	9	7.11	5	14.6	6	1.94		749,07	14	14,70	15	41.3	7	4.7	17	58.23		84.42,47
12	Niklaus GER	7891		511,01	13	7.11	2	14.37	8	1.94		1349,26	15	14,83	14	41.14	15	4.6	11	58.11		94.42,66
13	Tebbich AUT	7632		1611,03	10	6.94	11	14.17	16	1.94		649,33	17	14,97	10	40.38	5	4.5	8	55.62		134.46,57
14	Llanos PUR	7613		711,08	15	6.93	13	13.78	9	1.91		1649,90	11	15,06	13	40.18	13	4.5	4	54.56		154.47,22
15	SchnallingerA UT	7576		1211,09	14	6.89	14	13.67	11	1.88		1250,14	13	15,07	6	39.52	17	4.4	13	54.32		174.48,52
16	Walser AUT	7546		1111,31	17	6.83	12	12.99	10	1.85		1550,25	16	15,27	16	39.45	16	4.2	12	51.95		74.49,58
17	Walser AUT	7506		1511,35	16	6.81	15	12.98	17	1.82		1150,51	5	15,43	17	37.2	14	4.1	9	50.33		144.59,38

# Decathlon points-commeasurable

P	Athlete	Points	P	100m	P	Long	P	Shot	P	High	P	400m	P	110mh	P	Disc	P	Pole	P	Javelin	P	1500m
1	Šebřle CZE	9026	1	942	1	1089	4	847	1	915	2	964	1	985	4	840	2	1004	1	892	5	799
2	Nool EST	8604	4	938	2	1010	3	841	5	915	8	924	3	976	1	827	4	972	6	861	1	798
3	Dvorak CZE	8527	2	922	3	982	9	831	7	859	1	919	4	946	3	803	11	941	2	843	12	770
4	Lobodin RUS	8465	17	915	8	932	1	810	12	831	9	909	7	936	5	803	10	910	3	839	10	760
5	Zsivoczky HUN	8173	3	897	6	908	8	800	4	803	14	877	10	936	7	800	12	910	14	797	11	734
6	Ambrosch AUT	8122	10	890	11	898	16	796	13	803	3	873	9	929	9	796	9	880	15	763	3	721
7	Kürtösi HUN	8099	14	885	4	891	10	780	2	776	17	873	2	916	11	748	1	849	5	746	4	706
8	Warners NED	8085	8	883	5	859	7	776	3	776	10	872	8	913	2	732	6	849	16	737	6	703
9	Hämäläinen FIN	8028	6	876	12	854	6	772	14	776	5	870	6	903	8	698	8	849	7	735	2	686
10	Jensen NOR	8004	9	863	7	853	17	769	15	776	4	866	12	897	12	696	3	819	10	715	16	679
11	Schönbeck GER	7891	13	863	9	840	5	765	6	749	7	858	14	886	15	691	7	819	17	711	8	665
12	Niklaus GER	7891	5	858	13	840	2	751	8	749	13	849	15	870	14	688	15	790	11	709	9	664
13	Tebbich AUT	7632	16	854	10	799	11	739	16	749	6	846	17	853	10	672	5	760	8	672	13	640
14	Llanos PUR	7613	7	843	15	797	13	715	9	723	16	819	11	842	13	668	13	760	4	656	15	636
15	Schnallinger AUT	7576	12	841	14	788	14	708	11	696	12	808	13	841	6	655	17	731	13	653	17	628
16	Walser AUT	7546	11	793	17	774	12	667	10	670	15	803	16	817	16	653	16	673	12	617	7	621
17	Walser AUT	7506	15	784	16	769	15	666	17	644	11	791	5	798	17	608	14	645	9	593	14	563

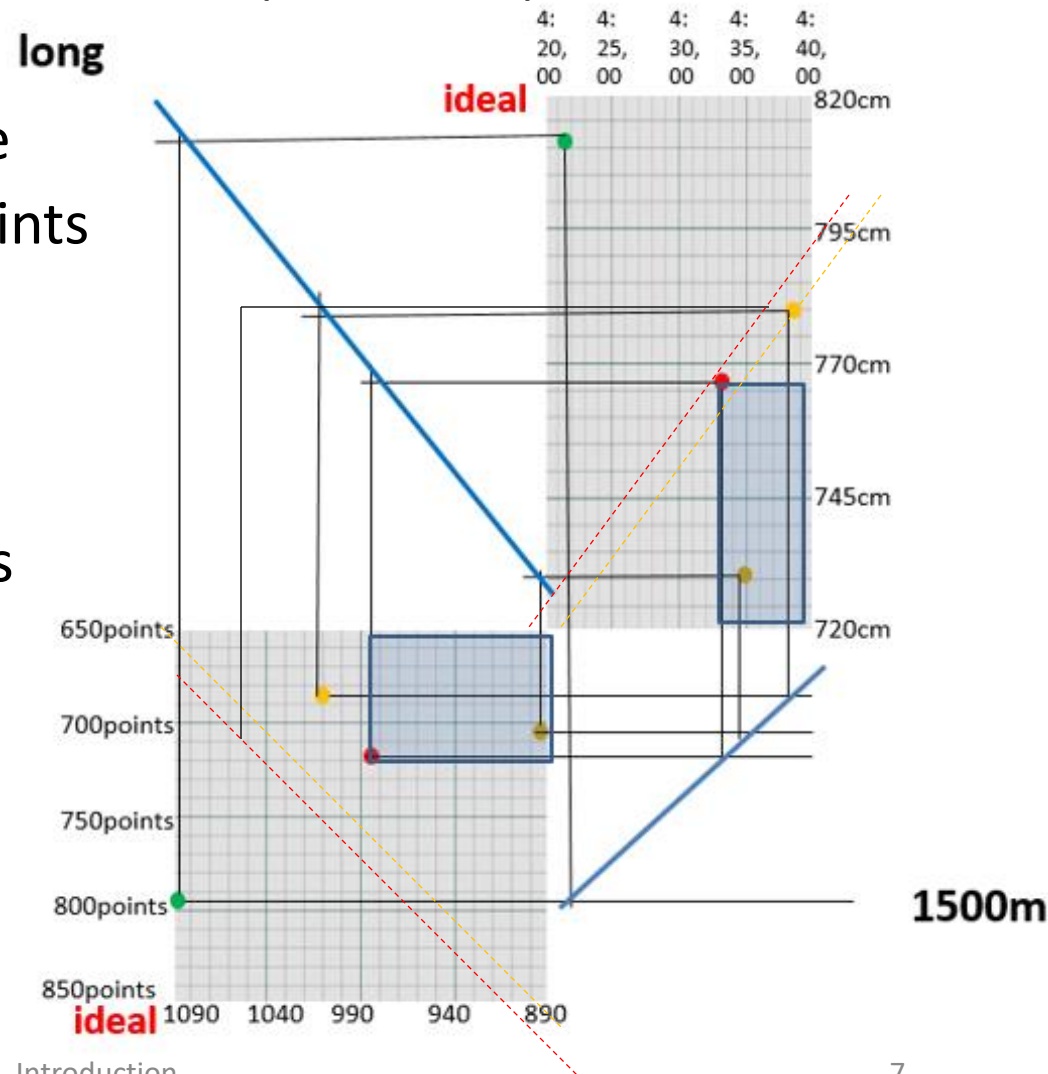
# Sum of points makes Decathlon linear

P	Athlete	Points
1	Šebřle CZE	9026
2	Nool EST	8604
3	Dvorak CZE	8527
4	Lobodin RUS	8465

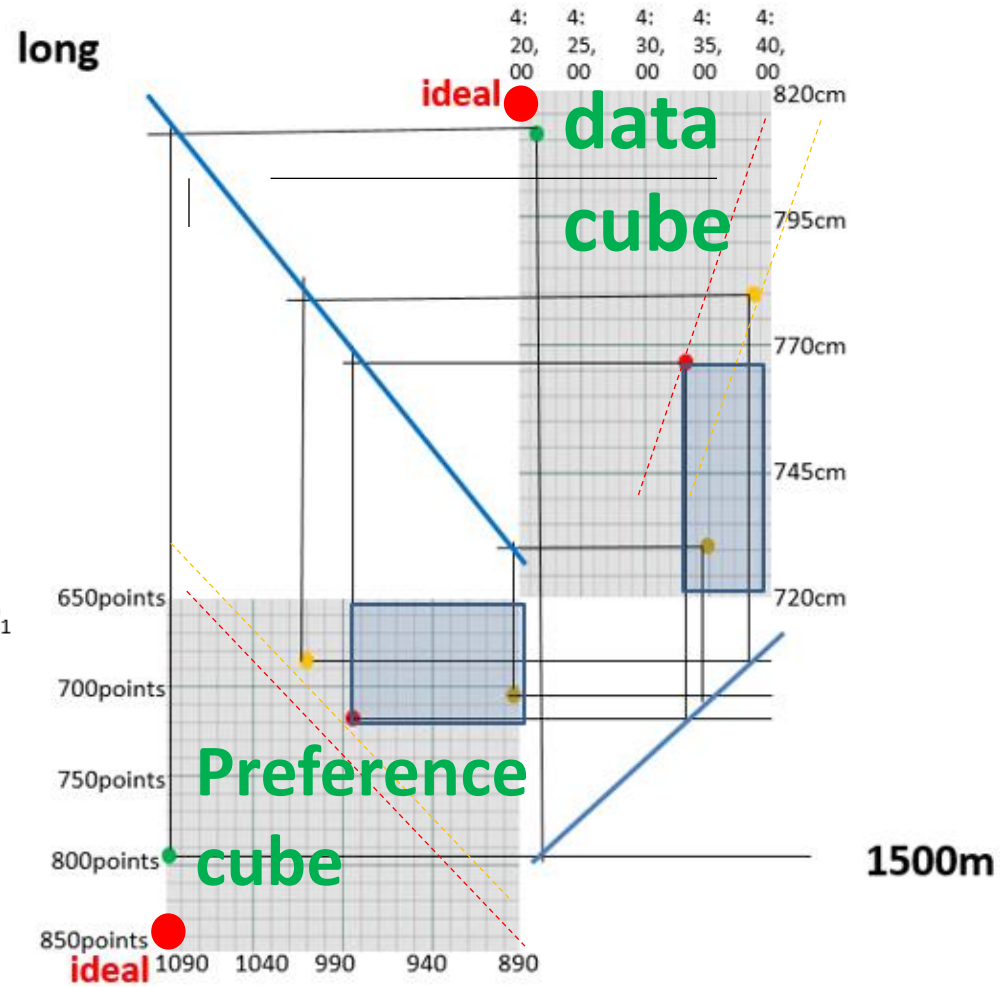
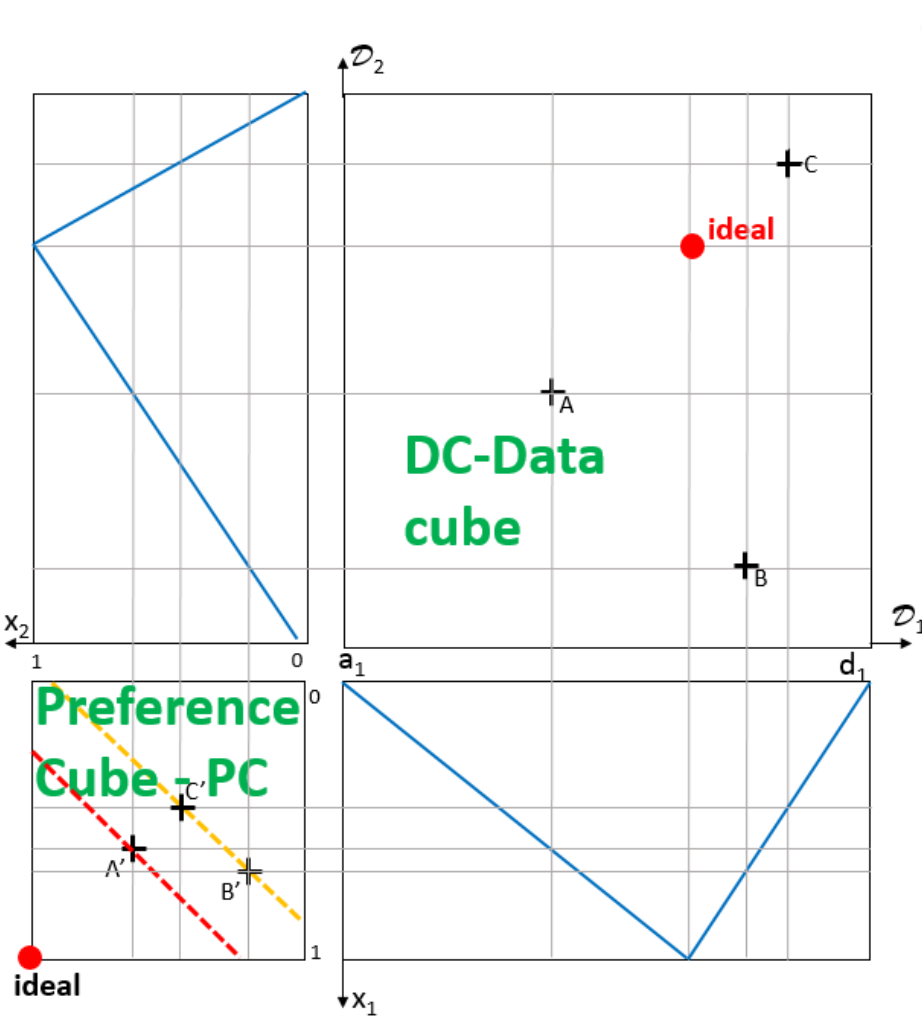
- Data cube (upper right) – **point function** transforms achievements to preference cube (lower left)

- ● dominates ●
- ● and ● are incomparable
- Sum (aggregation) of points in these two events

- ● = 1703 points
- ● = 1696 points
- PC contour line connects points with same result in Pareto cube
- Contour line can be propagated to data cube



# Decathlon like preference model = analogy for information ordering in web e-shops





# Linear **Monotone** Preference Model-LMPM

- Decathlon – “**single user**” **IAAF** rules order athletes
    - Disciplines  $\mathcal{A}_1, \dots, \mathcal{A}_{10}$ ; domains  $\mathcal{D}_1, \dots, \mathcal{D}_{10}$ ; ideal (field / track)
    - $\mathcal{A}_i$  point function  $\mathbf{f}_i: \mathcal{D}_i \rightarrow \mathbb{N}$  makes results commensurable
      - Winner - overall IAAF achievement is obtained via sum
$$\Sigma\{\mathbf{f}_i(\text{athleteID}.\mathcal{A}_i): i = 1, \dots, 10\}$$
  - Retail, e-shop – **set of users U**, LMPM<sup>u</sup> orders items
    - Attributes  $\mathcal{A}_1, \dots, \mathcal{A}_m$ ; domains  $\mathcal{D}_1, \dots, \mathcal{D}_m$ ; ideal points can be for each user different
    - Degree of preference for  $\mathcal{A}_i$  and user  $\mathbf{u} \in \mathbf{U}$   $\mathbf{f}_i^{\mathbf{u}}: \mathcal{D}_i \rightarrow [0, 1]$  – hardly made commensurable in response time
    - Winner, top-k, overall degree of preference - aggregation
$$r^{\mathbf{f}, \mathbf{t}}(\text{objectID}) = \mathbf{t}^{\mathbf{u}}\{\mathbf{f}_i^{\mathbf{u}}(\text{objectID}.\mathcal{A}_i): i = 1, \dots, m\}$$
- Here  $\mathbf{t}^{\mathbf{u}}: [0, 1]^m \rightarrow [0, 1]$ ,  $\mathbf{t}^{\mathbf{u}}(0, \dots, 0) = 0$ ,  $\mathbf{t}^{\mathbf{u}}(1, \dots, 1) = 1$ ,  
**t<sup>u</sup> monotone**(linear) - preserves Pareto ordering,

# Who, what, when, where, why

- **Design thinking** - is a term used to represent a set of cognitive, strategic and practical processes by which design concepts - is also associated with prescriptions for the **innovation** of products and services within business and social contexts
- **Lean start up** - is a methodology for developing businesses and products that aims to shorten product development cycles and rapidly discover if a proposed business model is viable; this is achieved by adopting a combination of business-hypothesis-driven experimentation, iterative ( $\beta$ ) product releases, and validated learning
- [Lean Startup Meets Design Thinking](#)
- Three-legged stool: Design Thinking, Lean Startup, Agile
- B2B/B2C, **our** story, use-case, dream, running example
- (partly) linear models to enable lab paper solutions

## Competitive Advantage by Learning and Experimentation Leveraging Design Thinking, Lean Startup and Agile



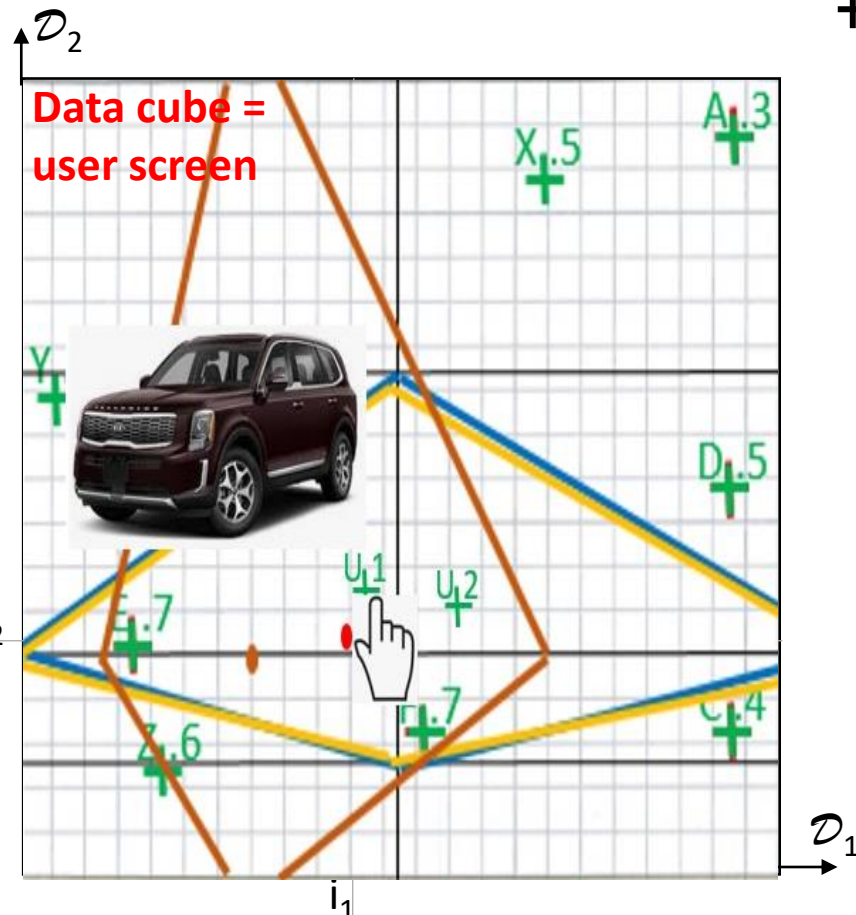
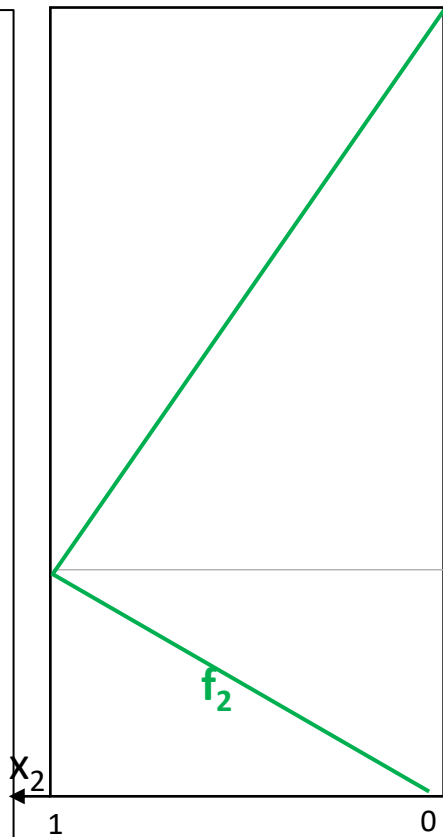
is on this research, see "Enterprise Architects Combine Design Thinking, Lean Startup and Agile to Drive Digital Innovation."

# Dream – Data cube = user screen

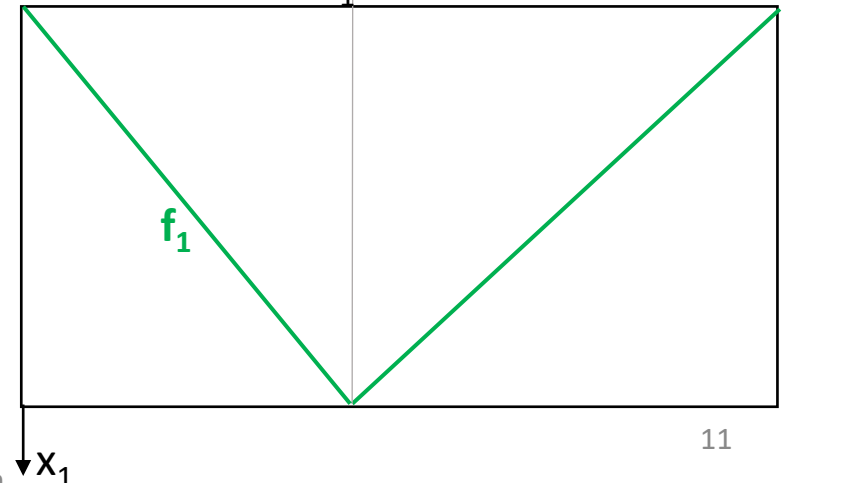
Let us build LMPM step by step

- Data model: attributes
- Either known  $A_1, A_2$ ;
  - domains  $\mathcal{D}_1, \mathcal{D}_2$ ;
  - Or latent

Triangular (trapezoidal) degree of preference of  $A_j$ , a value from  $\mathcal{D}_j$  (local preference) is given by an ideal point  $i_j$  and function  $f_j$  (can have also different shape)



Some sort of computation



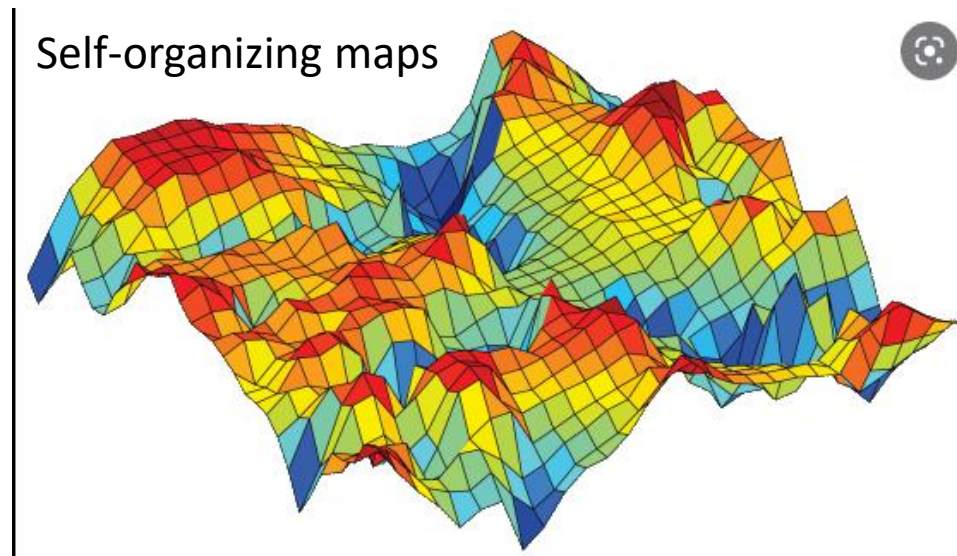
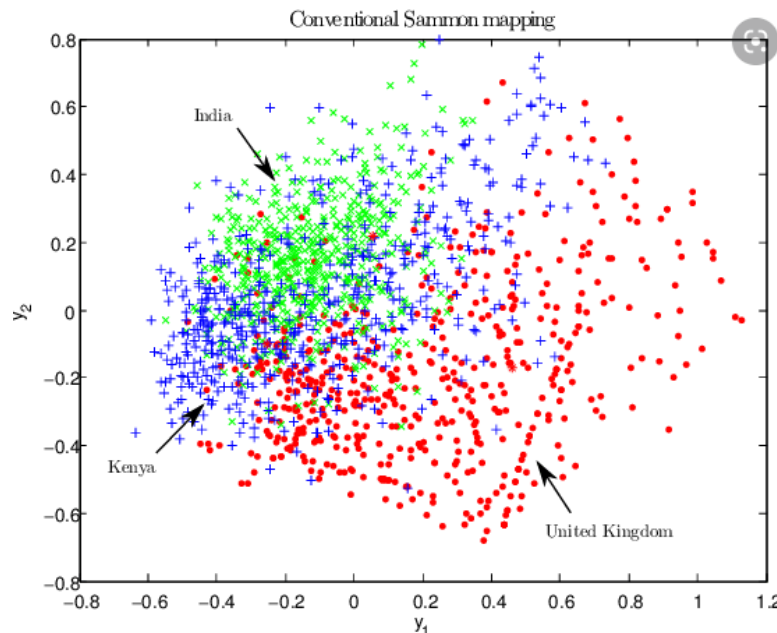
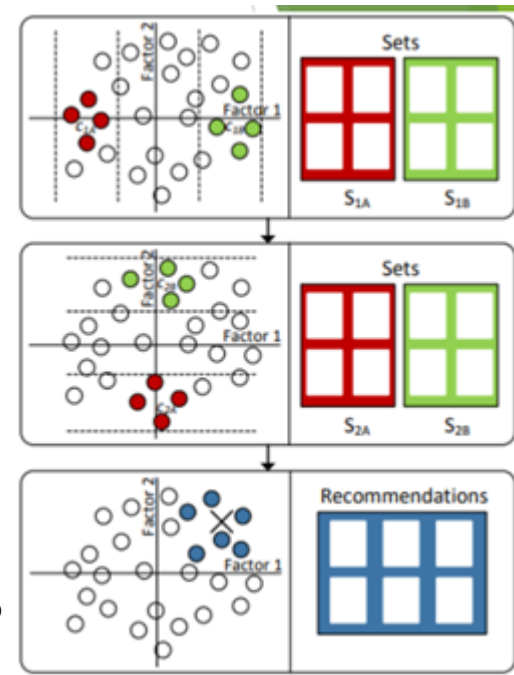
# Visual dimensionality reduction

Our eyes process global visual information more easily

- Keeps similar objects close, dimensionality reduction
- Sammon mapping, Kohonen self-organizing map, latent factors, ... 2D/3D axes do not have real meaning

Peska-Lokoc. Rating-aware self-organizing maps, MMM, oriented to VBS competition (prominent display areas, so the most relevant results should be mapped there).

Do users prefer visual information by triangle-rule (F-rule, Z-rule, ...), there is a room for eye-tracking user experiments?

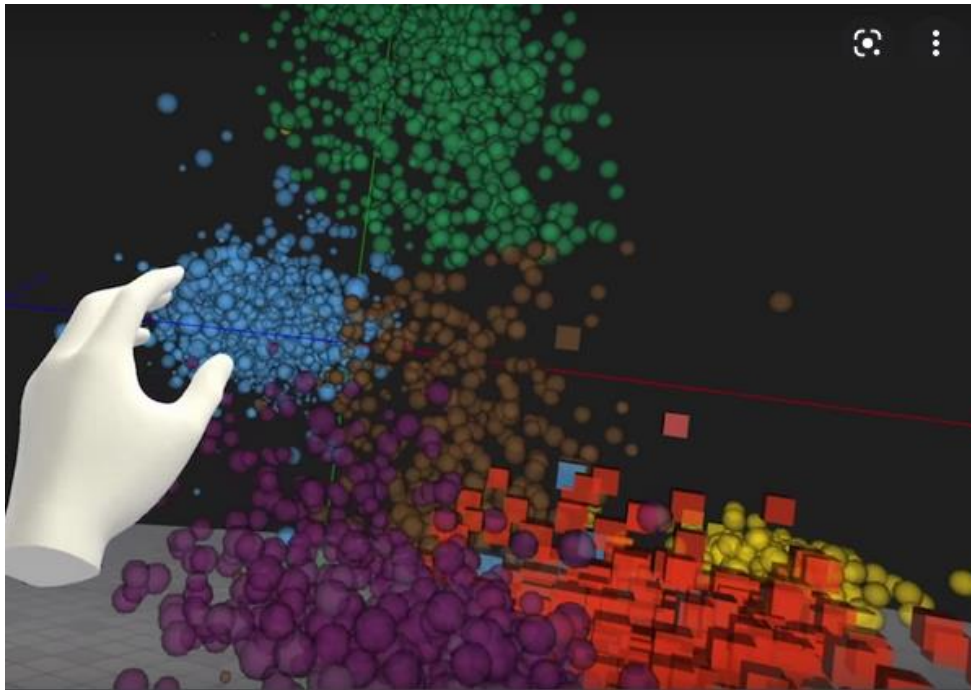
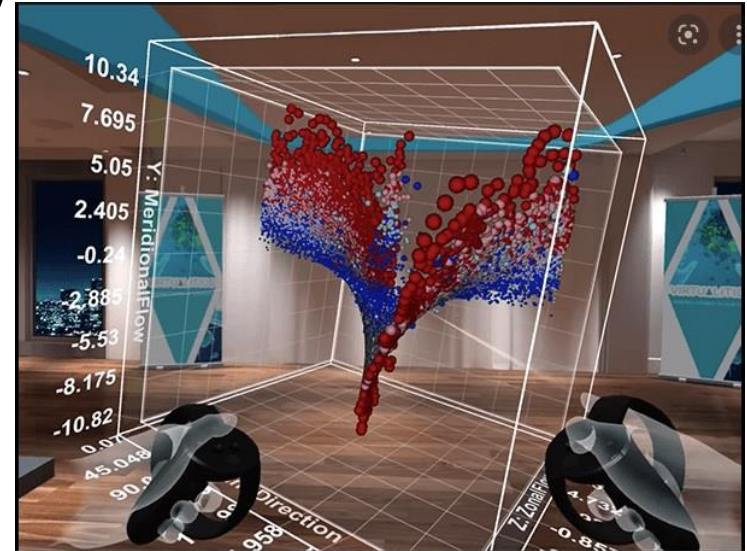


# Augmented/virtual reality

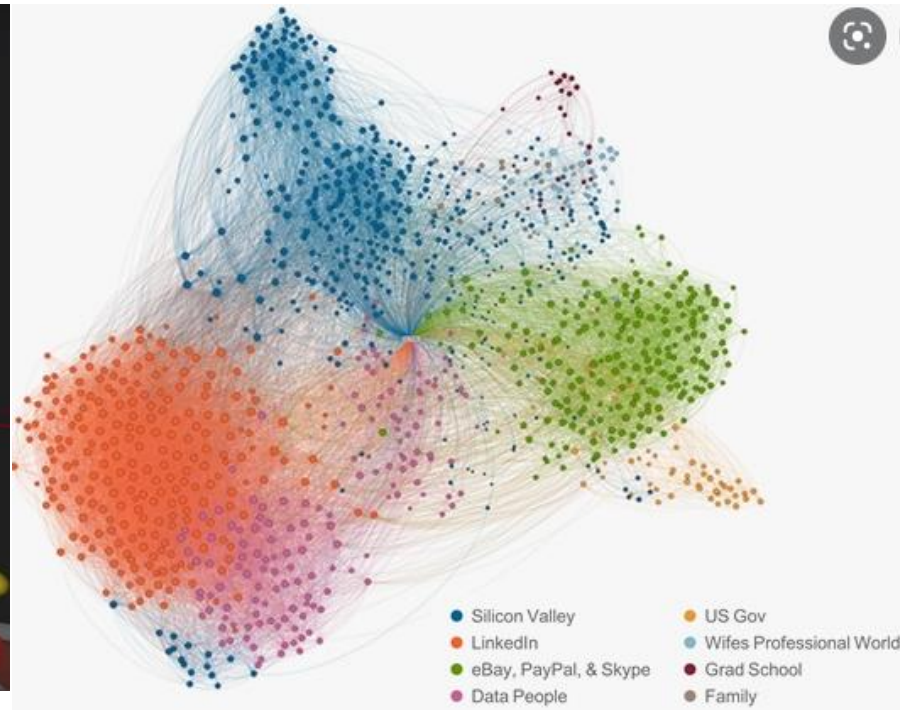
True attributes represented by 2D/3D position, color, size, shape (cube, ball), transparency, glittering

- human can percept more than 7-8 dimensions
- You need to wear AR/VR glasses

....



NDBIO21 User Preferences  
Vojtaš 11/14



Introduction

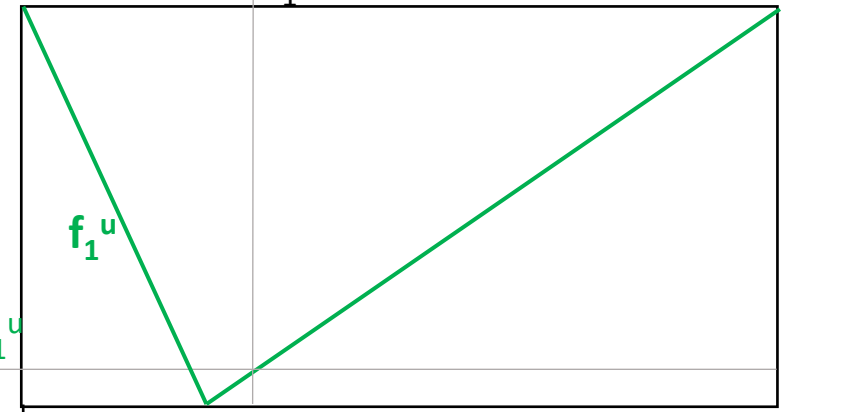
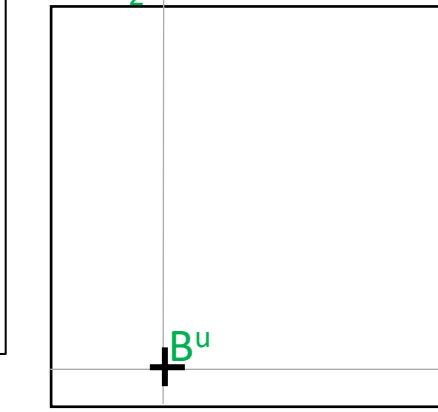
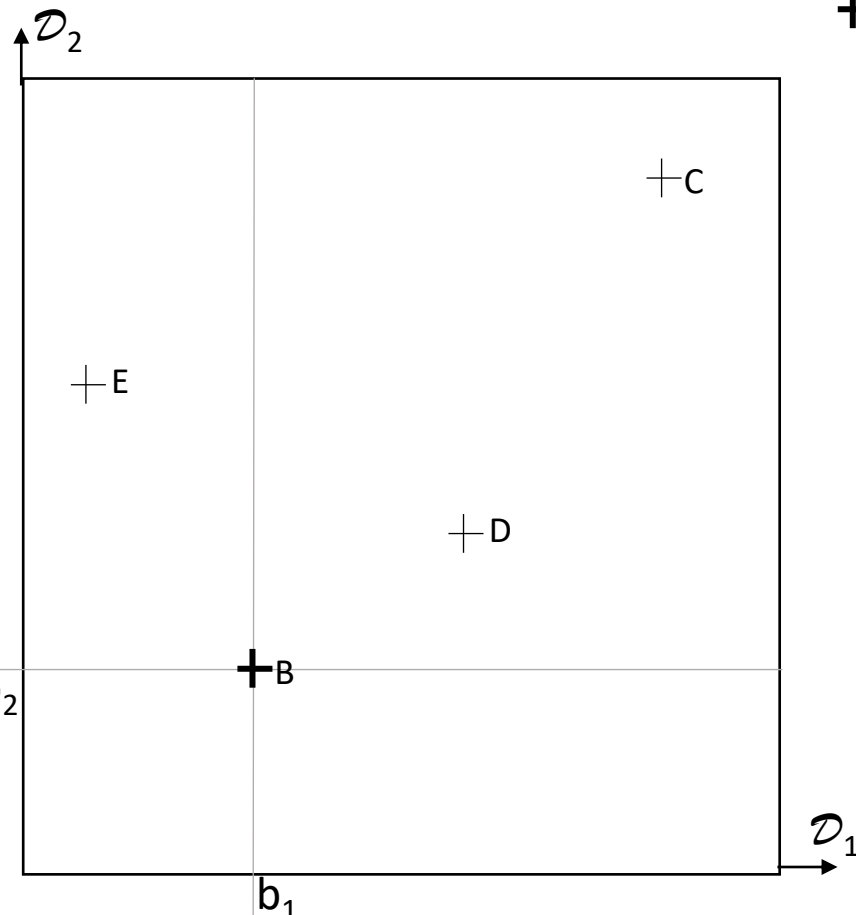
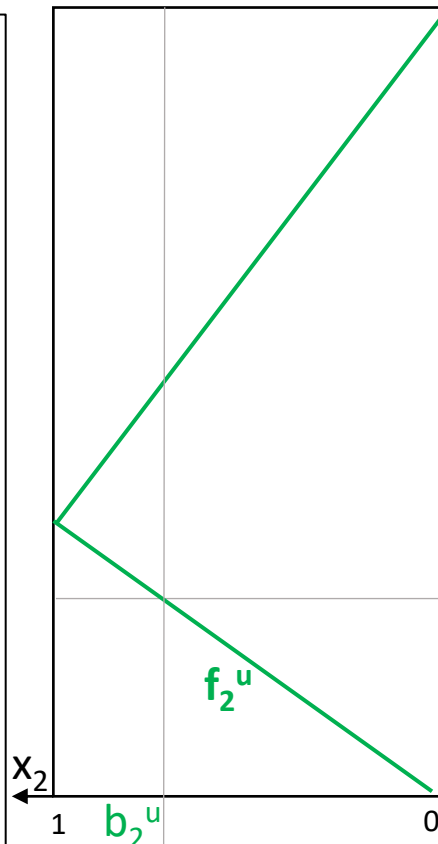
# LMPM – Linear Monotone Preference Model

Let us describe steps leading to calculation of preference degree of item B (for user u), we first describe mapping DC-data cube to PC-preference cube

Assume degree of attribute preference  $f_i^u: \mathcal{D}_i \rightarrow [0, 1]$ ,

Object with objectID = B has attribute values  $B.A_1 = b_1$  and  $B.A_2 = b_2$ , sometimes we write  $B = (b_1, b_2)$ .

Attribute preference degrees  $f_j^u(B.A_j) = b_j^u$  and corresponding point in preference cube is  $B^u = (b_1^u, b_2^u)$ , similarly C, D,...

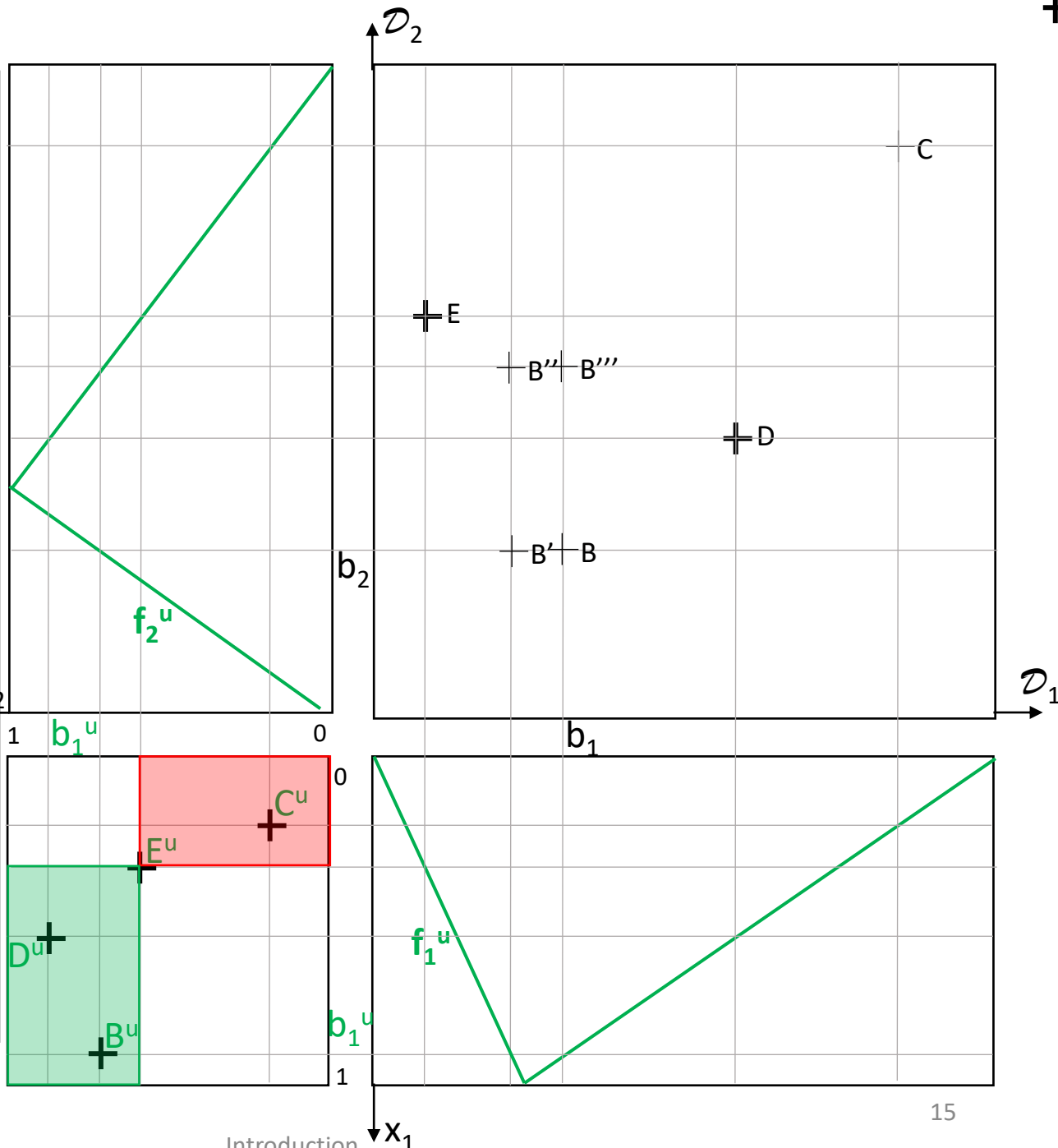


Note, that point  $B^u$  has 4 coimages  $B, B', B'', B'''$   
 Degree of preference for user  $u \in U$  are given by  $f_1^u$  and  $f_2^u$ .

Note that both  $D^u$  and  $B^u$  are in both attributes better than  $E^u$ ,  $B^u$  and  $D^u$  are incomparable, define Pareto ordering of pref. cube  $(\underline{x}) <_{\text{Pareto}} (\underline{y})$  iff (for each  $i$ )  $x_i \leq y_i$  &  $(\exists i) x_i < y_i$ , We say that  $\underline{y}$  dominates  $\underline{x}$

Item  $E^u$  dominates whole red area and is dominated by whole green area

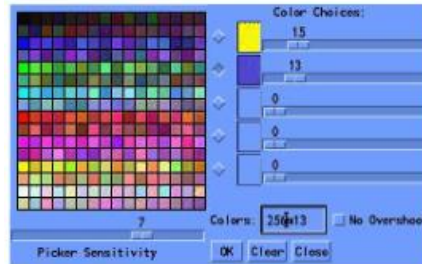
$<_{\text{Pareto}}$  is not linear, e.g.  $B^u$  and  $D^u$  are not comparable  
 Items in white areas are incomparable with  $E^u$



Combining queries,  
requirements,  
services,



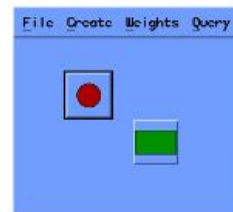
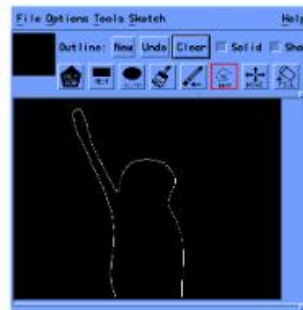
Combining = aggregating  
ratings (numbers in [0, 1])



User's requirements are also  
called criteria. Our typical  
problem is multicriterial  
(differs from multicriterial  
optimization).

Display size from 14" to 17.3" X  
Size of operational RAM from 8 GB to 32 GB X  
Storage capacity from 1,500 GB to 2,000,000 GB X

Certified X SUV / Crossover X Min Year: 2000 X Max Year: 2016 X  
Min Price: \$10,000 X Max Price: \$14,000 X Mileage: Under 30,000 X  
Automatic X

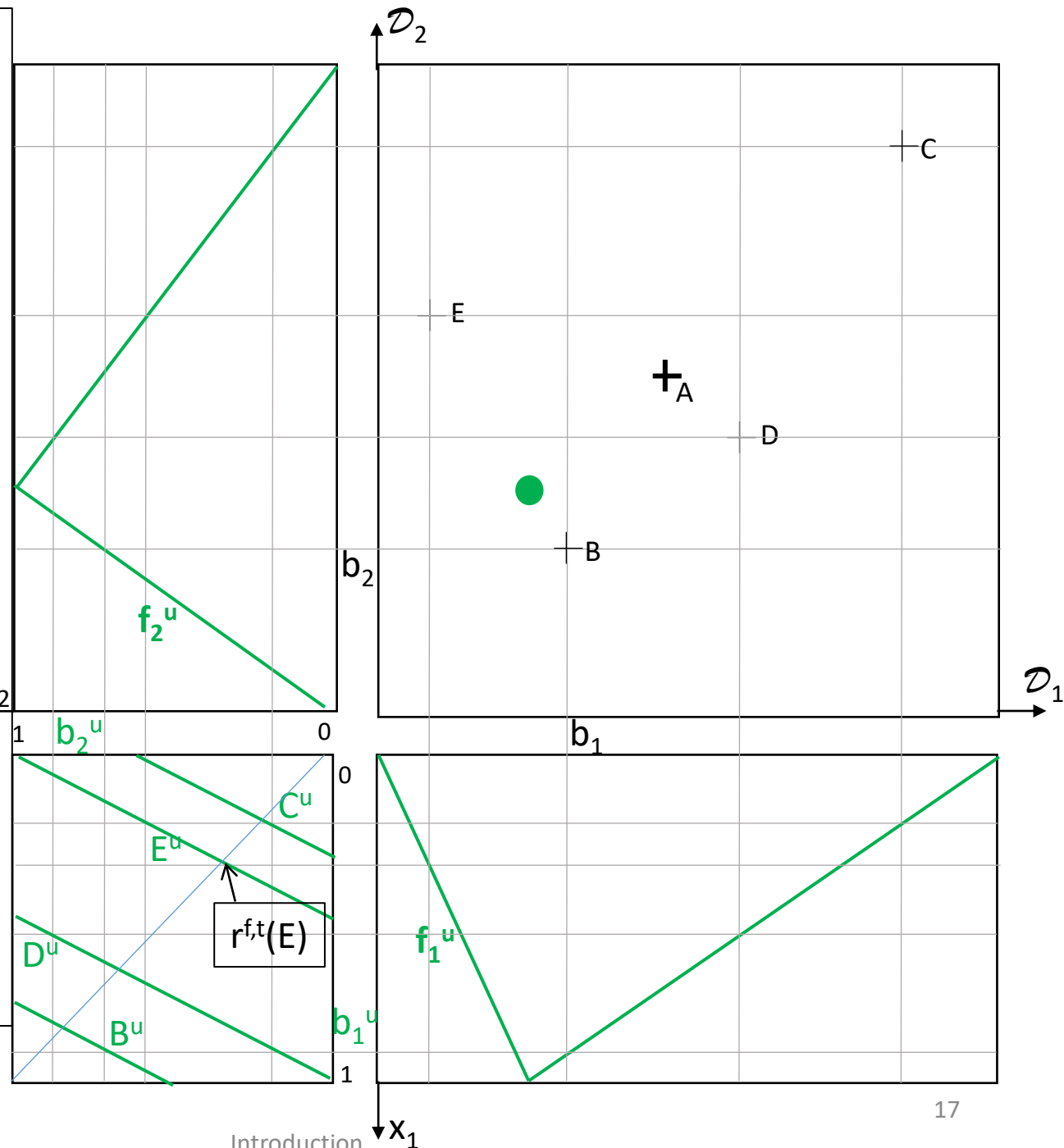




To get global preference degree of items we need aggregation functions. It is a function  $[0,1]^2 \rightarrow [0,1]$   
 $t(x_1, x_2) = w_1 * x_1 + w_2 * x_2$ ,  
 where  $w_1, w_2 \geq 0$  are attribute weights with  $w_1 + w_2 = 1$

Graph of  $t$  is a 3D object. Intuition behind display of aggregation function are contour lines for user  $u$

Note, that on the preference cube diagonal  $x_2$  corresponding contour line  $cl_y$  of preference degree  $y \in [0,1]$  intersect the diagonal at point  $(y, y)$ ,  
 $w_1 * x + w_2 * x = y$  gives  $x * (w_1 + w_2) = y$ , i.e.,  $x = y$



Preference model of user  $u_{f,t}$  on data cube

Function  $R^{f,t}: \prod D_i \rightarrow [0,1]$

$R^{f,t}(a_1, \dots, a_m) = t([f_i(a_i) : i = 1, \dots, m])$

Ordering on data

cube  $(a_1, \dots, a_m) \geq^{f,t} (b_1, \dots, b_m)$  iff  $R^{f,t}(a_1, \dots, a_m) \geq R^{f,t}(b_1, \dots, b_m)$  Ordering

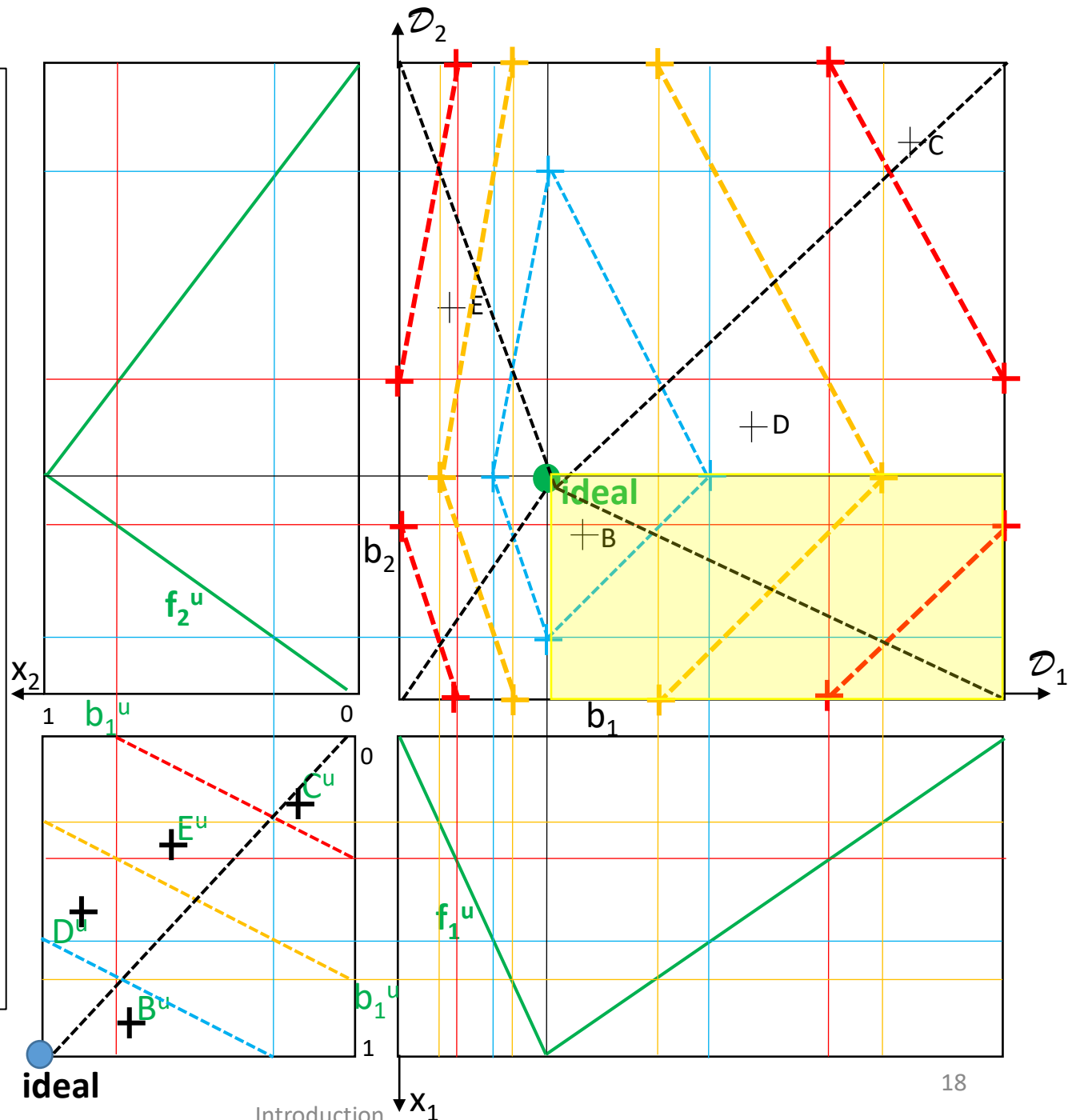
can be visualized as contour lines on  $\prod D_i$

For better understanding are different contour lines (of same  $t$ ) in colors

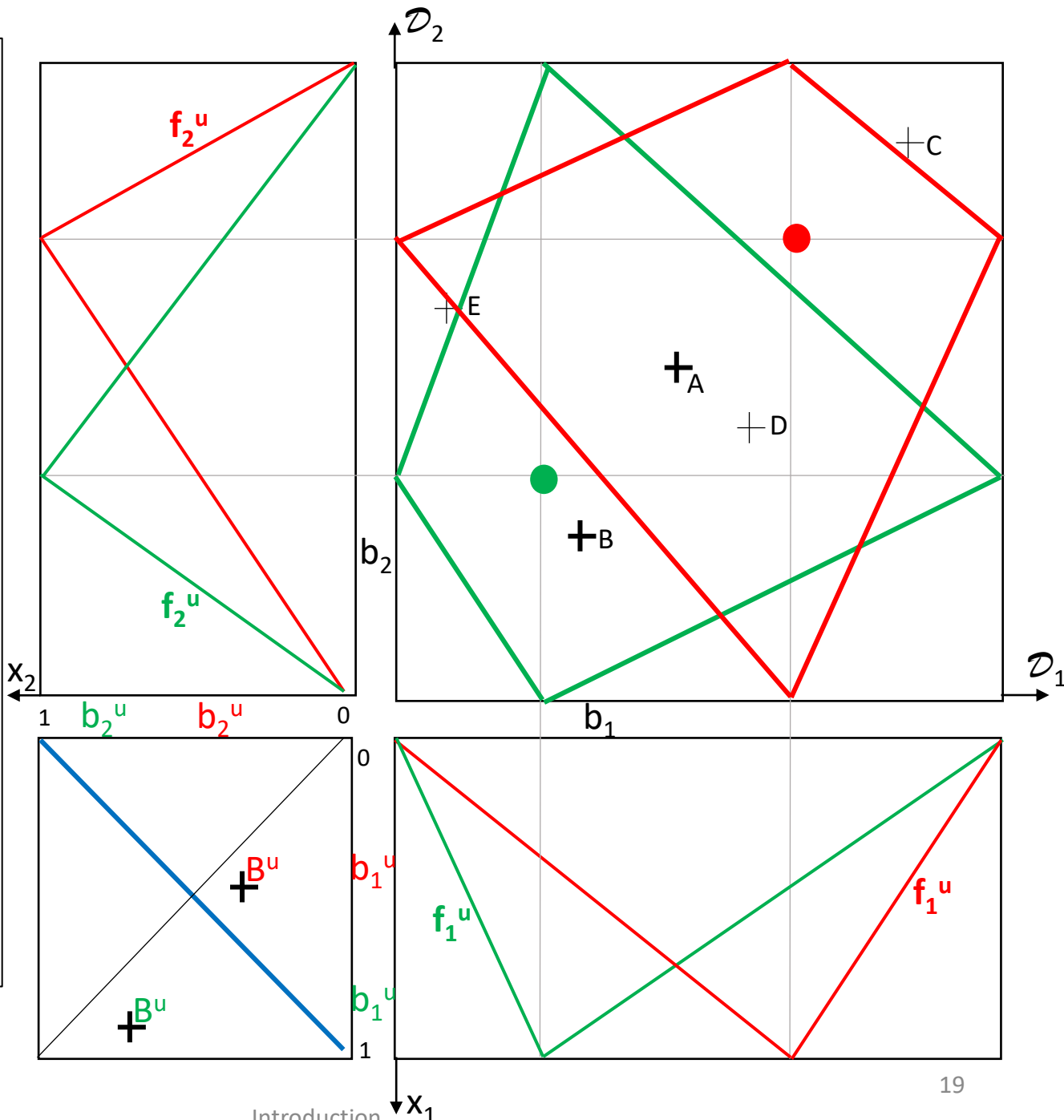
User  $u_{f,t}$ , preference of user  $u_{f,t}$ ,  $R^{f,t}: \prod D_i \rightarrow [0,1]$

$R^{f,t}(a_1, \dots, a_m) = t([f_i(a_i) : i = 1, \dots, m])$

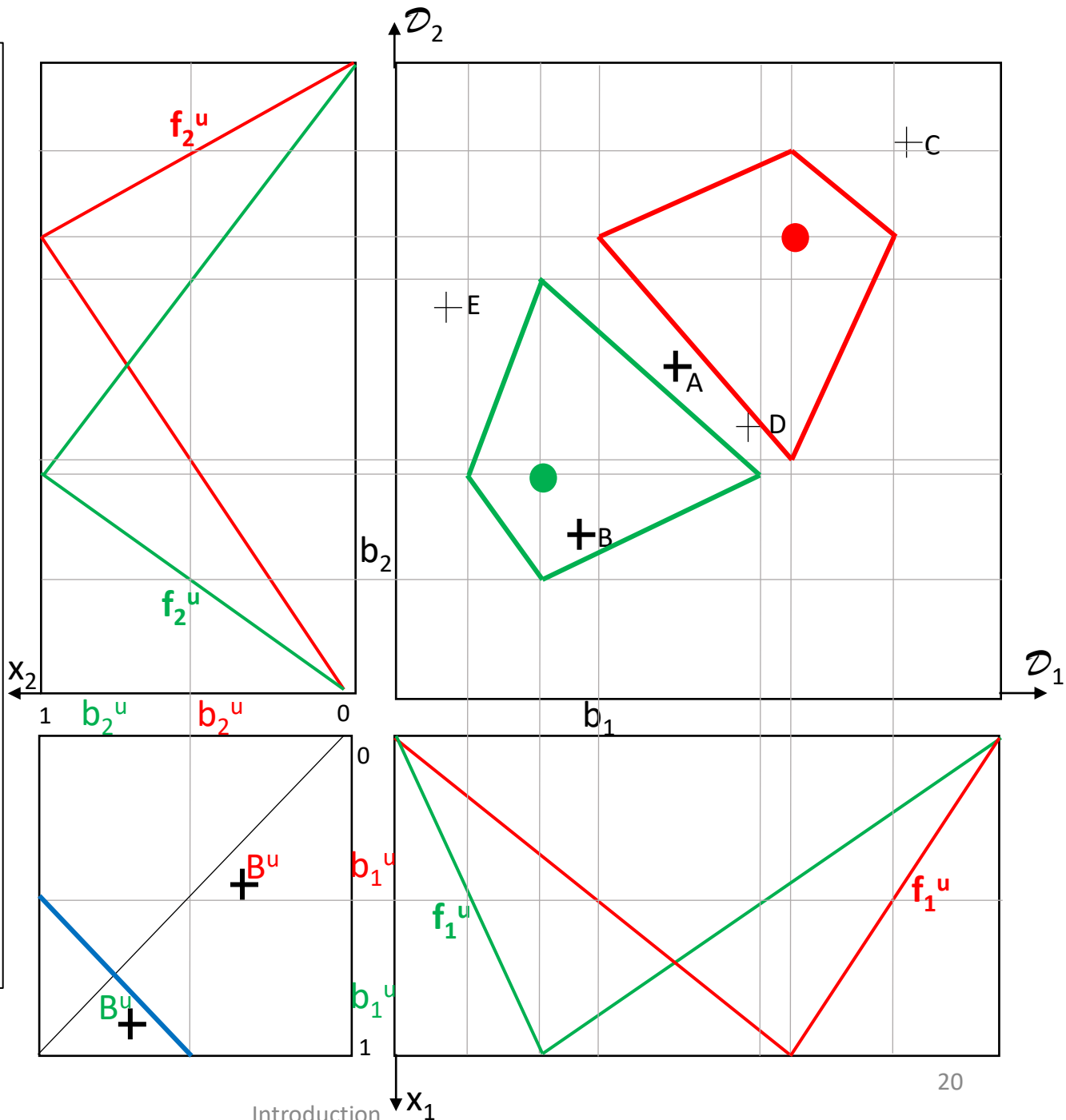
$(a) \geq^{f,t} (b)$  iff  $R^{f,t}(a) \geq R^{f,t}(b)$



Data model: attributes  $A_1, A_2$ ; domains  $\mathcal{D}_1, \mathcal{D}_2$ ;  
 Ideal points can be for each user different, we consider users  $u$  and  $u$ . Both have same aggregation average AVG  
 As before we have  $f_i^u: \mathcal{D}_i \rightarrow [0, 1]$  (for an user  $u \in U$ ), so we have  $f_i^u$  and  $f_i^u$ .  
 Object with objectID = B has attribute values  $B.A_1 = b_1$  and  $B.A_2 = b_2$ , sometimes we write  $B=(b_1, b_2)$  has two images in preference cube  $B^u$  and  $B^u$ .  
 Let us depict  $\frac{1}{2}$  contour line in DC



Data model: attributes  $A_1, A_2$ ; domains  $\mathcal{D}_1, \mathcal{D}_2$ ;  
 Ideal points can be for each user different, we consider users  $u$  and  $\bar{u}$ .  
 Both have same aggregation average AVG  
 As before we have  $f_i^u: \mathcal{D}_i \rightarrow [0, 1]$  (for an user  $u \in U$ ), so we have  $f_i^u$  and  $f_i^{\bar{u}}$ .  
 Object with objectID = B has attribute values  $B.A_1 = b_1$  and  $B.A_2 = b_2$ , sometimes we write  $B = (b_1, b_2)$  has two images in preference cube  $B^u$  and  $B^{\bar{u}}$ .  
 Let us depict  $\frac{3}{4}$  contour line in DC



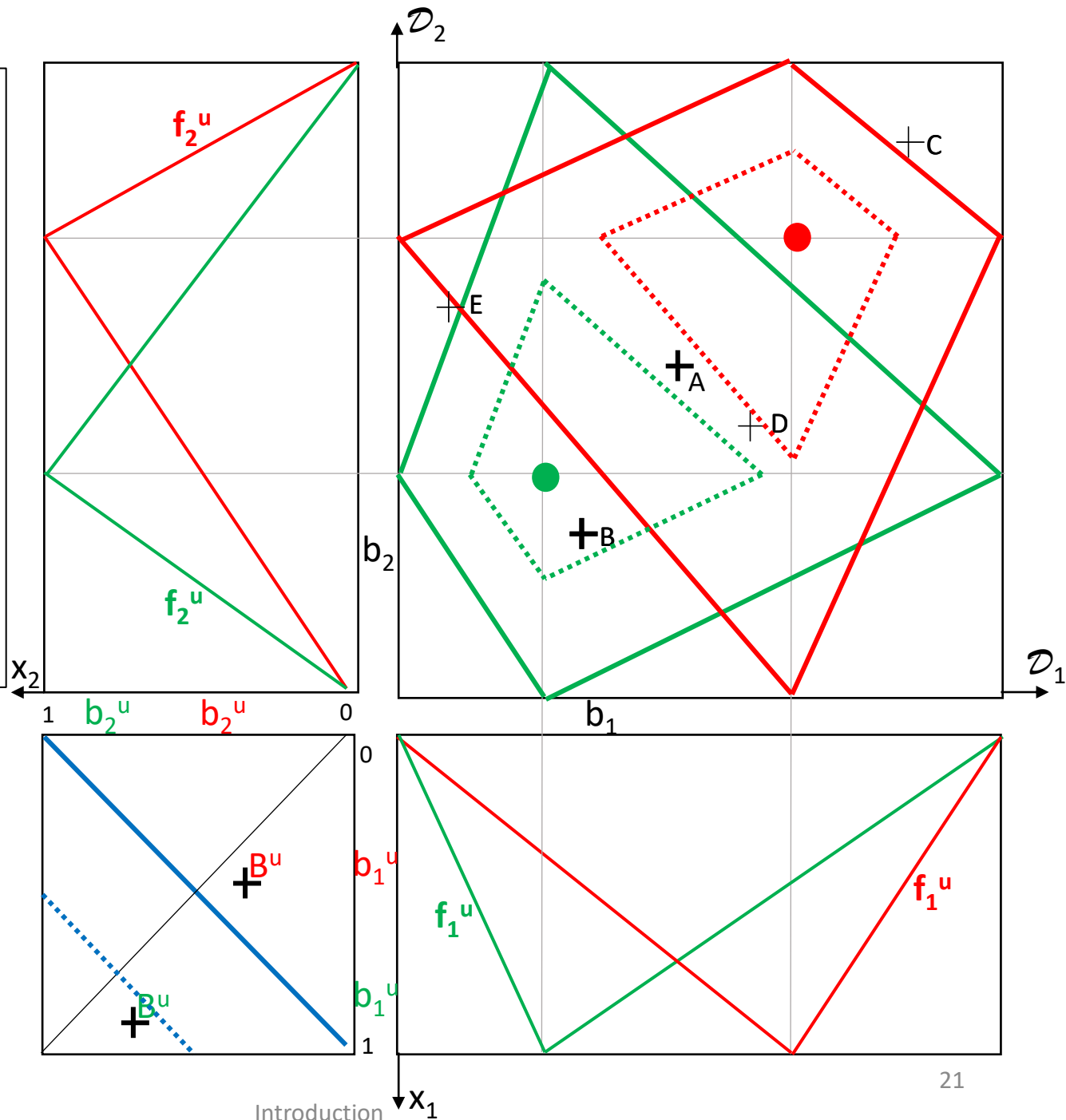
Previous two slides in one.

Observe  $\frac{1}{2}$  and  $\frac{3}{4}$  contour lines in DC.

It seems that there is some parallelism.

Formulate statement, prove or disprove.

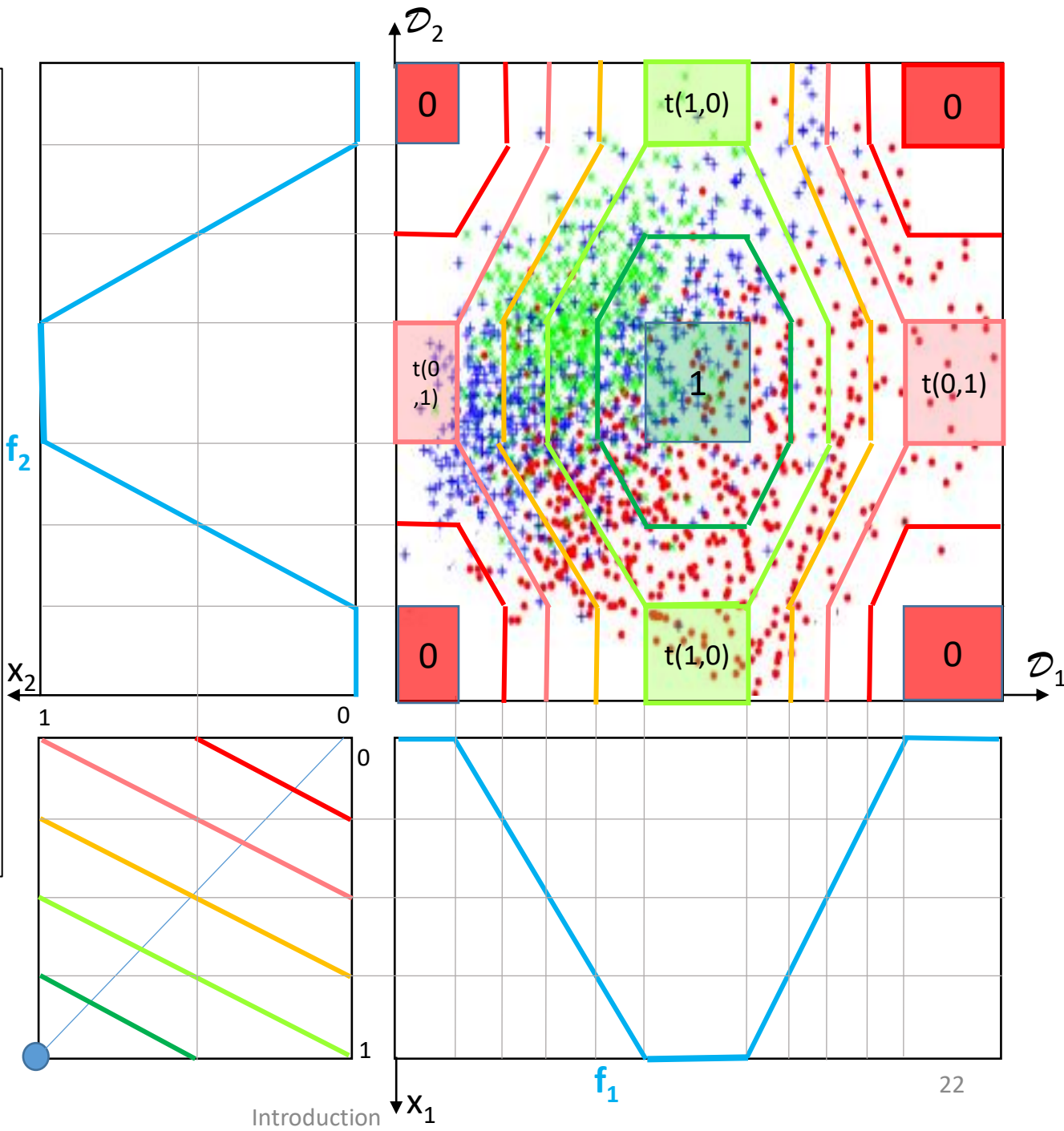
Interpret result, discuss intuitiveness



Trapezoidal degree of preference of  $\mathcal{A}_j$ , a value from  $\mathcal{D}_j$  (local preference) is given by an ideal interval  $[i_j^l, i_j^r]$  and analogically defined functions  $f_j$  (trapezoid is based on interval  $[a_j, d_j]$ )

Consider different combination of “hill” “valley” shaped attribute preferences

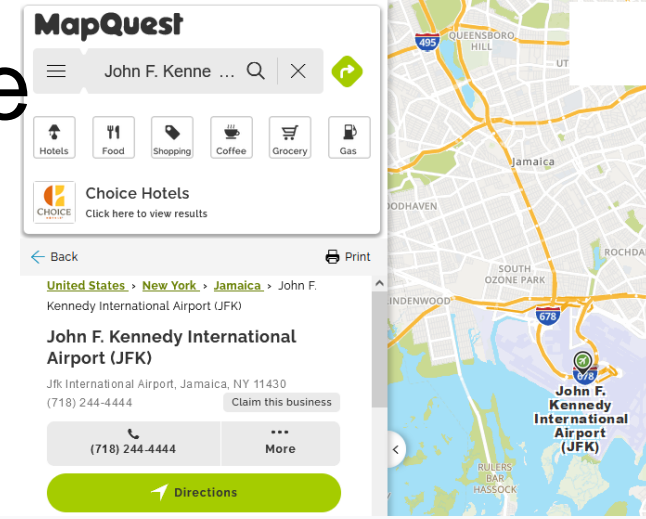
Arbitrary point/line from DC/PC can be mapped to point/line in PC/DC



# Web services – access mode

## – data types

- [MapQuest](#) returns the distance between two addresses.
- [NYTimes Review](#) gives the price range of a restaurant.
- [Zagat](#) gives a food rating to the restaurant.
- We follow paper [FLN] Fagin, Lotem, Naor, Optimal aggregation algorithms for middleware. Journal of Computer and System Sciences 66 (2003) 614–656 [JCSS2003](#)
  - Access mode – sorted, direct (random), stateless, ...
  - From multimedia middleware ([IBM Almaden Garlic project](#)) top-k optimal querying to our multiuser LMPM



The New York Times

## Zagat and Michelin Hit Pause on New York City Guides

There will be no New York restaurant guides from the two companies this year, as restaurateurs struggle to keep their businesses open.

The New York Times

FOOD

### Restaurant Search

Pete Wells, our restaurant critic; Ligaya Mishan, the author of the Hungry City column; and other New York Times critics review New York restaurants, from four-star dining rooms to neighborhood joints.

NYT COOKING | WINE, BEER, AND COCKTAILS | HOW TO COOK

Search bar with fields for Rating, Neighborhood, and Price.

Feb. 14, 2022  
Read Review  
Reserve a Table

#### Ci Siamo

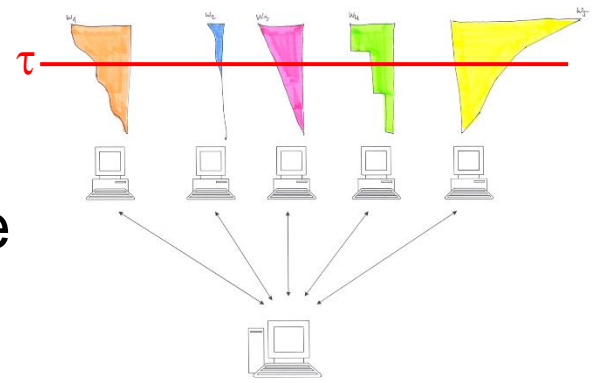
NYT Critic's Pick | Italian | \$\$\$ | Chelsea

Ci Siamo is Italian all the way, from the name you see on the door to the dessert you'll almost certainly want just before you leave. The chef, Hillary Sterling, has a lively, inviting style that she has broadened and intensified with a new tool — an open, wood-burning hearth that looks wide enough to roast a midsize lion.

By PETE WELLS



# FLN threshold algorithm TA



**1. Do** sorted access in parallel to each of the **As** an object  $R$  is seen under sorted access in some list, **do** random access to the other lists to find the grade  $x_j^R$  of object  $R$  in every list  $L_j$ . **Then** compute the grade  $t(R) = t(x_1^R, \dots, x_m^R)$  of object  $R$ .

**If** this grade is one of the  $k$  highest, we have seen, **then** remember object  $R$  and its grade  $t(R)$ .

**2. For** each list  $L_i$ , let  $\underline{x}_i$  be the grade of the last object seen under sorted access. **Define** the threshold value  $\tau$  to be

$$\tau = t(\underline{x}_1, \dots, \underline{x}_m)$$

**As soon as** at least  $k$  objects have been seen whose grade is at least equal to  $\tau$ ; **then** halt. **Else** go to **1**.

**3. Let**  $Y$  be a set containing the  $k$  objects that have been seen with the highest grades. The **output** is then the graded set  $\{(R, t(R)) \mid R \in Y\}$  (ordered by  $t(R)$ ).



# FLN-TA graphically (2D)

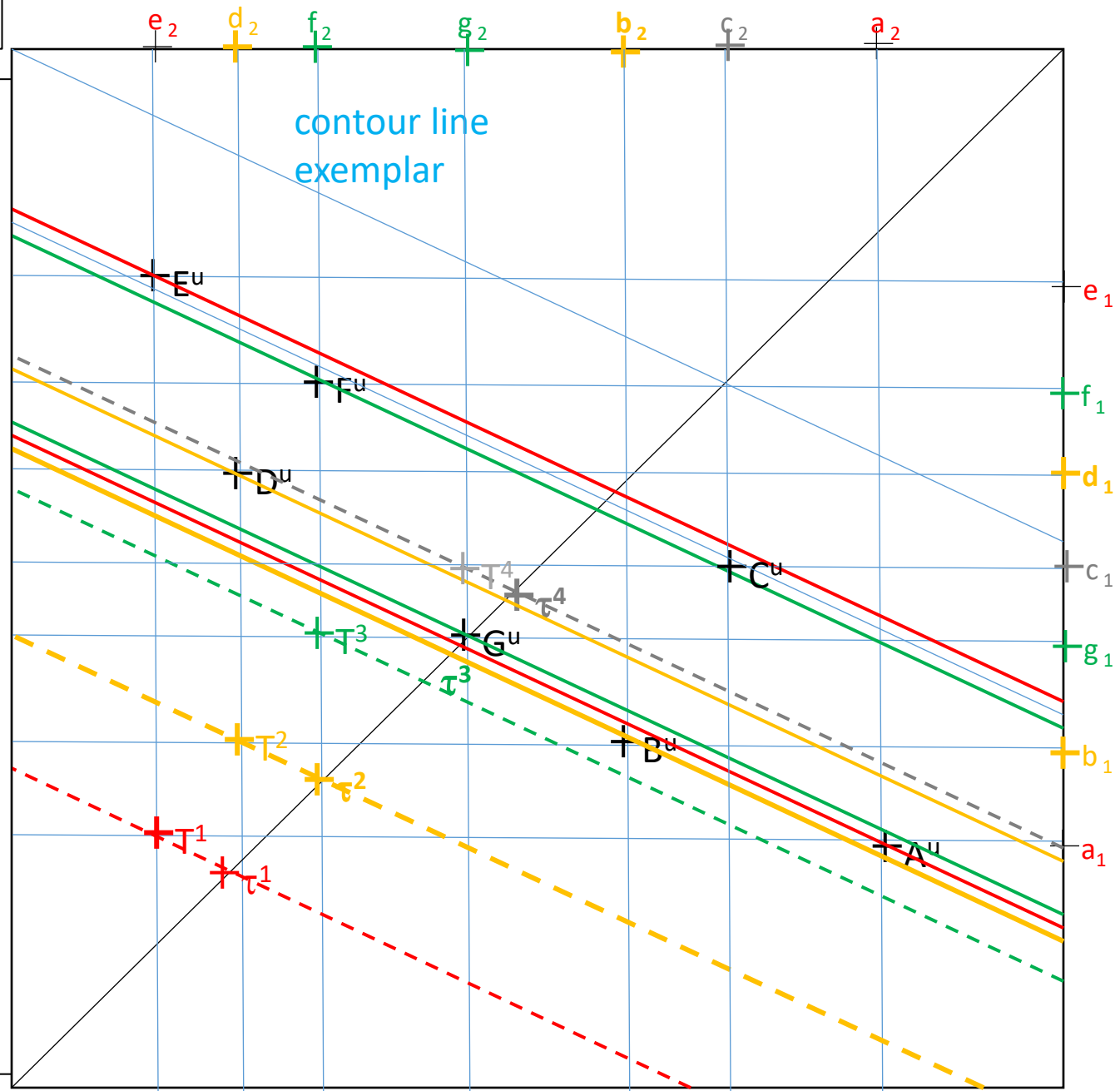
## Big picture

In this case we need 4 steps to decide the winner

Certified order of items so far is B, A, G, D (for F, C, E we have to wait)

It seems that number of steps needed to decide the winner is at most  $n/2 + 1$  where  $n$  is the # of items ( $\lfloor n/2 \rfloor + 1$ )

?can we find data distribution such that TA ends (decides winner / decides all) in arbitrary number of steps  $s \leq (\lfloor n/2 \rfloor + 1)$  ?



# FLN-TA graphically (4D)

In this  $[0,1] \times [0,1]$  rectangle we see lists from FLN data model.

Horizontally are weights  $w_1=0.4, w_2=0.3 \dots$  (summed up to 1) and vertically preference degrees of objects (items) A, B, ..., G in respective lists.

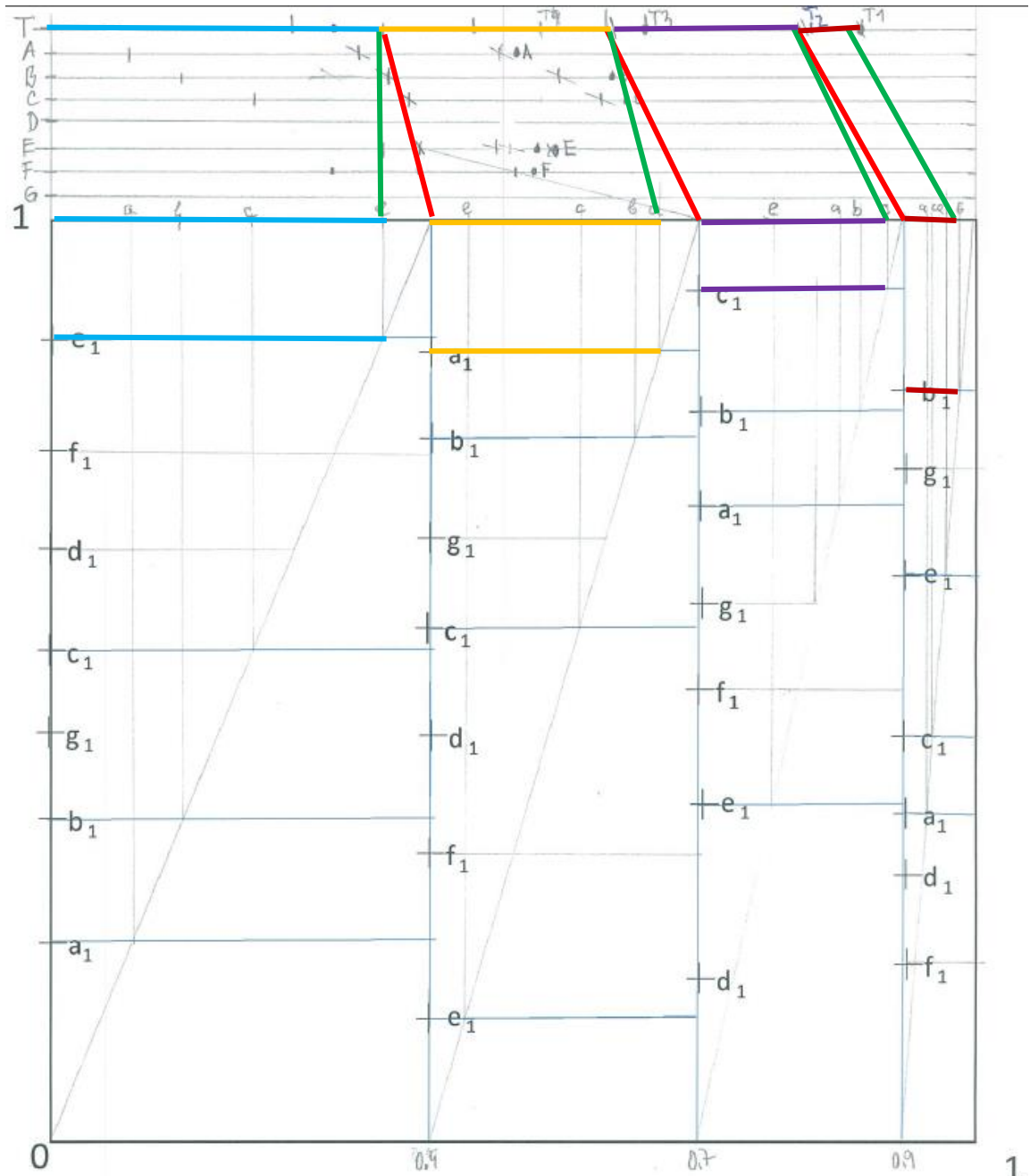
Above this there are 8 lines (for 7 points and threshold) where sum of attribute preferences are depicted.

Diagonal line helps to calculate attribute preference.

Parallelograms help to depict addition of respective quantity.

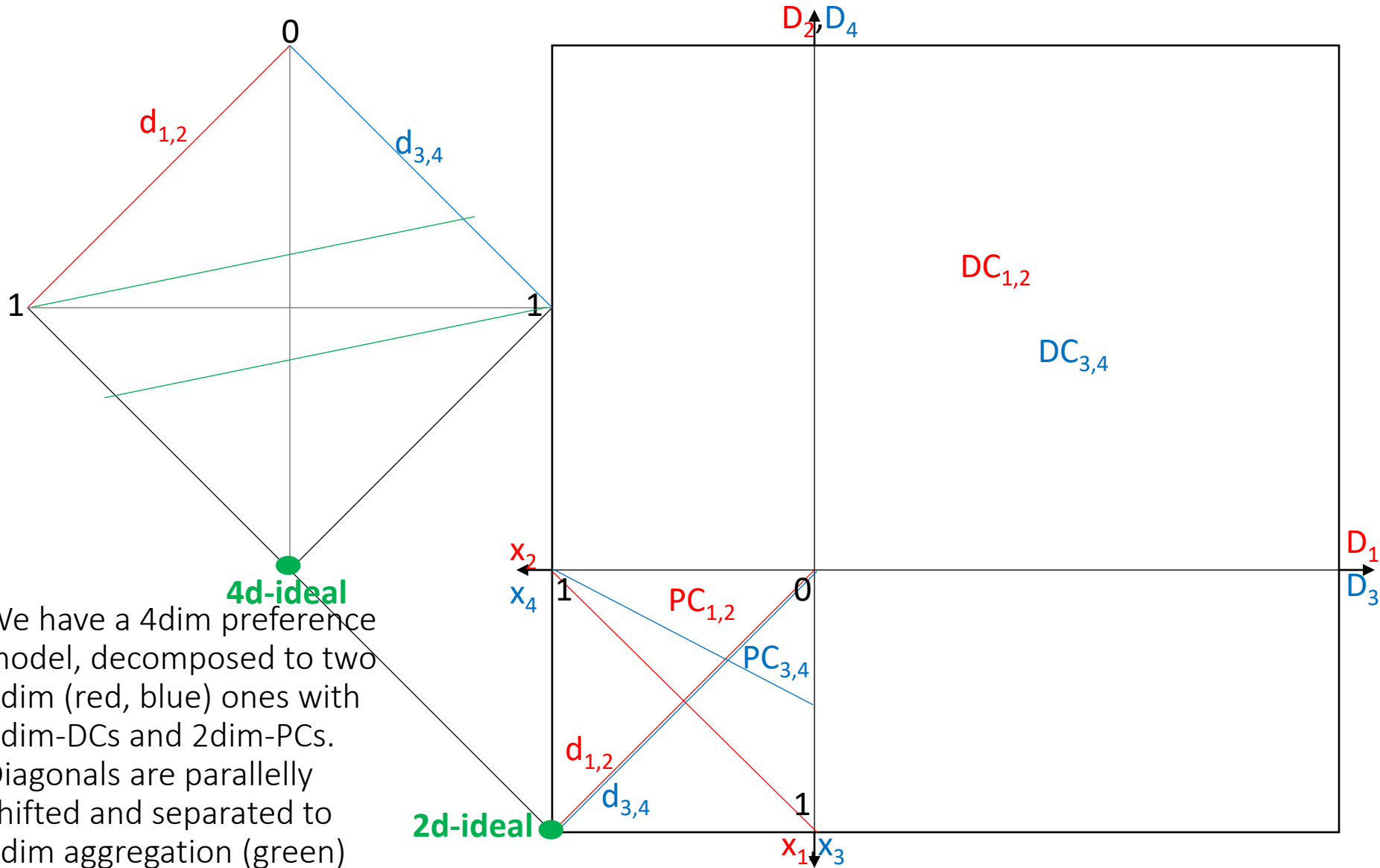
Here we depict the threshold after the first step of FLN-TA, here  $T^1 = \tau^1, \dots$

Colors depict where the value is taken from



# 4dim framework

$$2 * \frac{x_1 + x_2}{2} + 3 * \frac{2 * x_3 + x_4}{3} = \frac{2 * y_{1,2} + 3 * y_{3,4}}{5} = z$$



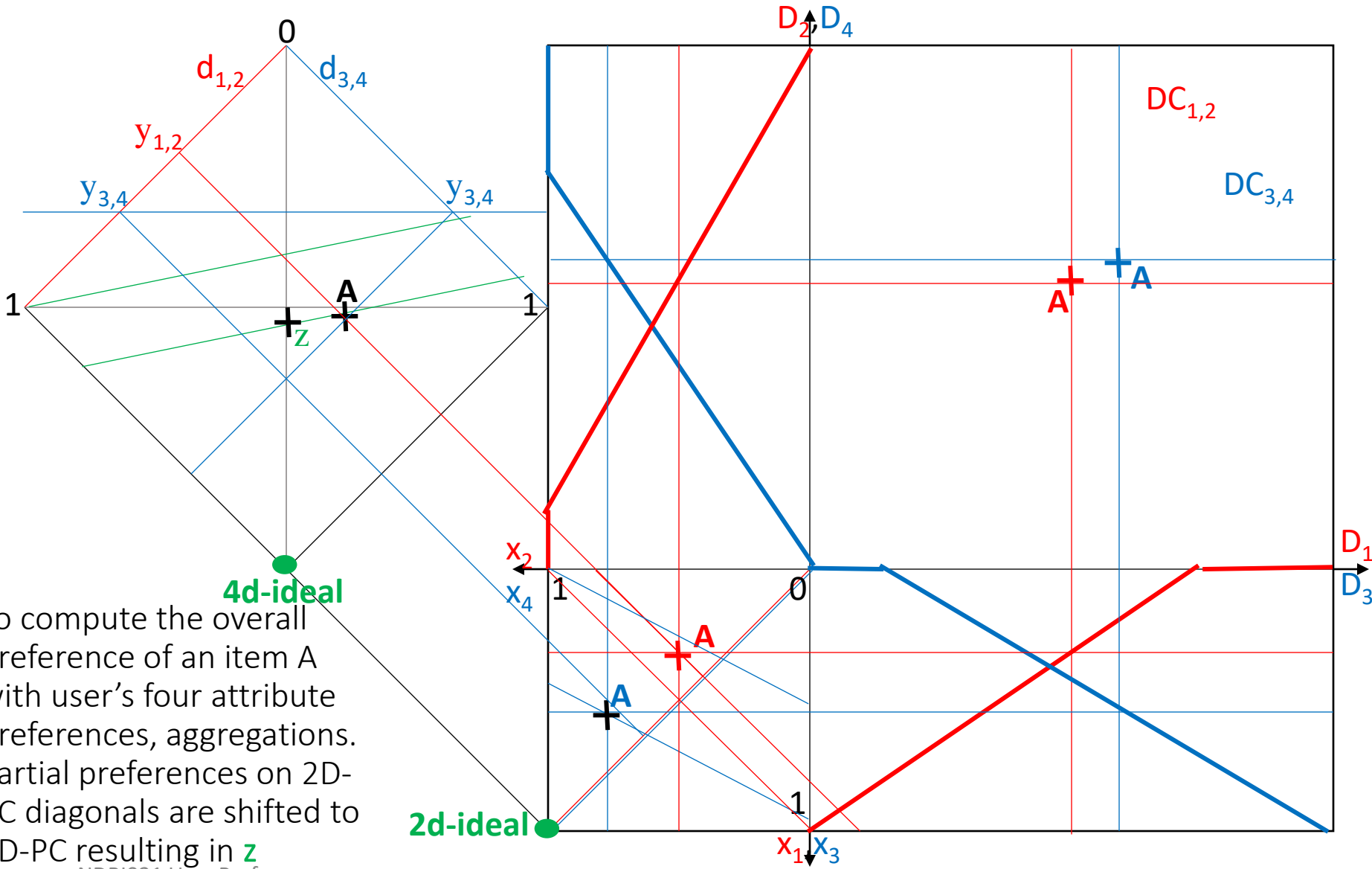
**4d-ideal**

**2d-ideal**

We have a 4dim preference model, decomposed to two 2dim (red, blue) ones with 2dim-DCs and 2dim-PCs. Diagonals are parallelly shifted and separated to 4dim aggregation (green)

$$2 * \frac{x_1 + x_2}{2} + 3 * \frac{2 * x_3 + x_4}{3} = \frac{2 * y_{1,2} + 3 * y_{3,4}}{5} = z$$

Two 2D-DC → 4D-PC



4d-ideal

2d-ideal

To compute the overall preference of an item A with user's four attribute preferences, aggregations. Partial preferences on 2D-PC diagonals are shifted to 4D-PC resulting in z

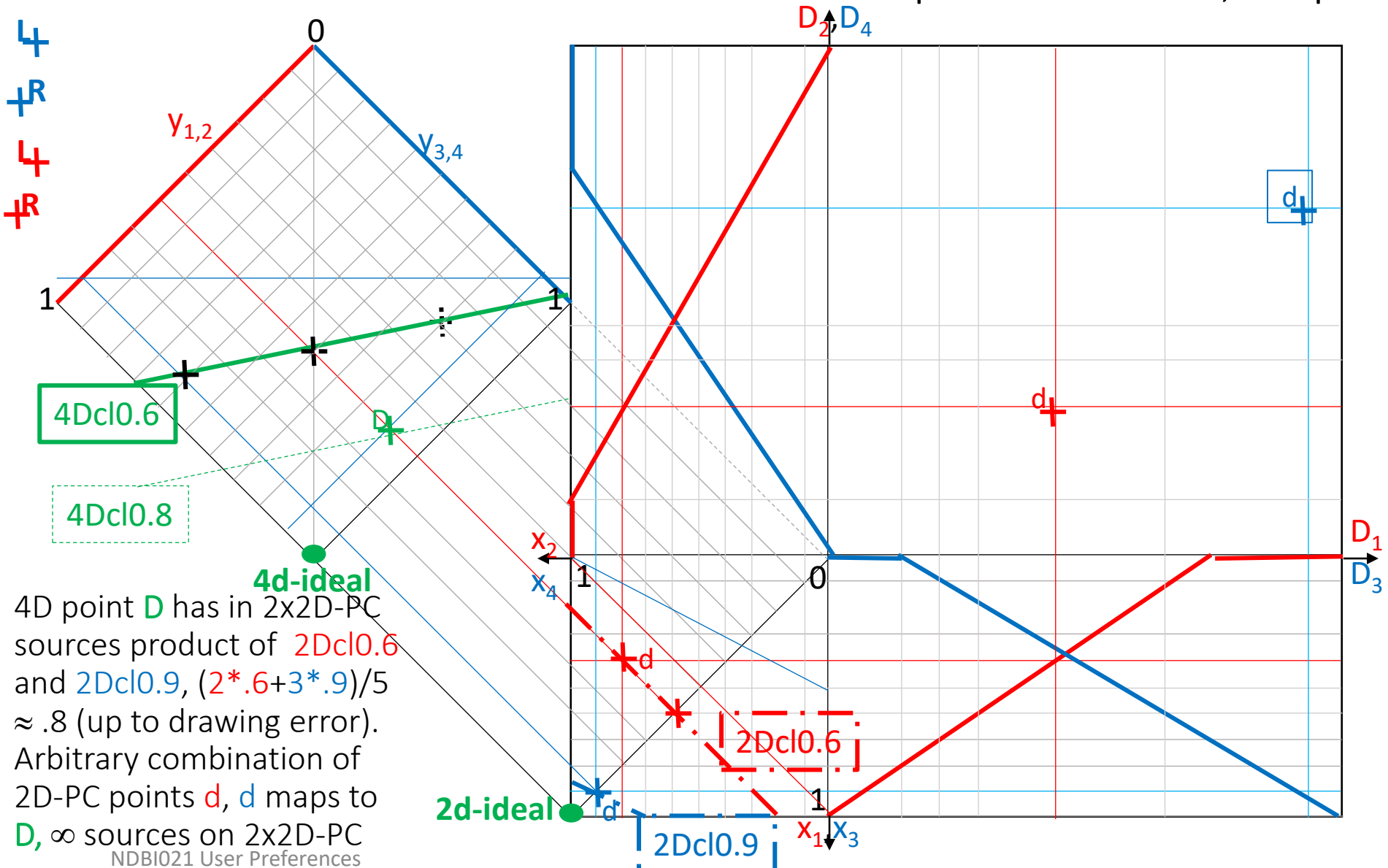
$$\frac{2 * \frac{x_1 + x_2}{2} + 3 * \frac{2 * x_3 + x_4}{3}}{5} = \frac{2 * y_{1,2} + 3 * y_{3,4}}{5} = z$$

Starting with 4dim

- 4 dim deduction – easy part
  - We know the whole model
  - DC → PC it is easy to graphical calculate an item overall preference
- 4 dim from PC → DC
  - Calculate contour lines graphically is the same as ask query:
    - “which items are preferred more than ...”
  - It is a little bit more involved as 4 dim contour lines are **3dim hyper cubes**
- Induction will be challenging
  - Because FLN-LMPM model needs to know each attribute preference separately, and
  - And our graphics (on paper) is 2 dimensional ...

$$2 * \frac{x_1 + x_2}{2} + 3 * \frac{2 * x_3 + x_4}{3} = \frac{2 * y_{1,2} + 3 * y_{3,4}}{5} = z$$

4D-PC point on 0.8-4d cl to pairs of 2d cl's, step 1



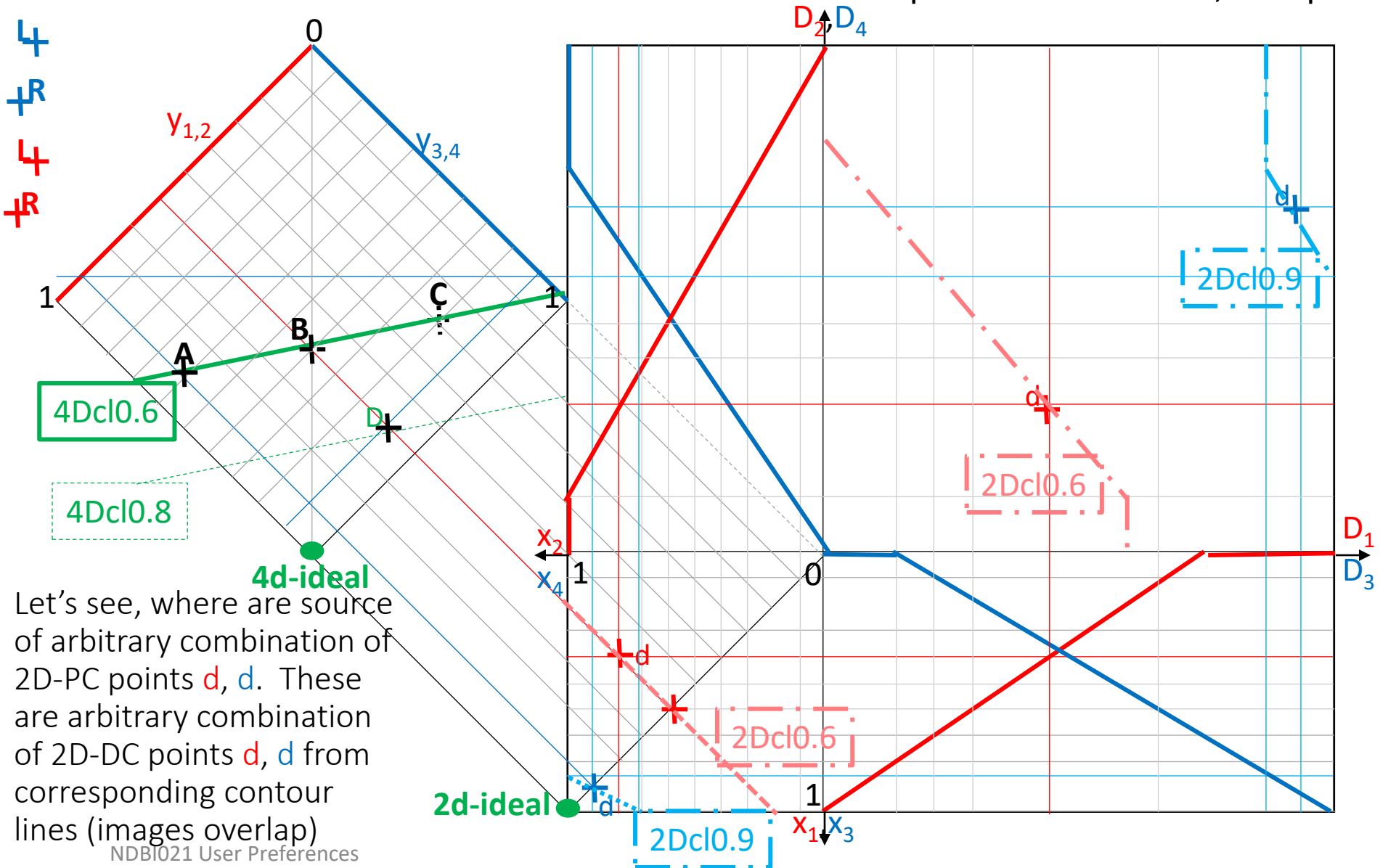
4D point **D** has in 2x2D-PC sources product of **2Dcl0.6** and **2Dcl0.9**,  $(2 * .6 + 3 * .9) / 5 \approx .8$  (up to drawing error). Arbitrary combination of 2D-PC points **d**, **d** maps to **D**,  $\infty$  sources on 2x2D-PC

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$$2 * \frac{x_1 + x_2}{2} + 3 * \frac{2 * x_3 + x_4}{3} = \frac{2 * y_{1,2} + 3 * y_{3,4}}{5} = z$$

4D-PC point on 0.8-4d cl to pairs of 2d cl's, step 2



4Dcl0.6

4Dcl0.8

4d-ideal

2d-ideal

2Dcl0.6

2Dcl0.9

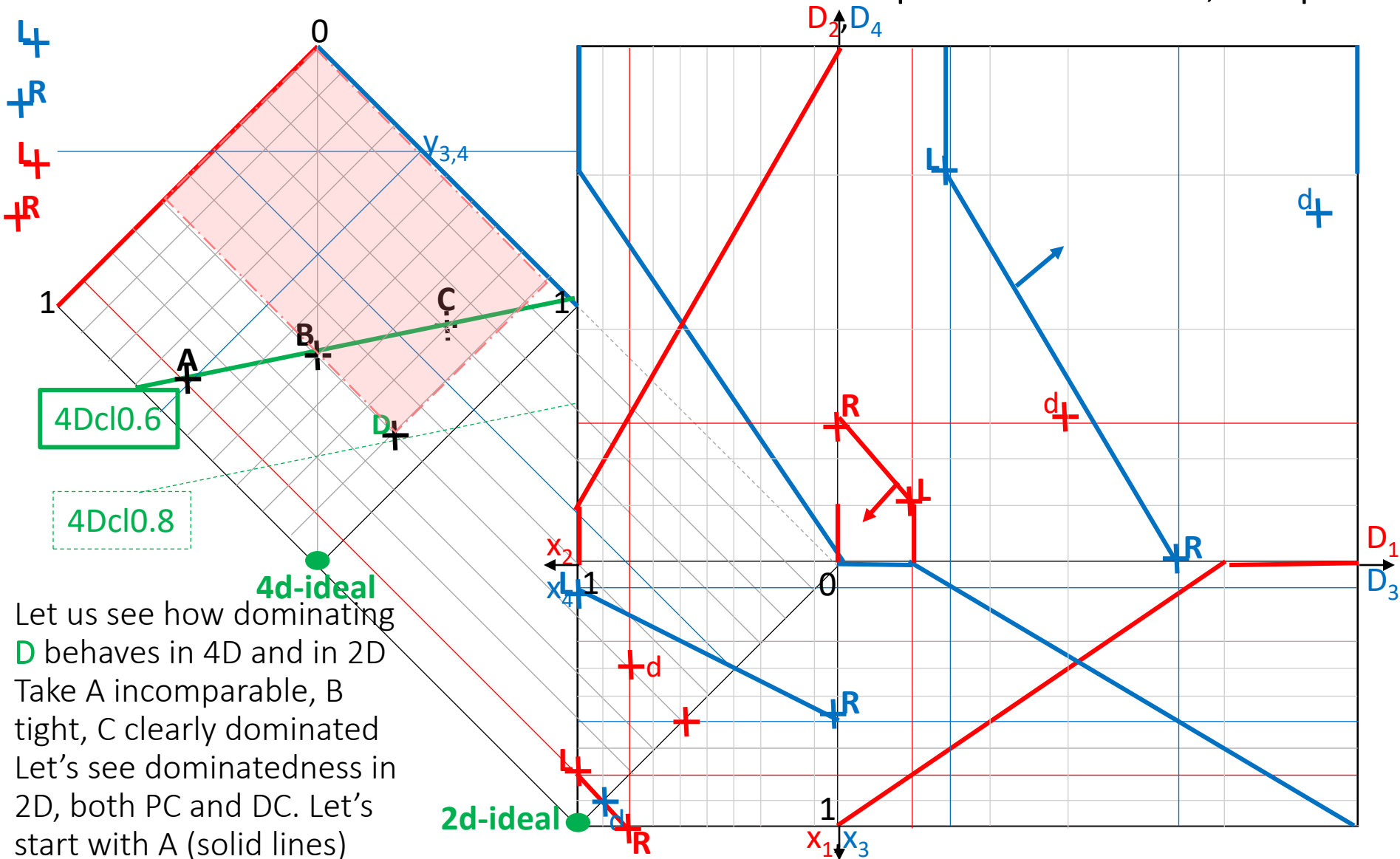
2Dcl0.6

2Dcl0.9

Let's see, where are source of arbitrary combination of 2D-PC points  $d, d$ . These are arbitrary combination of 2D-DC points  $d, d$  from corresponding contour lines (images overlap)

$$2 * \frac{x_1 + x_2}{2} + 3 * \frac{2 * x_3 + x_4}{3} = \frac{2 * y_{1,2} + 3 * y_{3,4}}{5} = z$$

0.6-4d cl to a system of pairs of 2d cl's, step 1

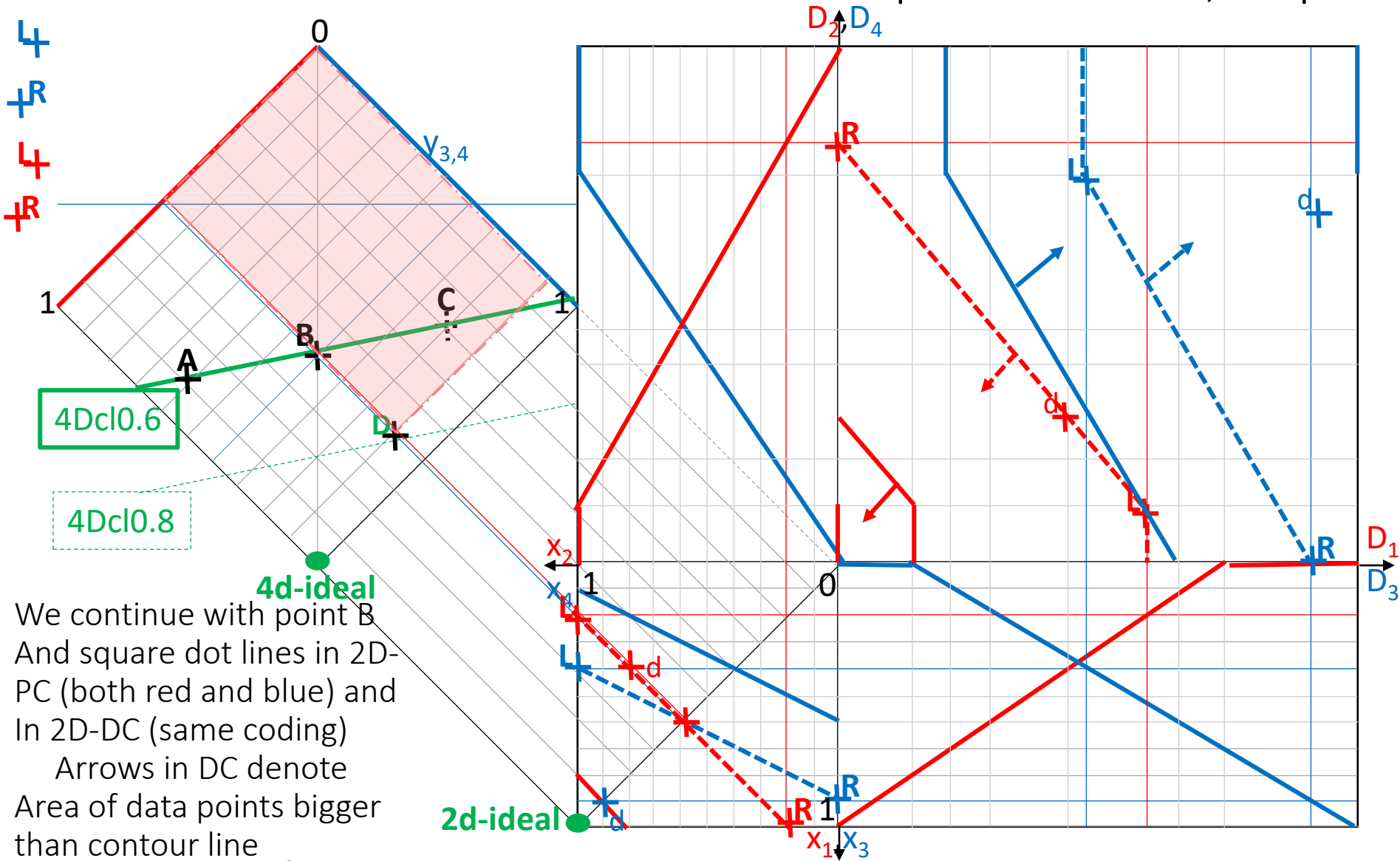


Let us see how dominating **D** behaves in 4D and in 2D  
 Take A incomparable, B tight, C clearly dominated  
 Let's see dominatedness in 2D, both PC and DC. Let's start with A (solid lines)



$$2 * \frac{x_1 + x_2}{2} + 3 * \frac{2 * x_3 + x_4}{3} = \frac{2 * y_{1,2} + 3 * y_{3,4}}{5} = z$$

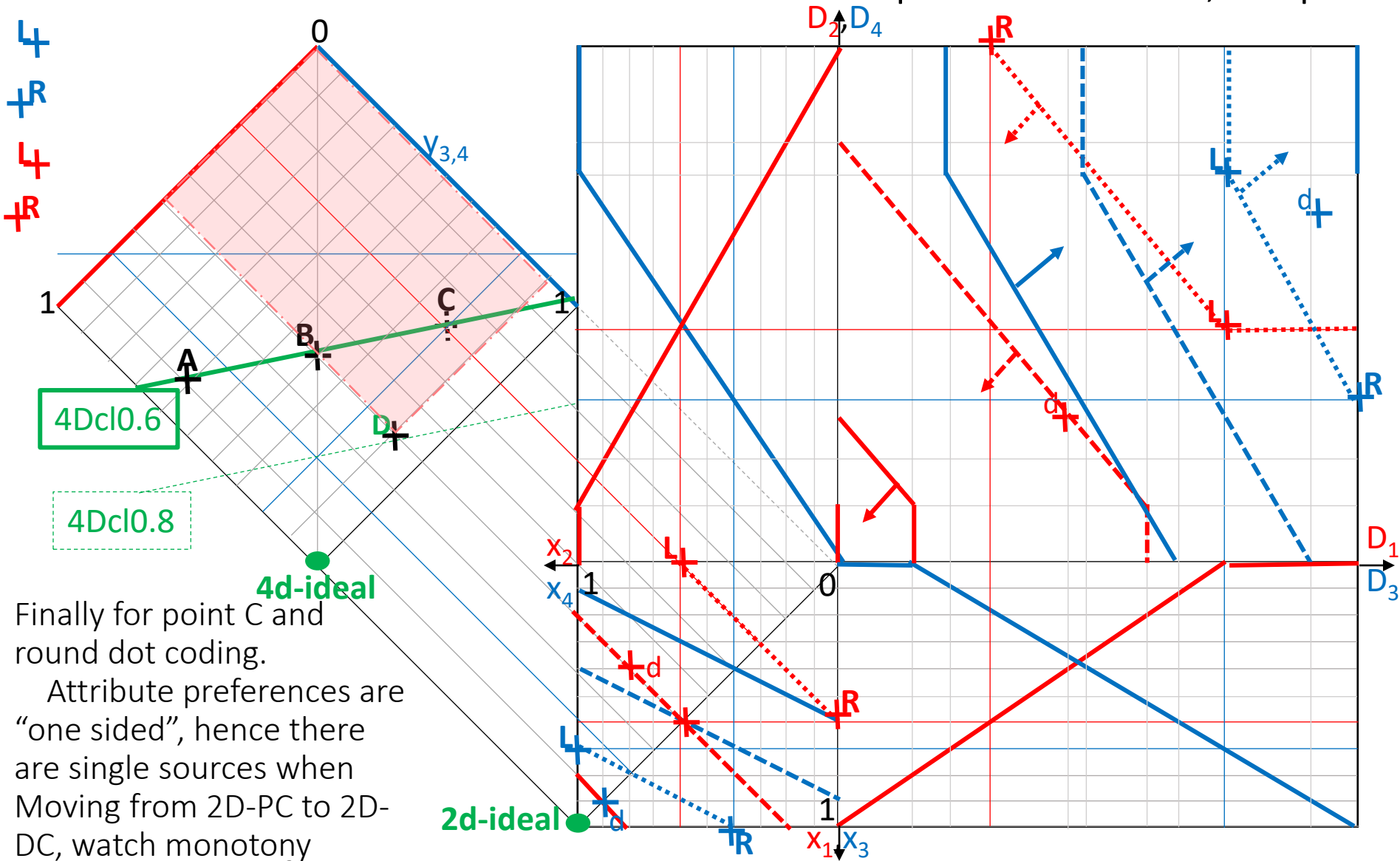
0.6-4d cl to a system of pairs of 2d cl's, step 2



We continue with point B  
 And square dot lines in 2D-PC (both red and blue) and  
 In 2D-DC (same coding)  
 Arrows in DC denote  
 Area of data points bigger  
 than contour line

$$2 * \frac{x_1 + x_2}{2} + 3 * \frac{2 * x_3 + x_4}{3} = \frac{2 * y_{1,2} + 3 * y_{3,4}}{5} = z$$

0.6-4d cl to a system of pairs of 2d cl's, step 3

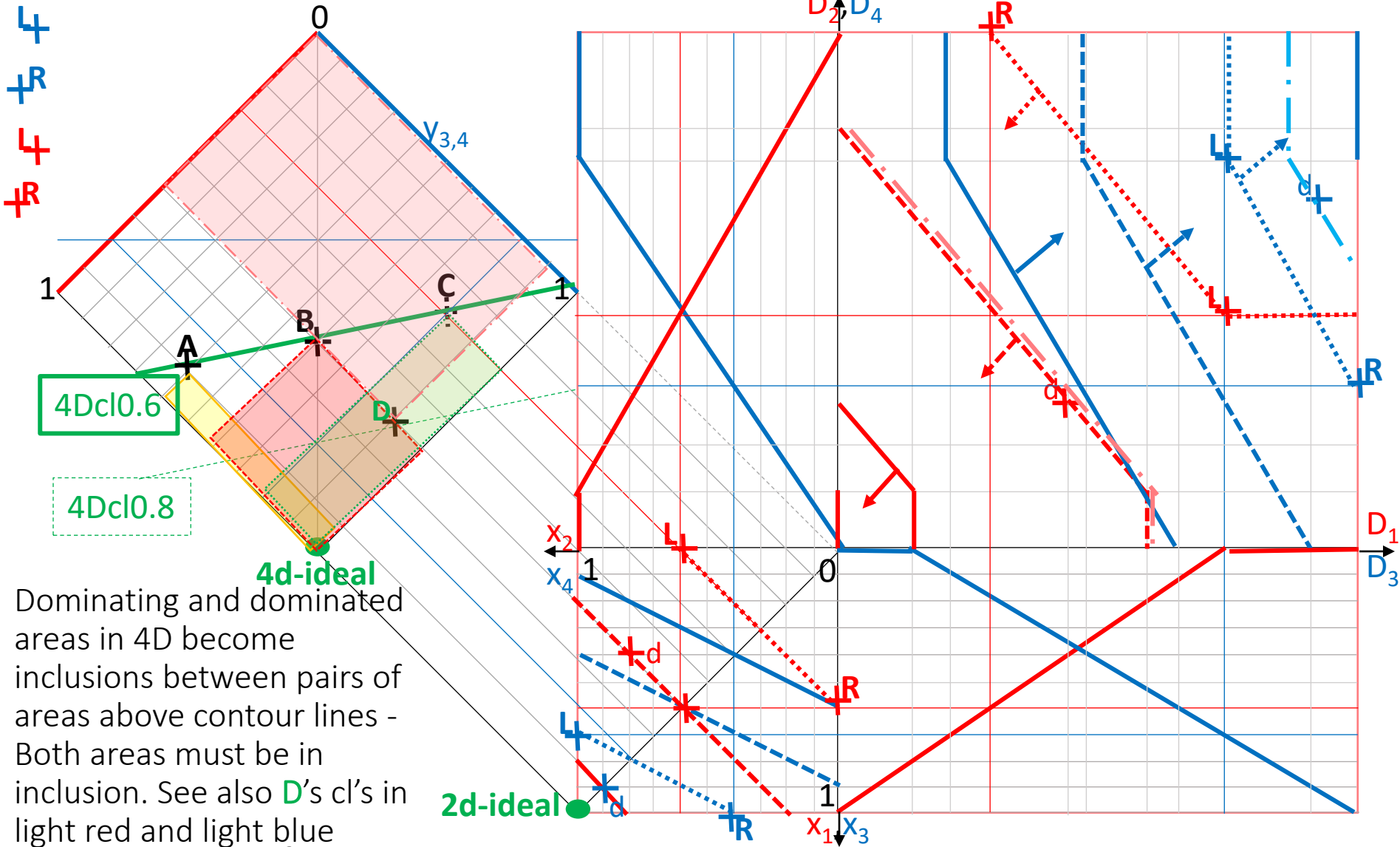


Finally for point C and round dot coding.

Attribute preferences are "one sided", hence there are single sources when Moving from 2D-PC to 2D-DC, watch monotony

$$2 * \frac{x_1 + x_2}{2} + 3 * \frac{2 * x_3 + x_4}{3} = \frac{2 * y_{1,2} + 3 * y_{3,4}}{5} = z$$

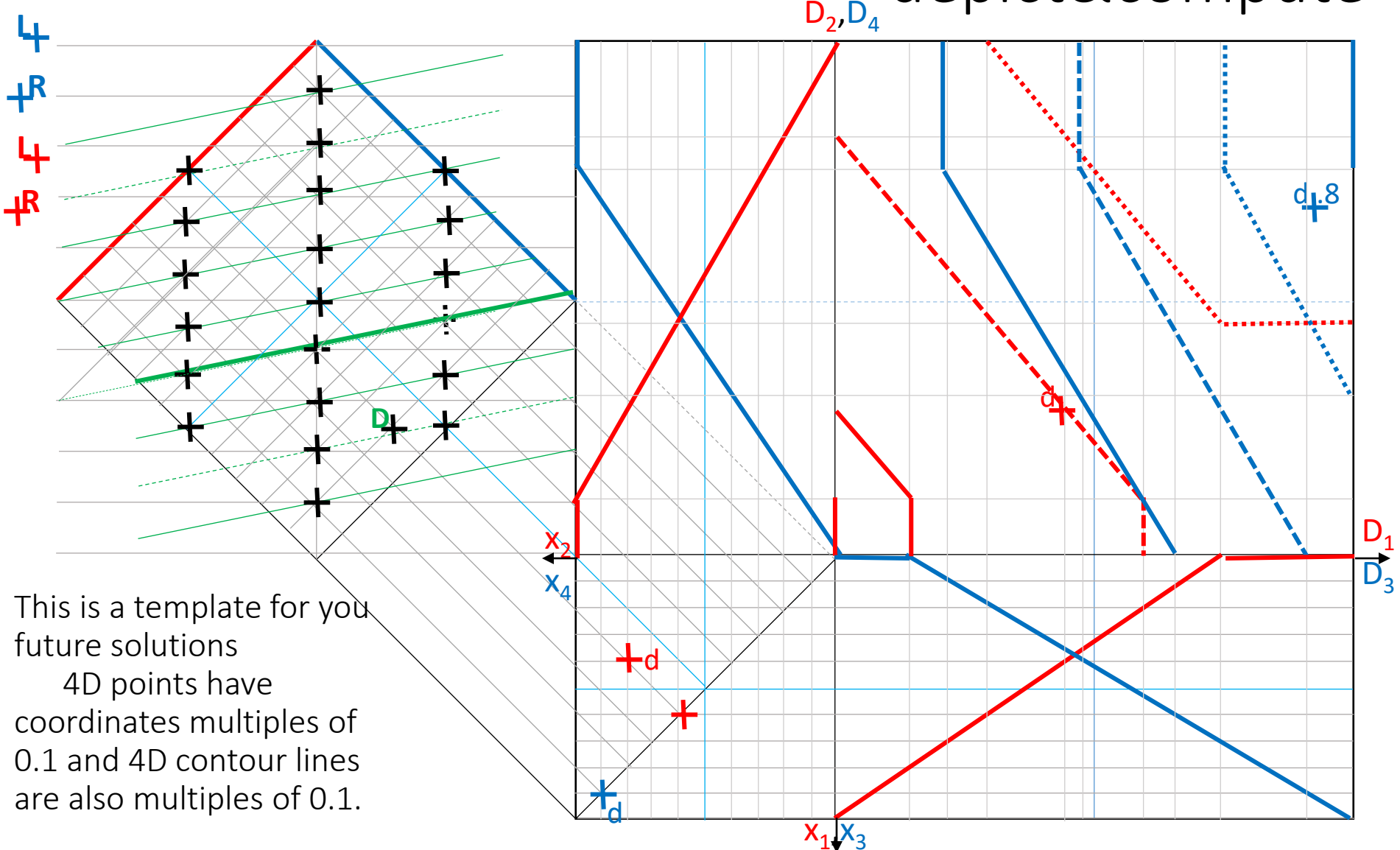
0.6-4d cl to a system of pairs of 2d cl's, step 4



Dominating and dominated areas in 4D become inclusions between pairs of areas above contour lines - Both areas must be in inclusion. See also  $D$ 's cl's in light red and light blue

$$2 * \frac{x_1 + x_2}{2} + 3 * \frac{2 * x_3 + x_4}{3} = \frac{2 * y_{1,2} + 3 * y_{3,4}}{5} = z$$

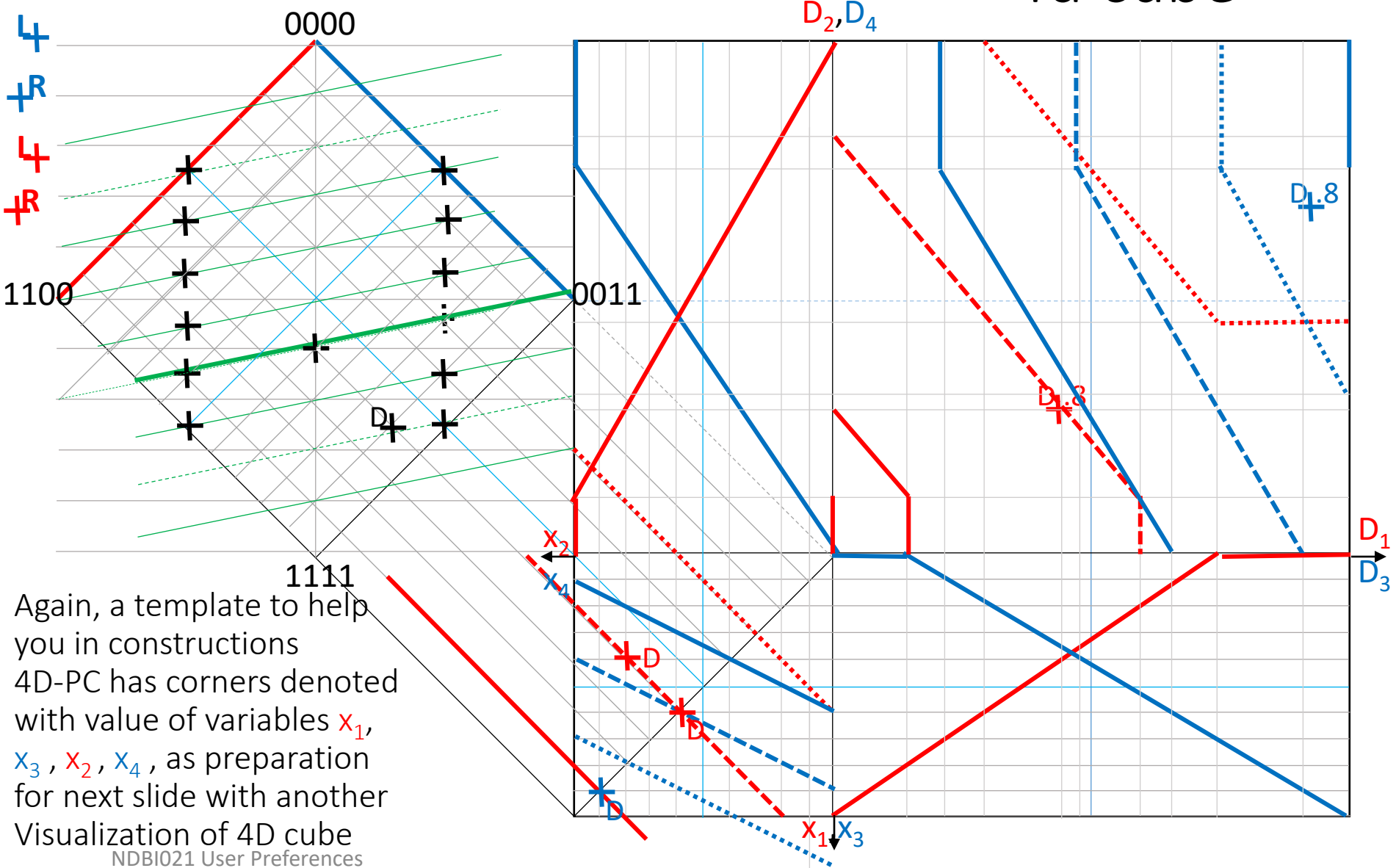
4d points easy to depict & compute



This is a template for you future solutions  
 4D points have coordinates multiples of 0.1 and 4D contour lines are also multiples of 0.1.

$$2 * \frac{x_1 + x_2}{2} + 3 * \frac{2 * x_3 + x_4}{3} = \frac{2 * y_{1,2} + 3 * y_{3,4}}{5} = z$$

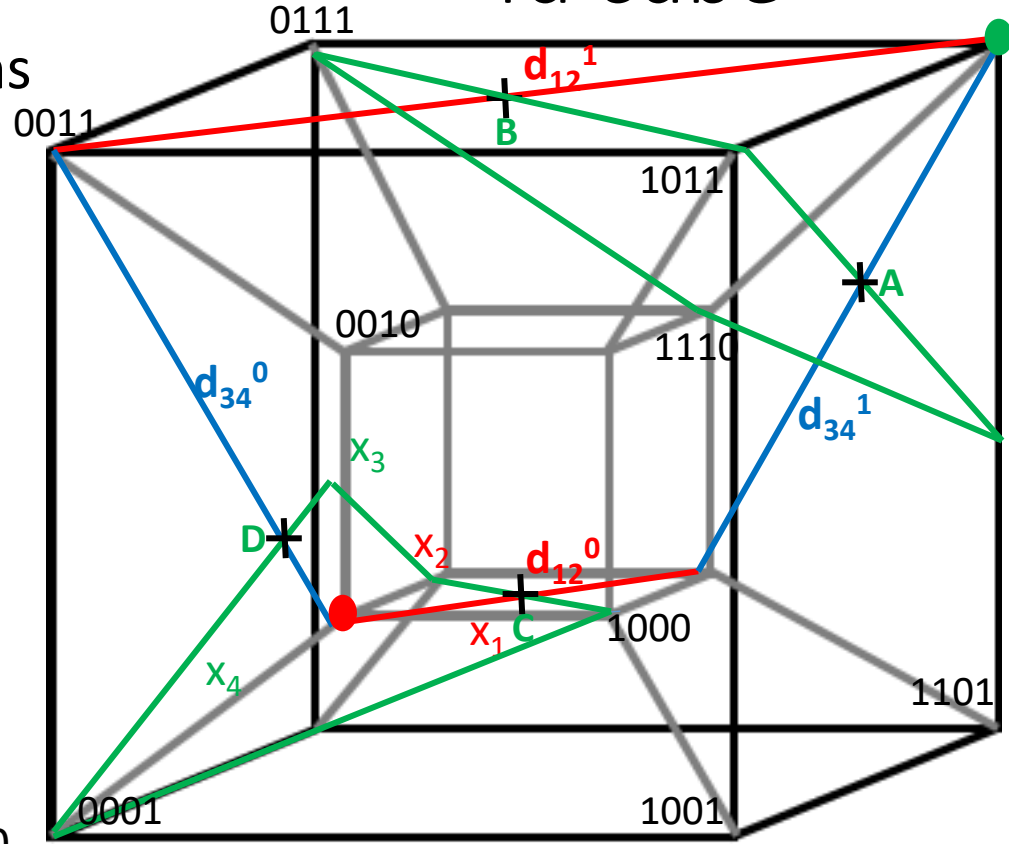
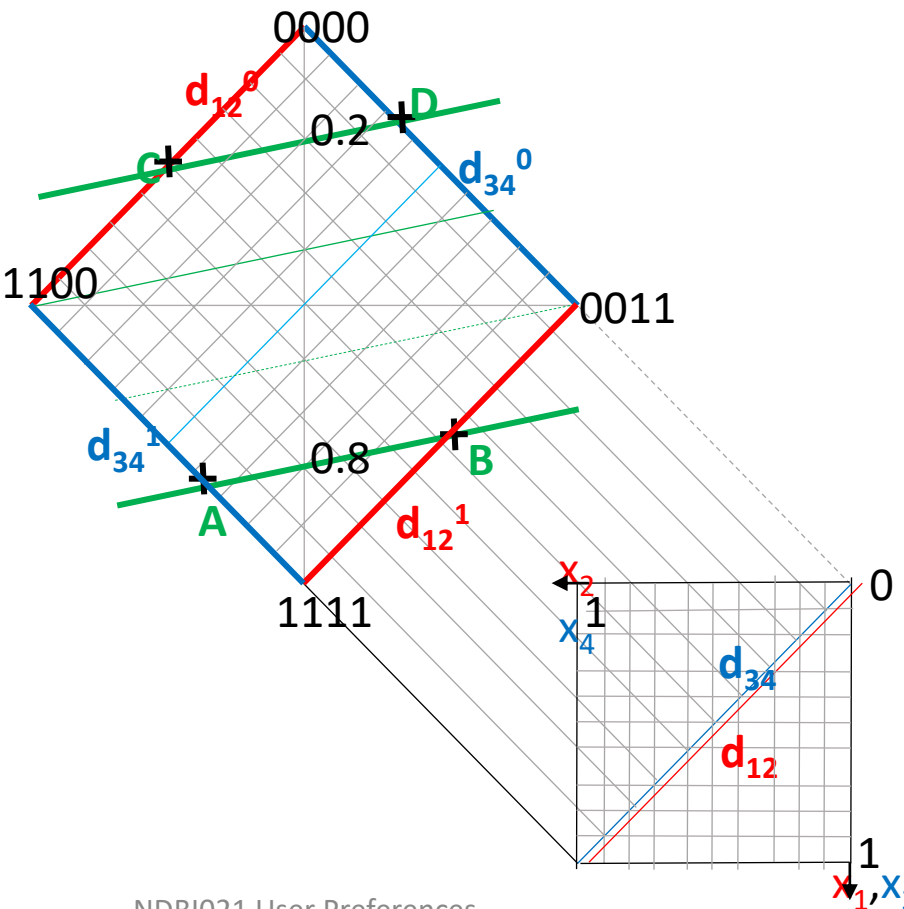
To compare with 4d cube



Again, a template to help you in constructions  
 4D-PC has corners denoted with value of variables  $x_1, x_3, x_2, x_4$ , as preparation for next slide with another Visualization of 4D cube

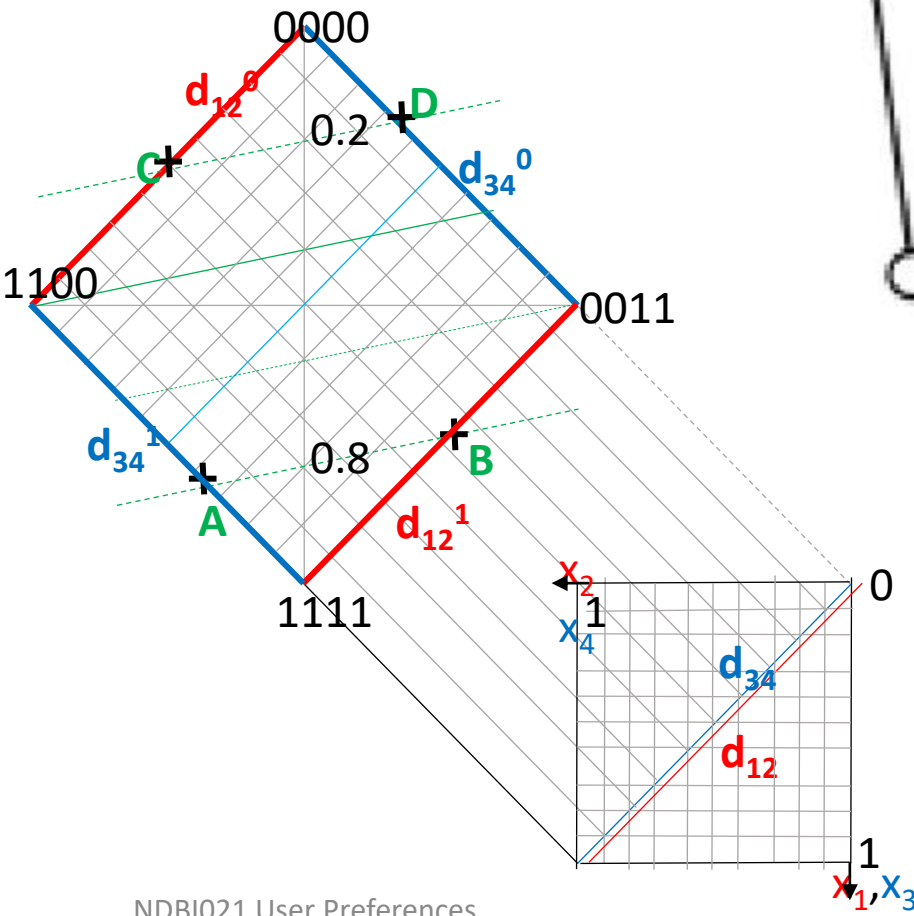
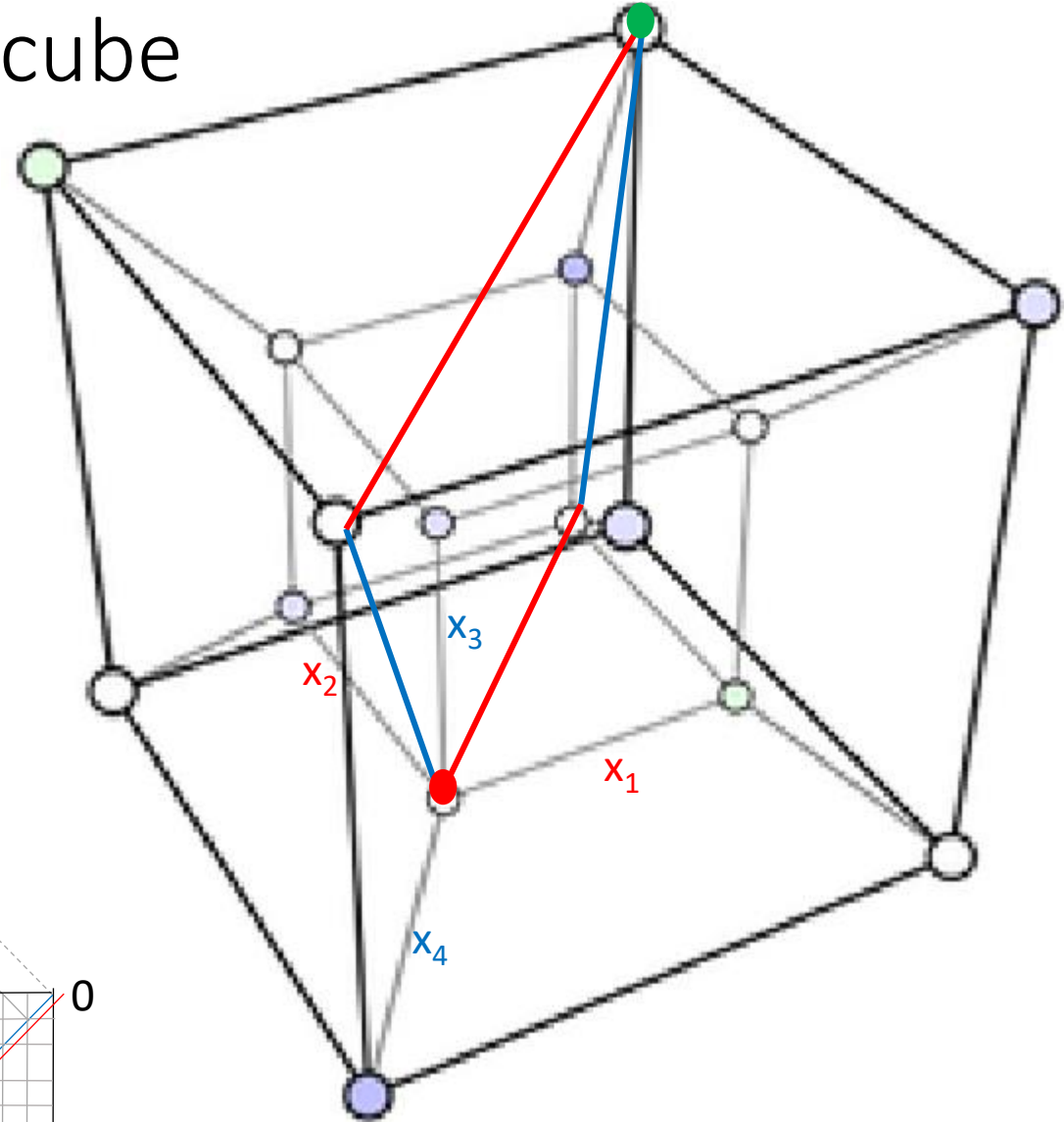
0.2/0.8 contour line in 4D is a 3D hypercube, here only intersections with 4D-cube faces are depicted

To compare with 4d cube



Each visualization has some advantages and disadvantages, please comment

Another view of 4d cube  
 construct all as in  
 previous slide



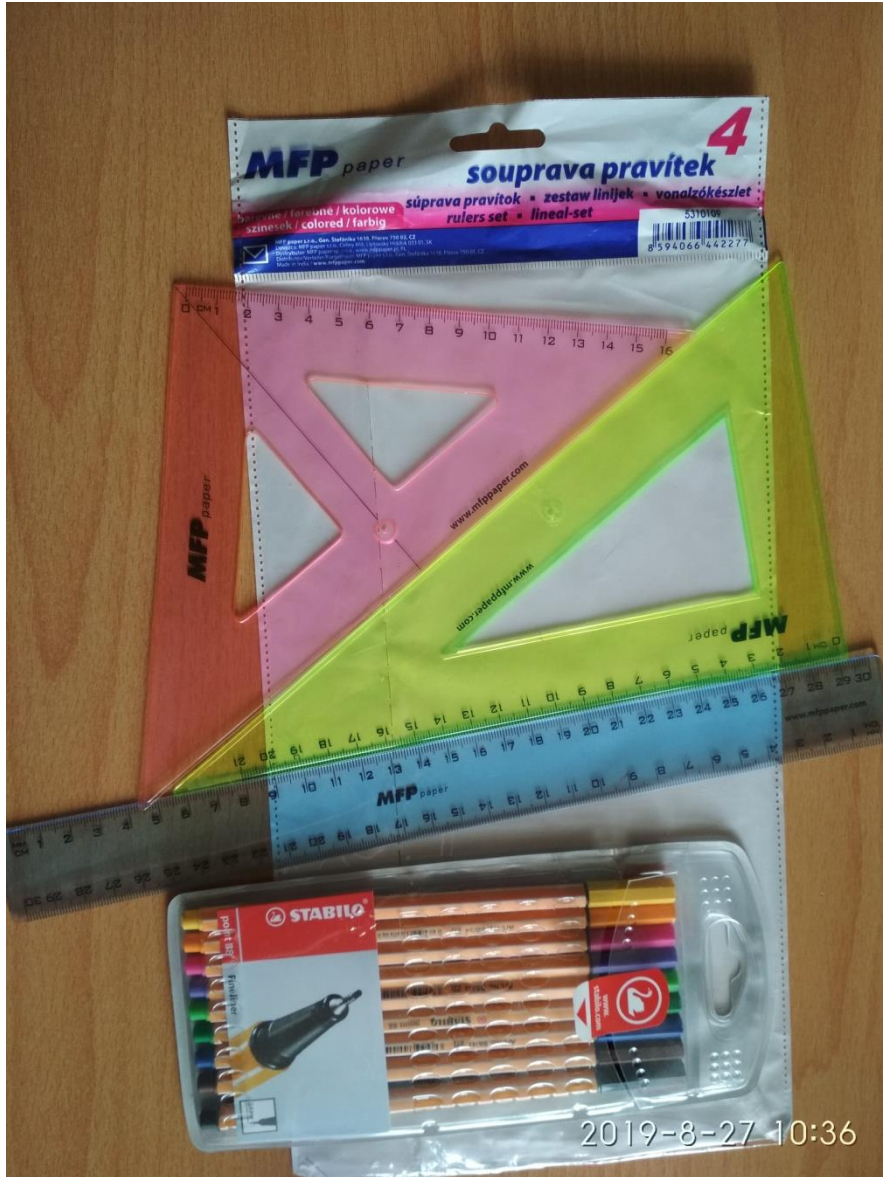
What is preserved? What not?  
 Parallelism, ratio of distances? ...

# No coding, simulation using drawing tools





# Main Railway station, southern wing

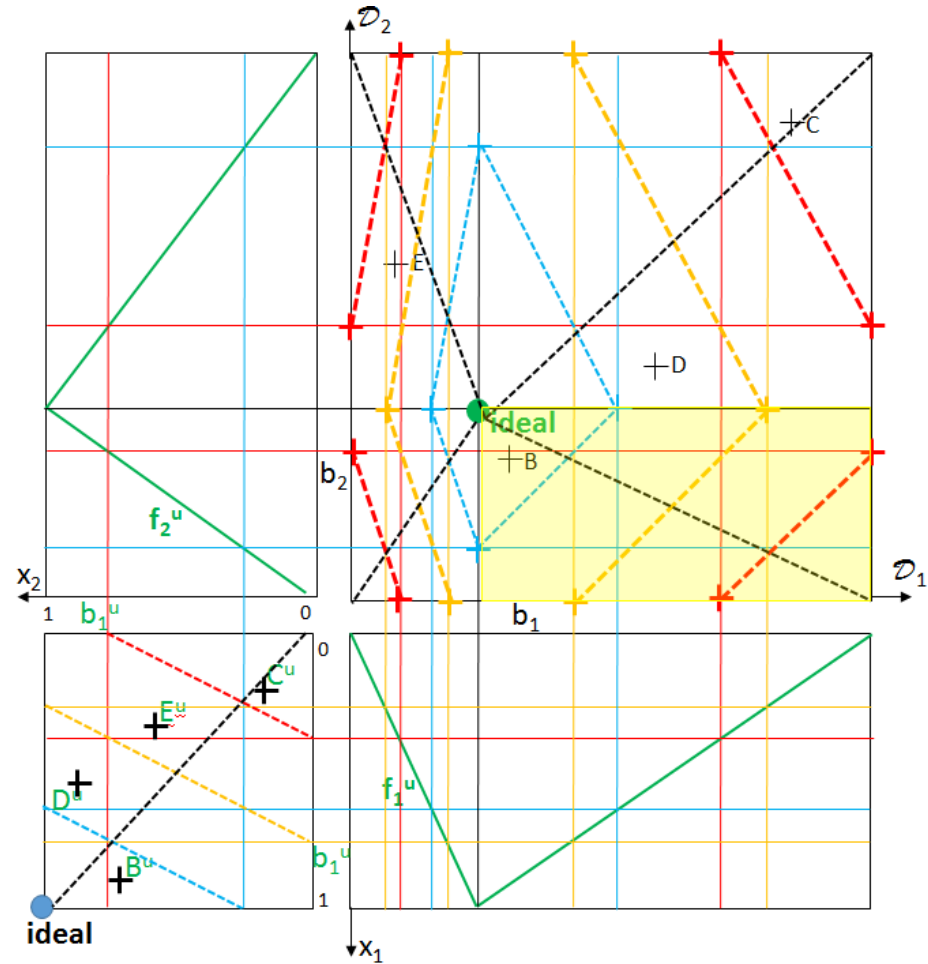
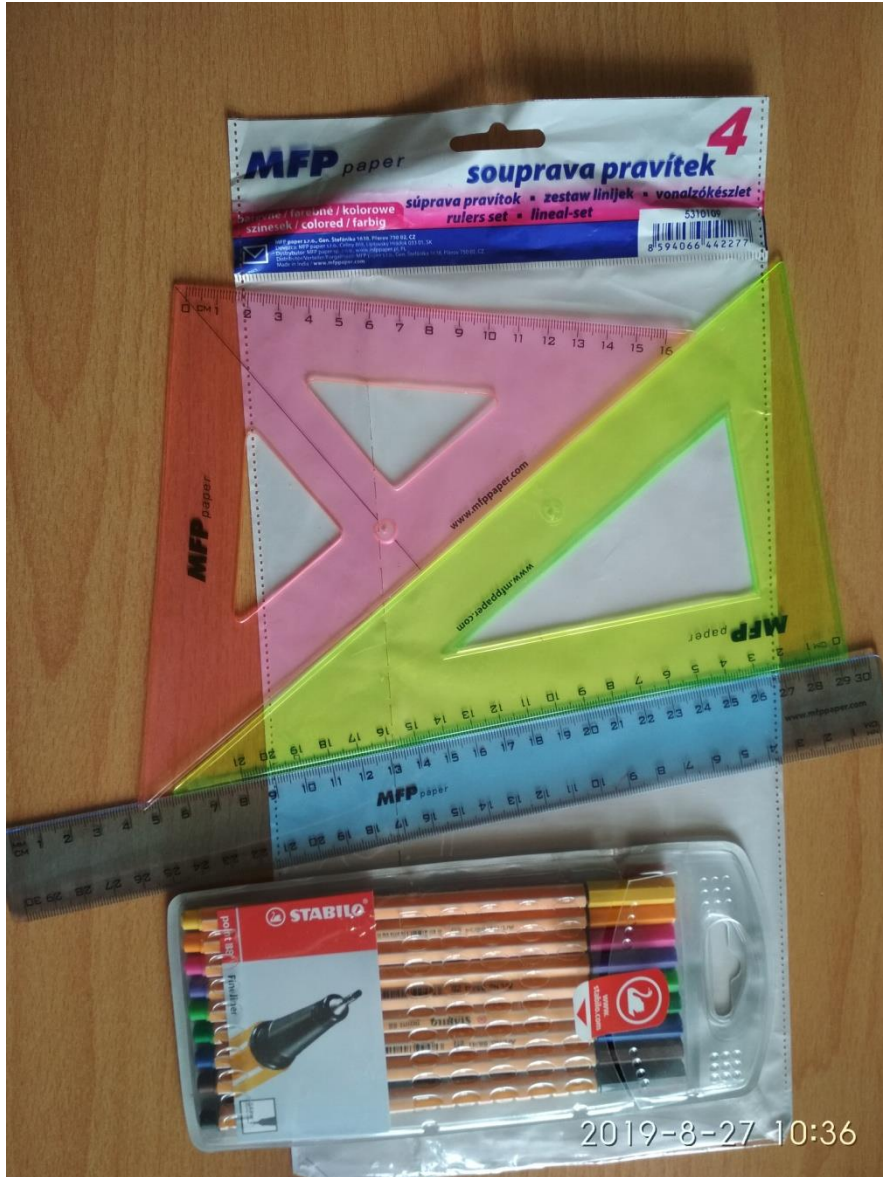


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Introduction

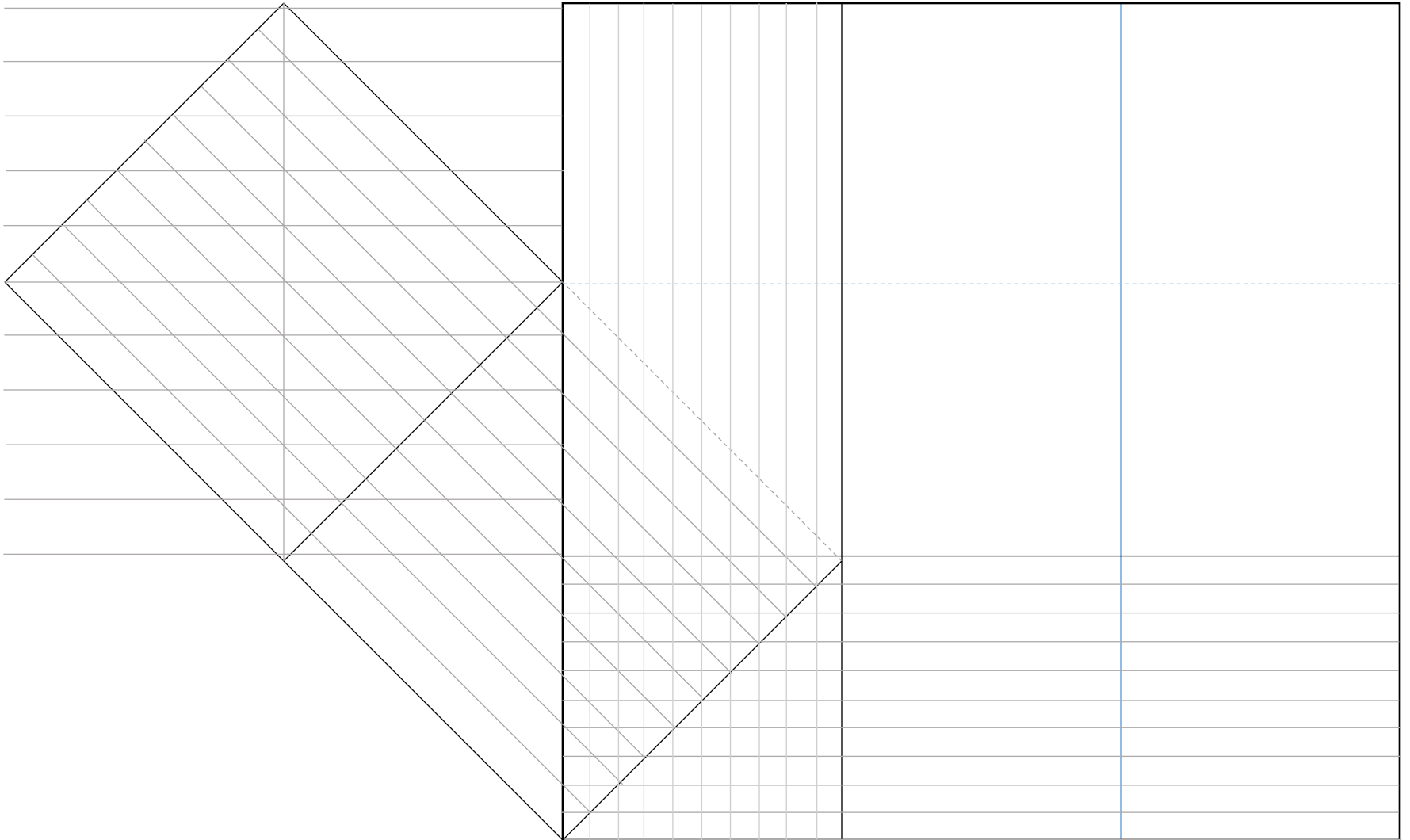
# Our solutions will look like ...



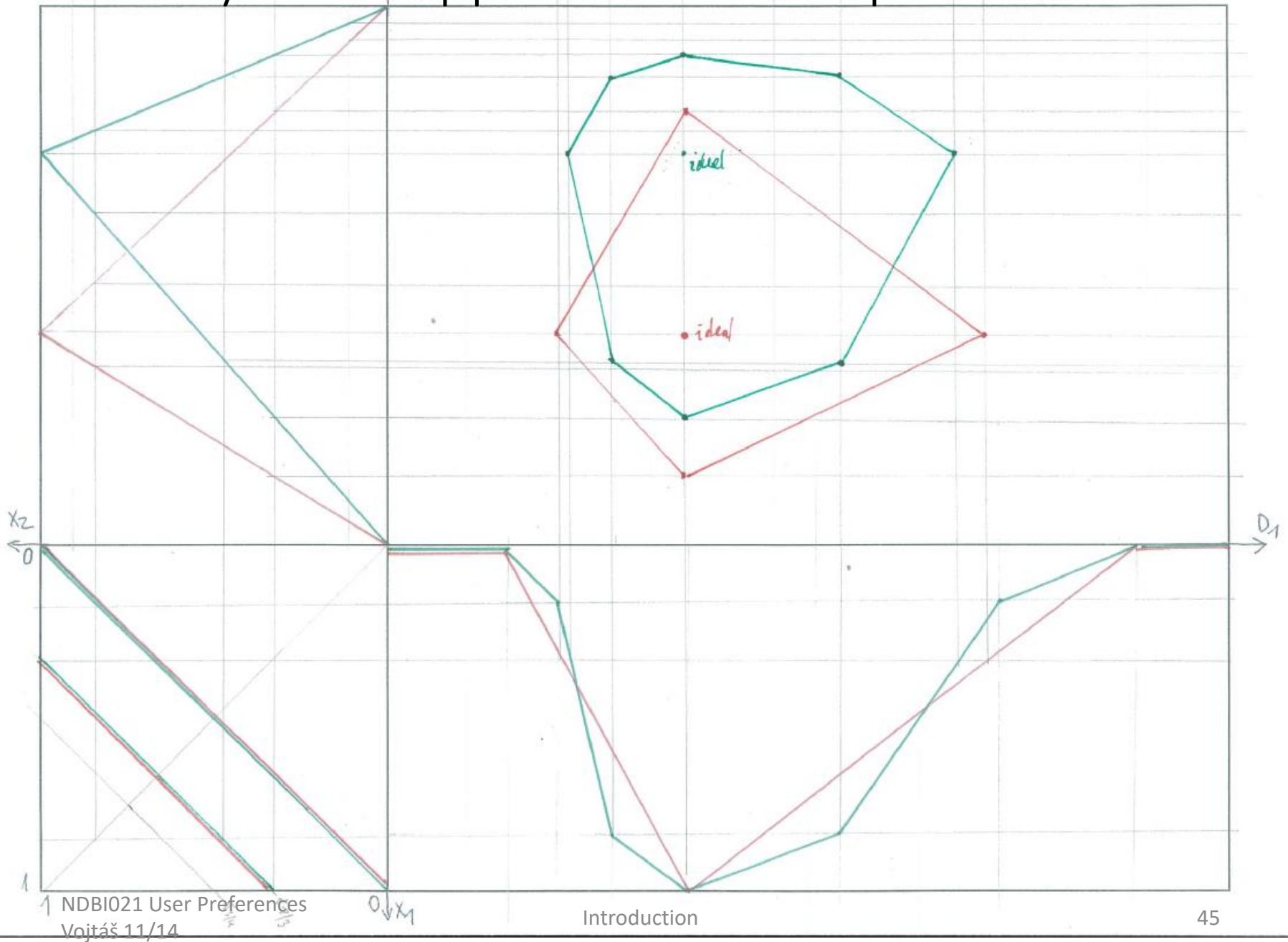
Questions?

Comments?

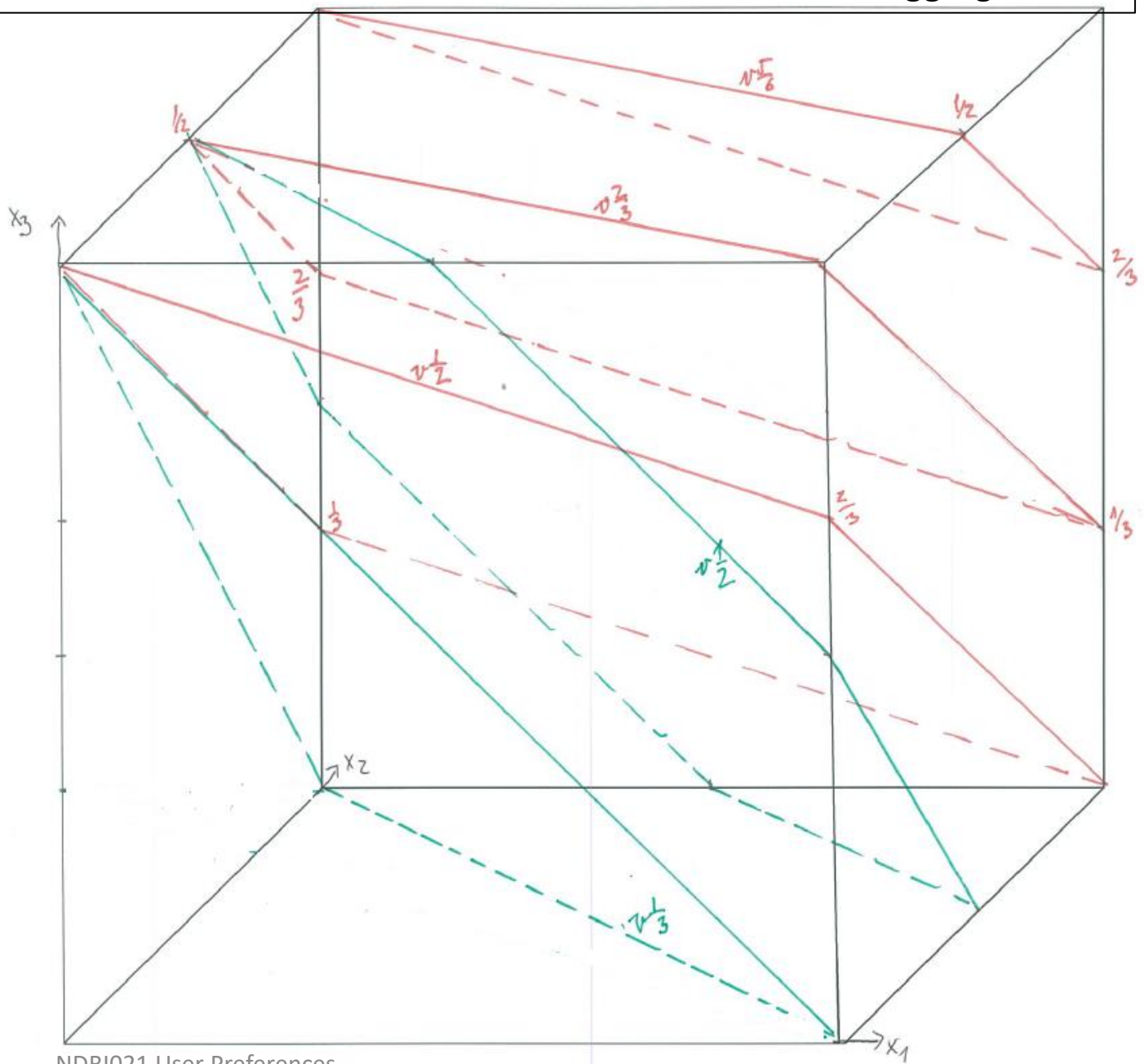
# We will use framework for 4dim, ...



# Partially linear approximations of preferences

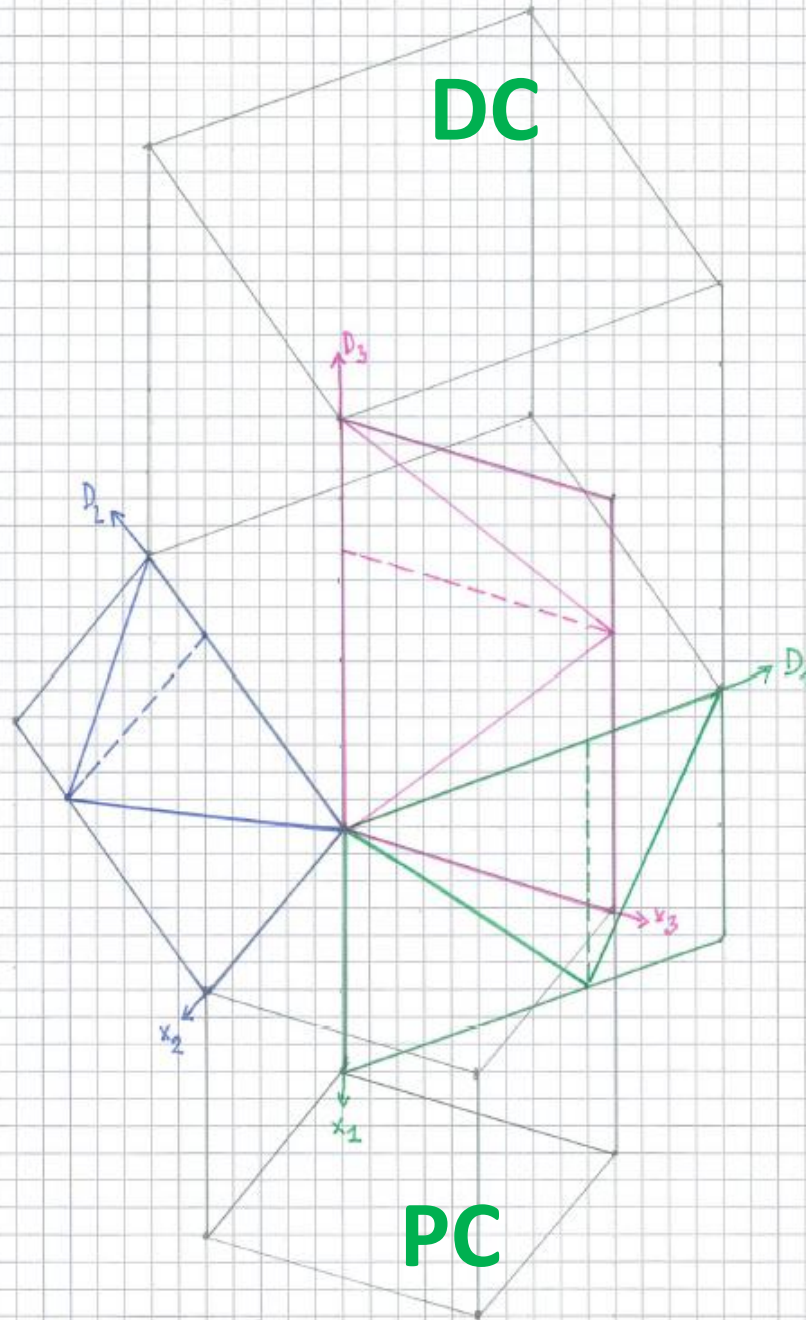


# Preference cube in 3D with contour surface wrt different aggregations



$$\frac{x_1 + 2x_2 + 3x_3}{6}$$

$$\frac{x_1 + x_2 + x_3}{3}$$



**Dynamical model** – three sessions – moving ideal points (aggregations remain same)

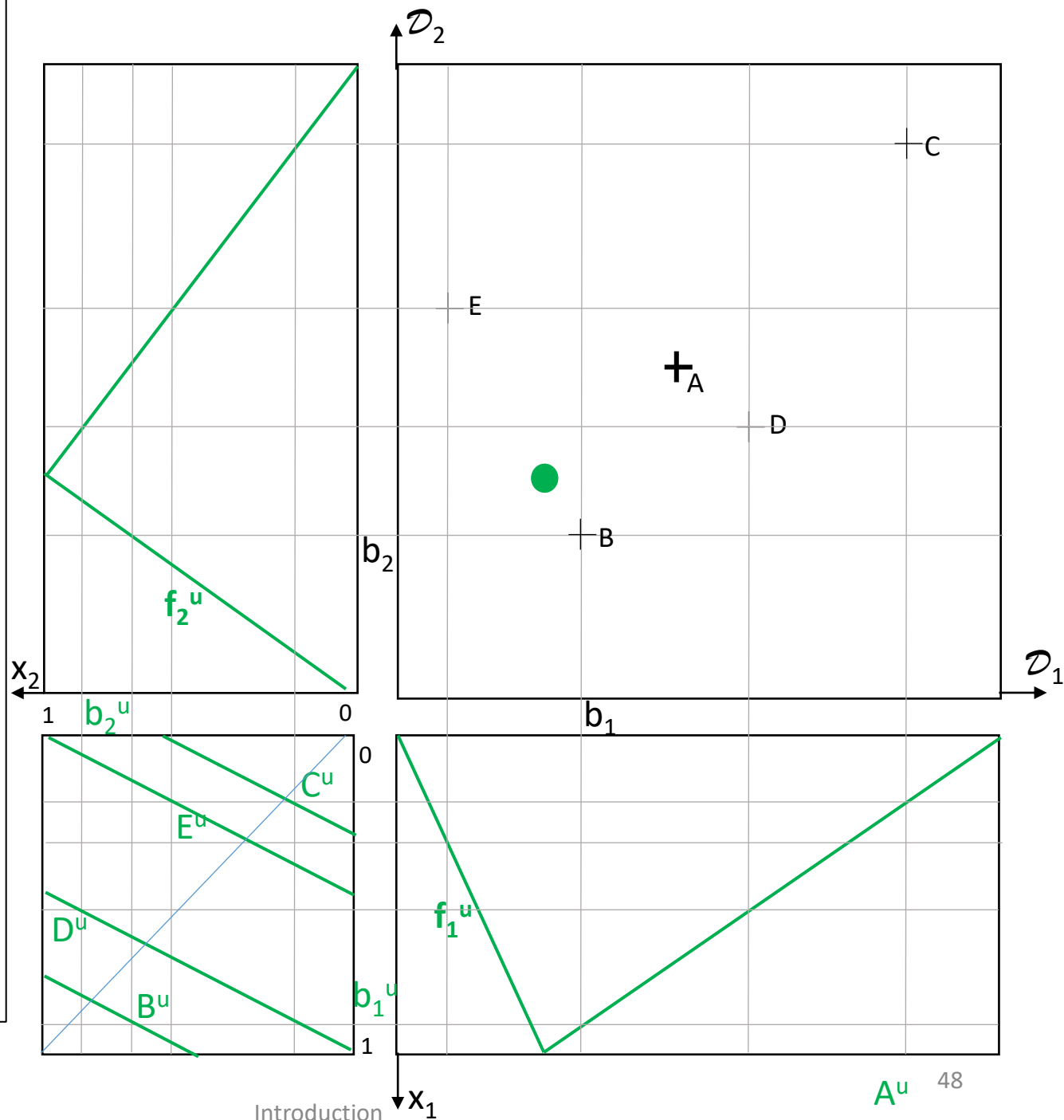
Simulation of development in time

Starting vector of attribute preferences  $f^0$  and aggregation  $t^0$  define an user  $u^0_{f,t} = u^0$  in time 0. Depict contour line in DC-data cube.

Assume user clicks on third item. In time 1,  $t^0 = t^1$ , ideal is clicked item (triangular max-min shape remains).

In time 1 user clicks on second item – this becomes ideal in time 2.

Describe order in time 2.





Dynamical model – three sessions – moving ideal points (aggregations remain same)

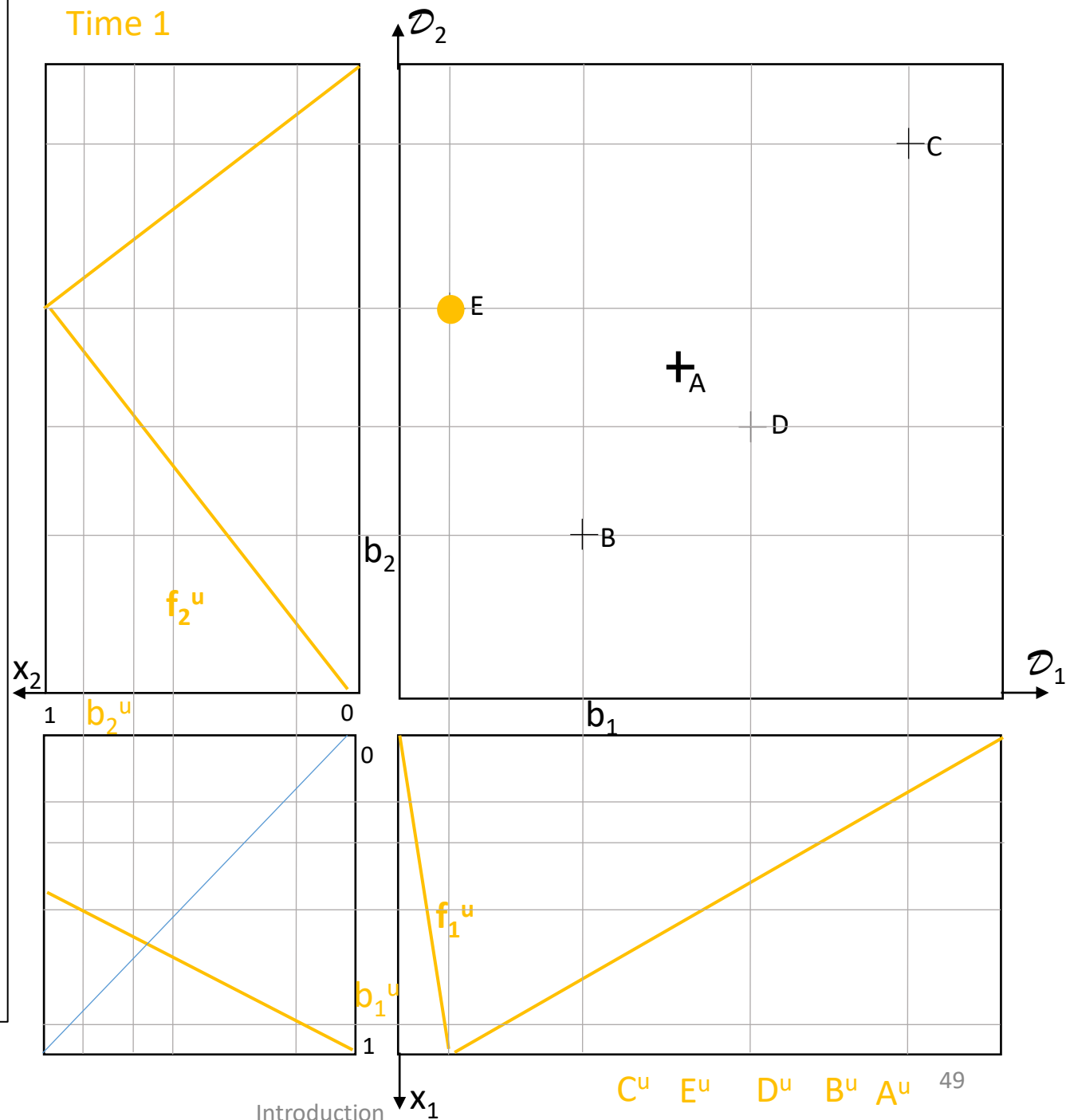
Simulation of development in time

Starting vector of attribute preferences  $f^0$  and aggregation  $t^0$  define an user  $u^0_{f,t} = u^0$  in time 0. Depict contour line in DC-data cube.

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In time 1 user clicks on second item – this becomes ideal in time 2.

Describe order in time 2.



Dynamical model – three sessions – moving ideal points (aggregations remain same)

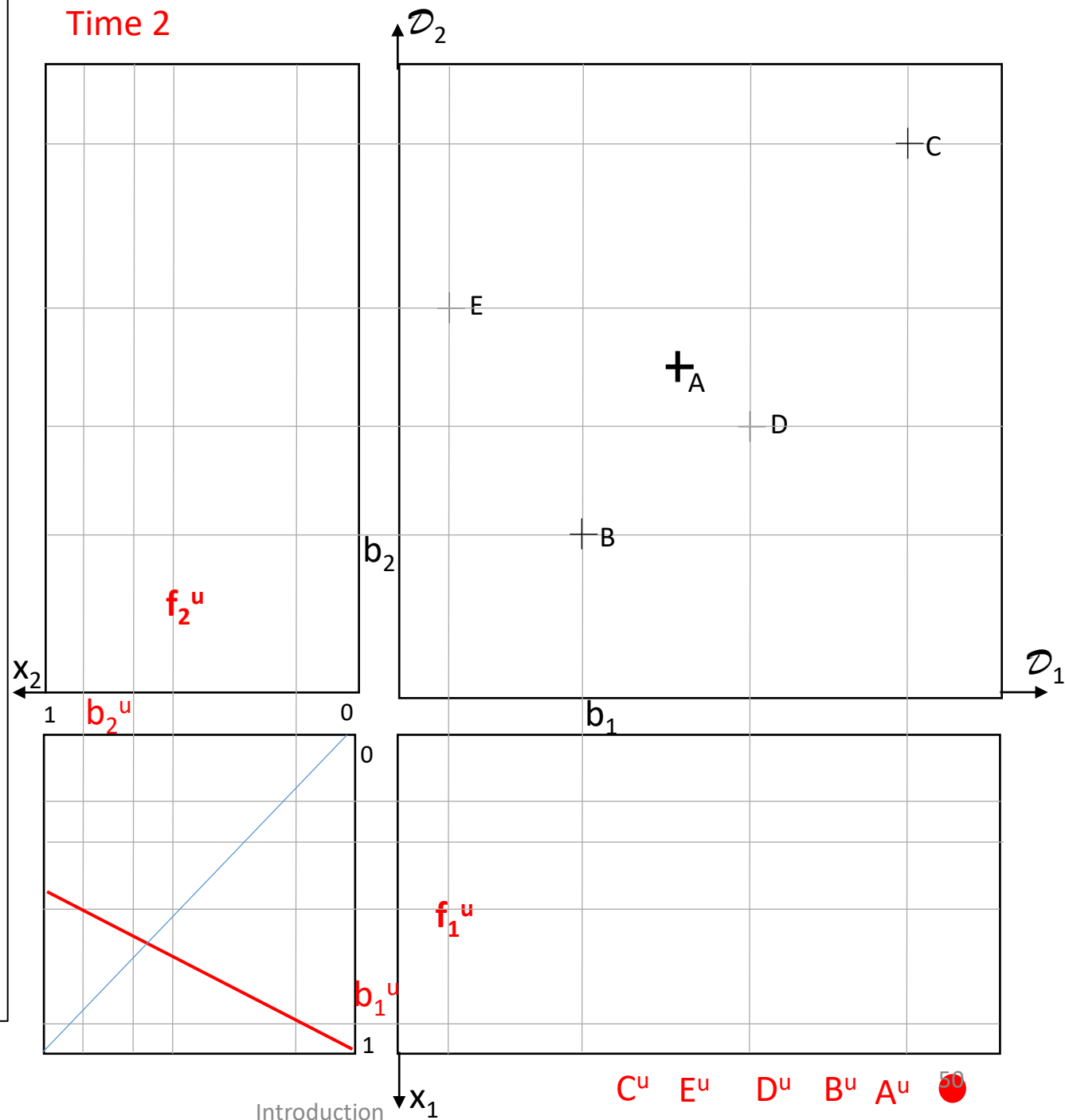
Simulation of development in time

Starting vector of attribute preferences  $f^0$  and aggregation  $t^0$  define an user  $u^0_{f,t} = u^0$  in time 0. Depict contour line in DC-data cube.

Assume user clicks on third item. In time 1,  $t^0 = t^1$ , ideal is clicked item (triangular max-min shape remains).

In time 1 user clicks on second item – this becomes ideal in time 2.

Describe order in time 2.



Dynamical model – three sessions – moving ideal points and **moving aggregation**

Simulation of development in time  
 Starting vector of attribute preferences  $f^0$  and aggregation  $t^0$  define an user  $u^0_{f,t} = u^0$  in time 0. Depict contour line in DC-data cube.

Assume user clicks on third item. In time 1,  $t^0 = t^1$ , ideal is clicked item (triangular max-min shape remains).

In time 1 user clicks on second item – this becomes ideal in time 2.

Describe order in time 2.

