

Solution

NDB1007: Practical class 2

Exercise 2.1: Primary Key Index (Solution)

- * Blocking factor of primary file $b = \left\lfloor \frac{B}{R} \right\rfloor = \left\lfloor \frac{4 \cdot 2^{10}}{256} \right\rfloor = 16$
 - * Number of blocks of primary file $n_B = 12,000,000 \div 16 = 750,000$
 - * Blocking factor of primary key index $b_{ID} = \left\lfloor \frac{B}{R} \right\rfloor = \left\lfloor \frac{4 \cdot 2^{10}}{9} \right\rfloor = 455$
- Primary key index levels
 - * The number of pages to index: 750,000, level size: $n_{PAGES,L=i} = \left| \frac{n_{PAGES,L=i-1}}{b} \right| = \left| \frac{750,000}{455} \right| = 1649$
 - The number of pages to index: 1649, level size: $\left| \frac{1649}{455} \right| = 4$
 - The number of pages to index: 4, level size: $\left[\frac{4}{455}\right] = 1$

Exercise 2.2: Direct Index (Solution)

* Blocking factor
$$b_{FIRST_NAME} = \left\lfloor \frac{B}{R} \right\rfloor = \left\lfloor \frac{4 \cdot 2^{10}}{29} \right\rfloor = 141$$

- Direct index levels
 - Number of records in primary file: 12,000,000, level size: $\left[\frac{12,000,000}{141}\right] = 85,107$
 - Number of pages to address: 85,107, level size: $\left[\frac{85,107}{141}\right] = 604$
 - Number of pages to address: 604, level size: $\left[\frac{604}{141}\right] = 5$
 - Number of pages to address: 5, level size: $\left[\frac{5}{141}\right] = 1$
- * The total size of index is 85,107 + 604 + 5 + 1 = 85,717 so the space equals to $85,717 \cdot 4 \cdot 2^{10} \approx 335 \ MB$
 - * The size of this index is much larger than the size of the primary key index, i.e., that is $(1649 + 4 + 1) \cdot 4 \cdot 2^{10} \approx 6 \ MB$

Exercise 2.3: Indirect Index (Solution)

- * First level blocking factor is $b_{SECOND_NAME,FIRST_LEVEL} = \left\lfloor \frac{B}{R} \right\rfloor = \left\lfloor \frac{4 \cdot 2^{10}}{37} \right\rfloor = 110$
- Other level blocking factor is $b_{SECOND_NAME,OTHER_LEVELS} = \left\lfloor \frac{B}{R} \right\rfloor = \left\lfloor \frac{4 \cdot 2^{10}}{36} \right\rfloor = 113$
- Indirect index levels
 - Number of records to address: 12,000,000, level size: $\left[\frac{12,000,000}{110}\right] = 109,091$
 - Number of pages to address: 109,091, level size: $\left[\frac{109,091}{113}\right] = 966$
 - Number of pages to address: 966, level size: $\left[\frac{966}{113}\right] = 9$
 - Number of pages to address: 9, level size: $\left[\frac{9}{113}\right] = 1$