

Query Optimization

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DBMS context

- A key module of DBMS
- Goal: to make optimization independent on strategy query expression

Counterexamples: navigational languages, SQL interpreter

- Parallel to evaluation of arithmetic expressions
 - Here: time complexity of operations of A_R using I/O operations
 - Crucial factors: size of relations, size of active domains, indexes, hashing, bitmaps etc.



Query languages 1

Optimizer

Phases of query processing

- Transfer into the internal form
 - SQL $\rightarrow A_R$
 - linear expression \rightarrow tree
 - Remark: calculi $\leftarrow \rightarrow A_R$ in polynomial time depending on the expression length
- conversion into canonic form
- > optimization
- evaluation plan
- code generating

Overview of the problem

Evaluation plan: query tree + algorithm for each operation.

- Two main ideas:
 which plans are considered for given query?
 how to estimate the plan cost ?
- From the plans considered it is chosen the one with the least cost.

Ex..: System R

- > using statistic data for cost estimation,
- > using equivalent algebraic expressions,
- restriction to *left-deep* plans.

Example of a schema

Clients (*client_ID*: int, *name*: string, *category*: int, *age*: real) Booking(*client_ID*: int, *flight_n*: int, *date*: date, *remark*: string)

- Semantics: Clients book their flights until a given date. Parameters: B = 4 KByte
- Booking:

R = 40 Byte, b = 100, $p_B = 1000$ pages.

Clients:

R = 50 Bytes, b = 80, $p_c = 500$ pages.

Alternative 1

SELECT C.name FROM Booking B, Clients C WHERE B.client_ID=C.client_ID AND B.flight_n=100 AND C.category>5

name

 Plan: join by nested-loops, selection+projection when the result is generated

- ✤ Cost: 500+500*1000 I/Os
- Apparently, the worst plan!
- Use possibilities: selections should be evaluated earlier, available indexes, etc.
- Optimization goal: To find the most effective plans, which lead to the same result (answer).





Sum: 1000+1+500+166 + 2*1*1 + 2*4*166 + 1 + 167 = 3027 I/O operations.

Query languages 1

(with indexes) With clustered index *flight_n* in Booking, we obtain 100,000/100 = 1000 tuples on 1000/100 = 10 pages.

 Join attribute is a key in Clients
 > at most one tuple, unclustered index on *client_ID* OK.

Alternative 3



- The decision not to propagate category >5 before join is based in the availability of index client_ID in table Clients.
- Cost: reading pages from Booking (10); for each Booking tuple 1 page from Clients is read (1000 ×); Sum: 1010 I/O operations

Query languages 1

Algebraic optimization

Enables to use various strategies for join and propagate selections and projection before operation join.

Commutativity of join and Cartesian product

$$E_1 \begin{bmatrix} \theta \end{bmatrix} E_2 \approx E_2 \begin{bmatrix} \theta \end{bmatrix} E_1$$
$$E_1 * E_2 \approx E_2 * E_1$$
$$E_1 \times E_2 \approx E_2 \times E_1$$

Associativity of (theta) join and Cartesian product

 $\begin{array}{l} (\mathsf{E}_1 \ [\theta_1] \ \mathsf{E}_2) \ [\theta_2 \land \theta_3] \ \mathsf{E}_3 \approx \mathsf{E}_1 \ [\theta_1 \land \theta_3] \ (\mathsf{E}_2 \ [\theta_2] \ \mathsf{E}_3), \\ \text{where } \theta_2 \text{ includes attributes only from } \mathsf{E}_2 \text{ and } \mathsf{E}_3 \\ (\mathsf{E}_1 \ ^* \ \mathsf{E}_2) \ ^* \ \mathsf{E}_3 \approx \mathsf{E}_1 \ ^* \ (\mathsf{E}_2 \ ^* \ \mathsf{E}_3) \\ (\mathsf{E}_1 \times \mathsf{E}_2) \times \mathsf{E}_3 \approx \mathsf{E}_1 \times (\mathsf{E}_2 \times \mathsf{E}_3) \end{array}$

Algebraic optimization

 Commutativity of selection and projection If all the attributes from ϕ are in {A₁,...,A_k}, then $E_1[A_1...A_k](\phi) \approx E_1(\phi)[A_1...A_k]$ If $B_1,...,B_s$ are not in ϕ , then $E_1(\phi)[A_1...A_k] \approx E_1[A_1...A_kB_1...B_s](\phi)[A_1...A_k]$ Remark: Propagation of selection to (basic) relations can be used also for operations \cup , -, \times . Commutativity of selection and Cartesian product If all attributes are ϕ are involved in E₁, then $(\mathsf{E}_1 \times \mathsf{E}_2)(\phi) \approx \mathsf{E}_1(\phi) \times \mathsf{E}_2$

Algebraic optimization

Commutativity of selection and union

 $(\mathsf{E}_1 \cup \mathsf{E}_2)(\phi) \approx \mathsf{E}_1(\phi) \cup \mathsf{E}_2(\phi)$

Commutativity of selection and difference

 $(\mathsf{E}_1 - \mathsf{E}_2)(\phi) \approx \mathsf{E}_1(\phi) - \mathsf{E}_2(\phi)$

Remark: Similarly, it is possible to use a projection.

Commutativity of projection and Cartesian product

 $(E_1 \times E_2)[A_1...A_n] \approx E_1[B_1...B_k] \times E_2[C_1...C_m]$

where $\cup_i B_i \cup \cup_i C_i = \cup_i A_i$, B_i concern E_1 and C_j concern E_2 .

Commutativity of projection and union

$$(E_1 \cup E_2)[A_1...A_n] \approx E_1[A_1...A_n] \cup E_2[A_1...A_n]$$

Heuristics for query optimization

- Selections as soon as possible. Use cascades of selections, commutativity of selections with projections and ×, distributiveness of selection over ∪, ∩, - in such way, to get selections as close at possible to leafs.
- Projections as soon as possible. Use cascades of projections, distributiveness of projection over ×, ∪, ∩, - and commutativeness of selection and projection in such way, to get projections as close as possible to leafs. Remove unnecessary projections.
- 3. If possible, transform \times into *. Selection on 1 argument in \times apply earlier.
- Sequence of selections and/or projections replace by one selection, one projection. Use possibilities to do more operations altogether! (pipeline: e.g., if * follows, generate tuples of join)

Query languages 1

Heuristics for query optimization

- Use associativity of *, ×, ∪, ∩ to regrouping relations in the query tree in such way, so that selections producing smaller relations were called earlier.
- Store results of common subqueries (if they are not too big).
 Remark: appropriate for queries on views

D: Find titles of books having copies, which should be returned back until 30.9.2015.

D_{RA}: (LOANS * READERS * COPIES * BOOKS) [TITLE, AUTHOR, ISBN, COPY_ID, NAME, ADDRESS, READER_ID, DATE_BACK] (DATE_BACK < 30.9.2015) [TITLE] Remark: D could originate as the query on view LOANS_INFO SELECT TITLE FROM LOANS_INFO WHERE DATE BACK < 30.9.2015

Transformations:

(1) 2 joins from 3 joins replace by \times ((LOANS × READERS)(L.READER ID = R.READER ID) [COPY ID, READER ID, DATE BACK, NAME, ADDRESS] * ((COPIES × BOOKS)(C.ISBN = B.ISBN) [TITLE, AUTHOR, ISBN, COPY ID, PURCHASE DATE])) [TITLE, AUTHOR, ISBN, COPY ID, NAME, ADDRESS, READER ID, DATE BACK (DATE BACK < 30.9.2015) [TITLE] (2) remove the last * and omit PURCHASE DATE from [] $(A \times B)(COPY ID = COPY ID)$ [TITLE, AUTHOR, ISBN, COPY ID, NAME, ADDRESS, READER ID, DATE BACK (DATE BACK < 30.9.2015) [TITLE]

- (3) Because DATE_BACK is in [] and conditions of selections commutate \Rightarrow
 - (A×B)(DATE_BACK < 30.9.2015)(COPY_ID = COPY_ID)[TITLE]

Remark: unnecessary projections were removed

- (4) Because DATE_BACK is only in A in relation LOANS \Rightarrow
 - ((LOANS(DATE_BACK < 30.9.2015) × READERS)(L. READER_ID = R. READER_ID)[COPY_ID, READER_ID, DATE_BACK, NAME, ADDRESS] × B) (COPY_ID = COPY_ID)[TITLE]

(5) Reduction of projections in () to [COPY_ID] and [COPY_ID,TITLE] ⇒ (LOANS(DATE_BACK < 30.9.2015)[COPY_ID] × (COPIES × BOOKS)(C.ISBN = B.ISBN)[COPY_ID, TITLE]) (COPY_ID = COPY_ID)[TITLE] ⇒ relation READERS disappears

(6) Result in operations selection, projections, and * \Rightarrow

- (LOANS(DATE_BACK < 30.9.2015)[COPY_ID] * (COPIES * BOOKS) [COPY_ID, TITLE])[TITLE]
- The query belongs to the class of SPJ-queries.
- It is possible to optimize them in way to minimalize the number of joins.
- (It is an NP-complete problem.)

Statistics-driven optimization

- Cost estimation for each plan: for each operation, cost and size result estimations are performed
- Information about R* size and indexes is needed.
- A Data catalogues typically contain a description of relation
 R and indexes:
 - > n_R (# tuples) and p_R (# pages)
 - $\succ V(A,R) = |R[A]|$ (tj. |adom_A|)
 - $> p_{RA}$ (# leaf pages B⁺-tree index for R.A).
 - I(A,R) the depth of B⁺-tree for index R.A, min/max values for each B⁺-tree index, 2min_A, 2max_A (the second lowest, resp. highest value in adom_A)
- Solution And A Control A Control

through the index

Result size estimation and reduction factors

SELECT list_of_attributes FROM list_of_relations WHERE atom₁ AND ... AND atom_k

- Maximum # tuples in result is given by a product of relations cardinalities being in the FROM clause.
- Reduction factor (RF) associated with each atom reflects the impact of the atom in reducing result size.
- Result cardinality = Max # tuples * product of all RF.
- Implicit assumption: terms are independent!

Estimation of size result and RFs

SELECT list of attributes FROM list of relations WHERE atom₁ AND ... AND atom_k

✤atom A=k

- > RF = 1/V(A.R), given index on A
- » RF = 1/10 index does not exist

✤atom A=B

- » RF = 1/MAX(V(A,R), V(B,S)), given indexes on A and B
- » RF = 1/V(A,R) given an index on A
- » RF = 1/10 no index exist

✤atom A>k

- » RF = (2max-k)/(2max-2min), given an index A
- > RF < $\frac{1}{2}$ if A is not of integer type or index does not exist

Optimization using rough estimation of RFs

Strategy: estimations of RF for operators Ex.: rough estimations by constants $RF_{=} = 20\%$, $RF_{>} = 40\%$ \Rightarrow FLIGHT.Cost > 26.000 (1)FLIGHT.Cost > 7.000(2)have the same RF, because evidently RF1_{>real} < RF2_{>real}

Example: Informix Online

Assumptions: i-attribute is attribute with index, *k* is constant, *m* is estimation of subquery size.

selekční condition R.i-attribute = kR.i-attribute IS NULL R.i-attribute = S.i-attribute i-attribute > k i-attribute < k attribute = expression attribute = NULL attribute LIKE expression Query languages 1

<u>RF</u>

1/10

1/5

1/V(R.i-attribute, R)
1/max(V(R.i-attribute,R), V(S.i-attribute,S))
(2max - k)/(2max -2min)
(k -2min)/(2max -2min)

Example: Informix Online

<u>Selection condition</u> attribute > expression attribute < expression EXISTS subquery

NOT selection selection₁ AND selection₂ selection₁ OR selection₂

attribute IN list-of-values attribute θ ANY subquery

<u>RF</u>

1/3 1, if there is estimation, that TRUE 0, otherwise $1-RF_{selection}$ $RF_{selection1} * RF_{selection2}$ $RF_{selection1} + RF_{selection2} - RF_{selection1} * RF_{selection2}$ \Leftrightarrow attribute = k₁ OR ... attribute = k_m \Leftrightarrow attribute θ k₁ OR ... attribute θ k_m

Statistics driven optimization

Histograms

- the assumption of uniform distribution is not real in applications
- a histogram on attribute is constructed by partitioning the data distribution D into mutually disjoint subsets called buckets and approximating the frequencies f and values V in each bucket in some common fashion, i.e., histograms approximate real data distribution
- they are maintained by DBMS
- Kinds of histograms
 - Equi-width: divides value range of the column into intervals supposing, that value distribution in interval is uniform
 - Equi-depth: number of tuples in interval is appr. of the same size

Statistics driven optimization



9.0

5

9

Enumeration of alternative paths

Two main cases:

- plans for a single relation
- plans for more relations
- queries over single relation are composed from operations selection, projection (and aggregation operations):
 - each available access path (scanning file/index) is considered and the one with the least estimated cost is chosen.
 - Two different operations can be performed altogether (e.g., when an index is chosen for selection, projection is done for each selected tuple and tuples are moved (pipelined) into aggregation calculation).

Example: System R

- Assumptions: Simple query q over relation R, some attributes with index, V(A, R)
- indexes:
 - > clustered (R(A=c) is \approx in minimal amount of pages)
 - > unclustered (R(A=c) is \approx in n_R/V(A,R) pages)
- Method: choose the cheapest strategy from (1)-(8) and on the result use the rest of conditions from q
- (1) A = c, where there is a clustered index for A
 - Cost: $p_R/V(A,R)$
- (2) A θ c, where $\theta \in \{\ge, \le, <, >\}$ and there is a clustered index for A Cost: $p_R/2$
 - Remark: for \neq it is necessary to read \approx entire R \Rightarrow (5)

Example: System R

(3) A = c, where for A there is unclustered index
 Cost: n_R/V(A,R)
 (4) When D is a acquirential file, then the entire D is

(4) When R is a sequential file, then the entire R is read.

Cost: p_R

(5) when R "mixed" with other relations and there is a clustered index for arbitrary attribute (group of attributes), then the whole R is read "over" it.

Cost: p_R

(6) A θ c, where $\theta \in \{\ge, \le, <, >\}$ and for A there is unclustered index Cost: $n_R/2$

Example: System R

(7) If there is any unclustered index, the entire R is read "over" it.
 Cost: n_R

- (8) (1)-(7) are not applicable. Then all pages potentially containing R are read.
 - Cost: $\geq n_R$

Remark: A = c AND B=d and there is index on A and B as well.
A better strategy would be "over both indexes" ⇒ intersection of two lists of pointers

Estimation of the plan cost for one relation – more precisely with RF

- Index on primary key A satisfies an equality: Cost: I(A,R)+1 for B⁺-tree, about 1.2 for hashed index.
- Clustered index I satisfies 1 or more comparisons:

 $(p_{R,A} + p_R)$ * product RF of satisfying selections.

Non-clustered index I satisfies 1 or more selections:

 $(p_{R,A} + n_R)$ * product RF of satisfying selections. rightarrow projections were performed without elimination of duplicates!

Example

SELECT C.client_ID FROM Clients C WHERE C.category=8

There is an index on category:

 $(1/V(A,R))*n_{c} = (1/10) * 40000$ tuples should be selected.

> clustered index: $(1/V(A,C)) * (p_{C.category} + p_C) = (1/10) * (50+500)$ pages ϵ_{31} elected.

> unclustered index: $(1/V(A,C)) * (p_{C.category} + n_C) = (1/10) * (50+40000)$ pages are selected.

There is an index on *client_ID*:

All tuple/pages should be read. Index is not usable. The whole file C (500) is scanned.

- Since the number of joins is increasing, the number of alternative plans is quickly increasing; it is necessary to restrict the search space.
 - For *n* relations R_1, \dots, R_n the number of plans is (2(n-1))!/(n-1)!, e.g., for n=7 it is 665280.
- Solution: using dynamic programming;
- Recursively calculate cost of each plan. Choose the cheapest of the 2ⁿ 2 alternatives.
- ✤ Basic case for recursion: Access plan for particular relation.

 \geq apply all selections on R_i using the best choices of indexes on R_i.

When the plan for any subset is computed, store it and reuse, when it is required again. Thus, it is not necessary to generate all join orders.

Query languages 1

procedure findbestplan(S) if $(bestplan[S].cost \neq \infty)$ return bestplan[S]//else: *bestplan*[S] ještě was not calculated, calculate it now if (S contains only 1 relation) set the *bestplan*[S].*plan* and *bestplan*[S].*cost* according to the best access to S else for each $S1 \subset S$ such that $S1 \neq \emptyset$ and $S1 \neq S$ P1 = findbestplan(S1)P2= findbestplan(S - S1) A = the best algorithm for join of results P1 and P2 cost = P1.cost + P2.cost + cost Aif cost < bestplan[S].cost then</pre> bestplan[S].cost = cost bestplan[S].plan = "call P1.plan; call P2.plan; join results P1 and P2 by algorithm A" **return** *bestplan*[S]

Complexity: $O(3^n)$ **

Query languages 1

- Section System R: for * only those linear trees are considered, which are of type left-deep.
 - Df.: linear: each non-leaf node has at least one child from $\, R \,$
 - Df.: left-deep: each right-hand-side child is from R
- ✤ left-deep joins enable generate *fully piplined* plans.
 - Intermediate results have to be not stored into temporary files
 - Remark: not all left-deep plans are fully pipelined (depends on the algorithm of join operation, e.g., sort-merge)
- It is not necessary to generate all join orders. Using dynamic programming, the cheapest alternative is generated only once for each subset {R₁, ..., R_n} and stored.

Remark: There are $O(n^*2^n)$ left-deep plans.





nelinear trees

linear trees

Query languages 1

Enumeration on left-deep plans

Left-deep plans distinguish only in order of relations, access method for each relation and method of a join for each relation.

Algorithm modification:

- ➢ replace "for each S1 ⊆ S such that S1 ≠ Ø and S1 ≠ S"
- by expression "for r ∈ S Let S1 = S - r"
- Enumerated using *n* passes (if *n* relations joined):
 - > Pass 1: Find the best 1-relation plan for each relation.
 - Pass 2: Find the best way to join result of each 1-relation plan (as outer) to other relation (all 2-relation plans)
 - Pass n: Find the best way to join the result of the (n-1)-relation plan (outer) to the *n*th relation (all *n*-relation plans)
- Time complexity is O(n2ⁿ) Query languages 1

Finding "the best" left-deep plan

```
procedure findbestplan(S)
  if (bestplan[S].cost \neq \infty) return bestplan[S]
               //else: bestplan[S] has not yet been calculated, calculate
                      it now
  if (S contains onlyt 1 relation)
        set bestplan[S].Plan and bestplan[S].cost according
        to the best access to S
   else for r \in S
       let S1 = S - r
       P1= findbestplan(S1)
       P2= findbestplan(S - S1)
       A = the best algorithm for join of results P1 and P2
       cost = P1.cost + P2.cost + cost A
       if cost < bestplan[S].cost then
                bestplan[S].cost = cost
                bestplan[S].Plan = "call P1.plan; call P2.plán;
                                     join results P1 and P2 by algorithm A"
  return bestplan[S]
Query languages 1
                                                                             38
```

Calculation of left-deep plans



For each subset of relations only the cheapest plan (for each *interesting tuple ordering* - see sorting, merging, group by).



The plan with B⁺-tree (sorted by category) is held

➢ Booking: B⁺-tree agrees on flight_n=100; the cheapest.
Pass 2:

We consider each plan retained from Pass 1 as the outer and consider, how to join it with the other relation

Booking as the outer: by hashing to Clients tuples, that satisfy client_ID = value of client_ID of outer tuple.



We consider each plan retained from Pass 1 as the outer and consider, how to join it with the other relation

Query languages 1

Query blocks: units of optimization

 Query in SQL is split into a collection of *block queries*, which are optimized always 1 block in time. SELECT C.name FROM Clients S WHERE C.age IN (SELECT MAX (S2.age) FROM Clients S2 GROUP BY S2.category)

outer block nested block

- A nested block corresponds
 (simply) to a procedure call for each tuple from outer block
 - for each block, the following plans are considered:
 - all available access methods for \forall relation in the FROM clause.
 - all trees for left-deep joins (how to join with relations in inner FROM (permutations and join methods are considered)

Nested queries

- Nested block is optimized independently, with the outer tuple considered as providing a selection condition.
- Outer block is optimized with the cost of `calling' nested block computation taken into account.
- Implicit ordering of these blocks means that some good strategies are not considered. The nonnested version of the query is typically optimized better.

```
SELECT C.name
FROM Clients C
WHERE EXISTS
(SELECT *
FROM Booking B
WHERE B.flight_n=103
AND B.client_ID=C.client_ID)
```

```
nested block k optimization:
SELECT *
FROM Booking B
WHERE B.flight_n=103 AND
C.client_ID = outer value
```

Equivalent non-nested query: SELECT C.name FROM Clients C, Booking B WHERE C. client_ID =B. client_ID AND B.flight_n=103

Syntax driven optimization

Ex.: SELECT * FROM Copies (1) WHERE Cost >'40' AND Issue_country = 'GB'

SELECT * FROM Copies (2)
WHERE Issue_country = 'GB' AND Cost >'40'
In some DBMS the evaluation depends of the order of conditions:
The one with the lowest RF is evaluated first.
⇒ variant (2) is more effective than (1).

Syntax driven optimization

How to bypass the optimizer?

Ex.: SELECT * FROM Copies (1) WHERE (Purchase_date >'23.04.99' AND Issue_country = 'GB') OR ISBN = '486';

(SELECT * FROM Copies (2) WHERE Purchase_date >'23.04.99' AND Issue_country = 'GB') UNION (SELECT * FROM Copies WHERE ISBN = '486'); Tendency of optimizer: (1) sequentially, (2) with indexes for subqueries

Query languages 1

Summary

- Query optimization is an important task solved by DBMS.
- Other approaches:
 - based on rules
 - probability algorithms
 - parametrized optimization
- It is necessary to understand optimization, to understand an influence of DB design (relations, indexes) on the load (set of queries).
- Trend: autonomous DBMS with AI.
 - Ex.:: platform Oracle 18c based on machine learning. DB is automatically upgraded, optimizes at run time, DBA is not necessary.